

LECTURE NOTES

PHYSICS

MEGNETISM,

E.M.I.

ALTERNATE CURRENT,

E.M.W.

BY

D.J. SIR

Book - 2

== = ==
"MAGNETISM"

श्री नाथ जी बुक डिपो

ALLEN सत्यार्थ गेट नं. 2

के सामने शॉप नं. 2

Date _____ Page _____

⊗ ⇒ Various source of Magnetic Field :-

- | | |
|---------------------------------|---------------------|
| ① Bar Magnet. | } CONSERVATIVE. |
| ② Earth Magnet. | |
| ③ Moving current. | } NON-CONSERVATIVE. |
| ④ current carrying system. | |
| ⑤ Variable Electric Field. (E). | |

☆ ⇒ Magnetic Field / Mag. Flux density / Mg. Induction: $\star(B)$

(i) "vector" Quantity.

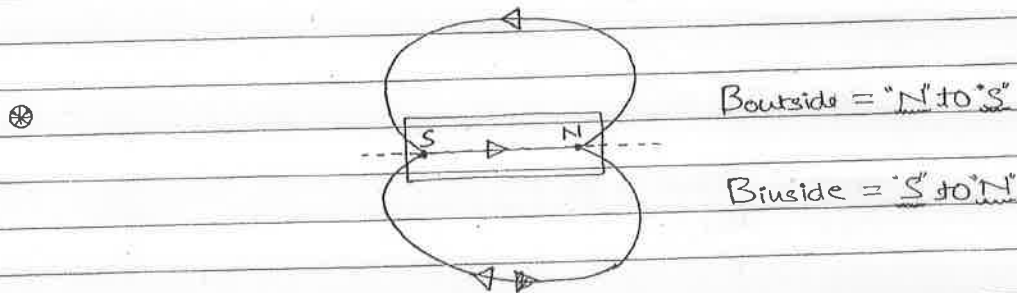
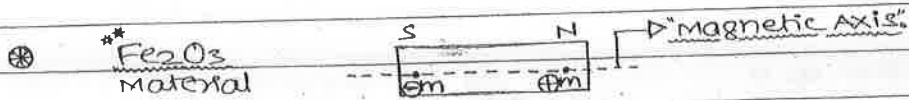
(ii) Unit

→ M.K.S:-	Tesla, $\frac{Wb}{m^2}$, $\frac{N}{Am}$
→ C.G.S:-	Gauss, $\frac{Maxwell}{cm^2}$, $\frac{Dyne}{Ab \times cm}$

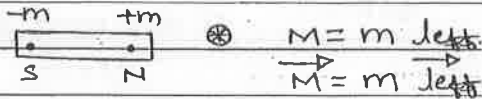
$1 T = 10^4 G$

(iii) It represents strength of magnetic field at given point.

(A) BAR-MAGNET :-



② Magnetic moment of Magnetic Dipole (M) :-



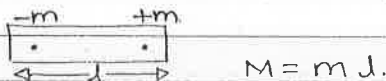
→ Effective = Minimum distance b/w magnetic Poles.
 (-m to +m) "or"
 (S to N)

→ vector quantity.

→ Unit → $A \times m^2$

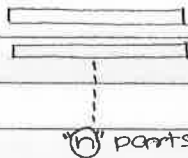
special unit = 1 Bohr magneton (μ_B) = $0.923 \times 10^{-23} \text{ A} \times \text{m}^2$

 Ques → Magnetic moment of a magnet is "M" :-



① If it is cut into "n" equal parts along magnetic axis.

soln :-



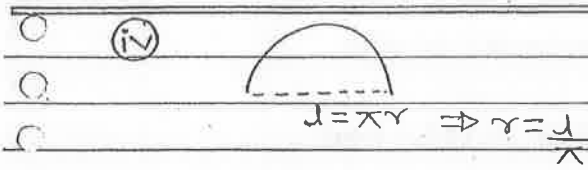
∴ For each small magnet :-

$$m' = \frac{m}{n}$$

$$l' = l$$

$$M' = m'l' = \left(\frac{m}{n}\right) l$$

$$M' = \frac{M}{n}$$

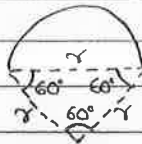


$$M' = (m) (2r)$$

$$= m \left(\frac{2 \times J}{\kappa} \right)$$

$$M' = \frac{2M}{\kappa}$$

NEET 2013 (V)



Angle = $\frac{\text{Arc}}{\text{Radius}}$

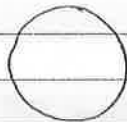
$$\frac{\pi}{3} = \frac{J}{\kappa} \Rightarrow r = \frac{3J}{\kappa}$$

$$M' = (m) (r)$$

$$= m \left(\frac{3J}{\kappa} \right)$$

$$M' = \frac{3M}{\kappa}$$

(vi)



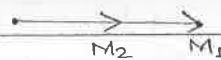
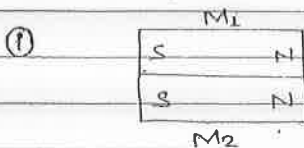
$m' = m$

Effective = 0

$$M' = 0$$

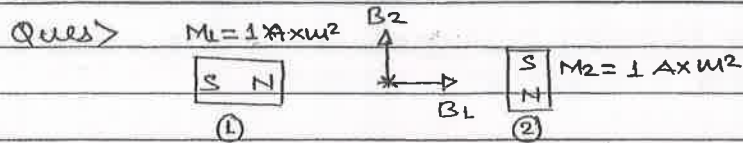
(vii) Toroid = 0

① COMBINATION OF MAGNET :-



$$M_{\text{net}} = M_1 + M_2$$

**sum positn



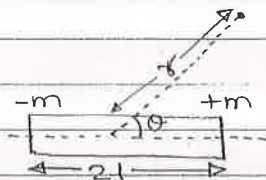
$B_{\text{net}} = ?$

soln: $B_1 = \frac{\mu_0 \cdot 2M}{4\pi r^3} = \frac{4\pi \times 10^{-7}}{4\pi} \times \frac{2 \times 1}{1^3} = 2 \times 10^{-7} \text{ T}$

$B_2 = \frac{\mu_0 \cdot M}{4\pi r^3} = \frac{4\pi \times 10^{-7}}{4\pi} \times \frac{1}{1^3} = 1 \times 10^{-7} \text{ T}$

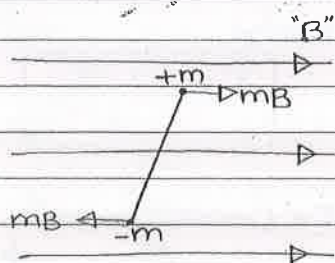
$\therefore B = \sqrt{B_1^2 + B_2^2} = \sqrt{5} \times 10^{-7} \text{ T}$

*** ③ MAGNETIC POTENTIAL DUE TO DIPOLE :-



$$V_m = \frac{\mu_0}{4\pi} \frac{M \cos \theta}{r^2}$$

*** ④ Behaviour in External Uniform Magnetic Field :-



(i) $F_{\text{net}} = 0$

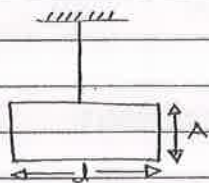
(ii) $\tau = MB \sin \theta$
 $\vec{\tau} = \vec{M} \times \vec{B}$

(iii) $U = -MB \cos \theta$
 $U = -\vec{M} \cdot \vec{B}$

(iv) $W = MB(\cos \theta_1 - \cos \theta_2)$

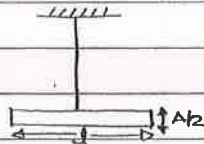
Ques > A magnet is vibrated in a magnetic field, Time period is T , if its half part is vibrated in same field than Time period = ?

soln :-



$$T = 2\pi \sqrt{\frac{I}{MB}}$$

(i) cut along $M \parallel B$ axis :-



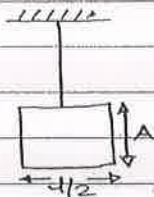
$$T' = 2\pi \sqrt{\frac{I'}{M'B'}}$$

$$= 2\pi \sqrt{\frac{I/2}{(M/2)(B)}}$$

$$T' = T$$

NEEE
(ii)

cut \perp to magnet axis :-



$$T' = 2\pi \sqrt{\frac{I'}{M'B'}}$$

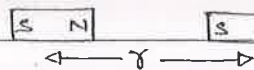
$$= 2\pi \sqrt{\frac{I/8}{(M/2)(B)}}$$

$$T' = \frac{T}{2}$$



Force b/wn dipoles :-

(i)



$$F = \frac{\mu_0}{4\pi} \cdot \frac{6M_1M_2}{r^4} \quad \because F \propto \frac{1}{r^4}$$

(Attractⁿ)

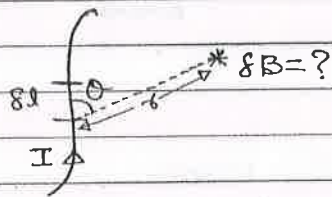
"MAGNETIC EFFECT OF CURRENT"

Date _____ Page _____

→ ~~✓~~ Osted experiment proved that magnetic field is produced around current carrying wire.

★ → BIOT SAVART LAW (B.S.L):-

It is used to calculate magnetic field due to current carrying small element.



$$dB \propto I$$

$$\propto dl$$

$$\propto \sin \theta$$

$$\propto \frac{1}{r^2}$$

$$\therefore dB \propto \frac{I dl \sin \theta}{r^2}$$

$$dB = \frac{\mu_0}{4\pi} \cdot \frac{I dl \sin \theta}{r^2}$$

⇒ vector Form:-

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \vec{r}}{r^2}$$

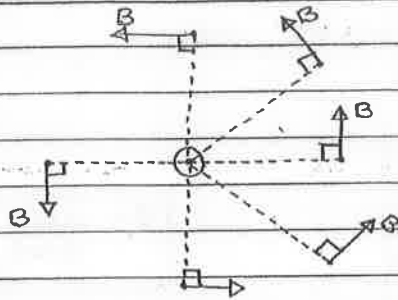
$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \vec{r}}{r^3}$$

$d\vec{l}$ ⇒ current element vector. (directⁿ along the current)

\vec{r} ⇒ Position vector of observation point.

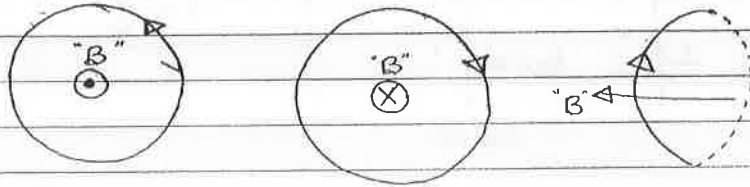
θ ⇒ Angle b/wⁿ these two vectors.

EX :-



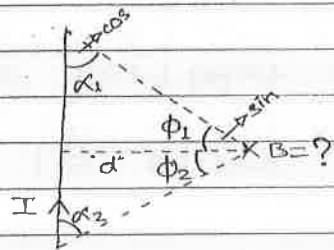
② FOR CLOSED CURRENT :-

If Right Hand fingers are along close current then Thumbs indicates, direction of "B" at centre.



☆ ⇒ MAGNETIC FIELD DUE TO FOLLOWING :-

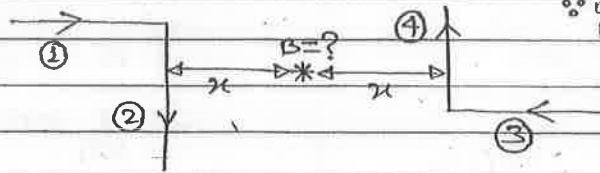
① STRAIGHT CURRENT CARRIENG WIRE :-



$$B = \frac{\mu_0 I}{4\pi d} (\sin\phi_1 + \sin\phi_2)$$

$$B = \frac{\mu_0 I}{4\pi d} (\cos\alpha_1 + \cos\alpha_2)$$

Ques >



∴ Diagram is wrong.
Push ② upto ① level.

Soln :-

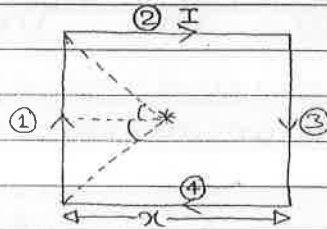
$B_1 = B_2 = 0$ ∴ Along the wire ($\theta = 0^\circ$)

$$\vec{B}_1 = \frac{\mu_0 I}{4\pi x} \odot$$

$$\vec{B}_2 = \frac{\mu_0 I}{4\pi x} \odot$$

$$\vec{B} = \frac{\mu_0 I}{2\pi x} \odot$$

Ques >



∴ $B_{\text{centre}} = ?$

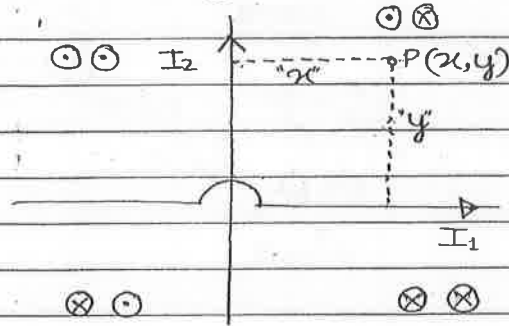
Soln :- $B_1 = \frac{\mu_0 I}{4\pi(x/2)} (\sin 45^\circ + \sin 45^\circ)$

$$\vec{B}_1 = \frac{\mu_0 I}{\sqrt{2}\pi x} \otimes = \vec{B}_2 = \vec{B}_3 = \vec{B}_4$$

$$\vec{B}_{\text{total}} = 2\sqrt{2} \left(\frac{\mu_0 I}{\pi x} \right) \otimes.$$

** Ques > A "Regular Polygon" made up of fixed length of wire l , " n "-sides, " I "-current than; $B_{\text{centre}} = ?$

Ques > Two long wire are along co-ordinate axis as shown. IF point P is Neutral point, than Find its Coords?



i) $\vec{B}_1 = \frac{\mu_0 I_1}{2\pi y}$ ii) $\vec{B}_2 = \frac{\mu_0 I_2}{2\pi x}$

∴ Neutral point :-

∴ $B_{net} = 0$

∴ $B_1 = B_2 \Rightarrow \frac{\mu_0 I_1}{2\pi y} = \frac{\mu_0 I_2}{2\pi x}$

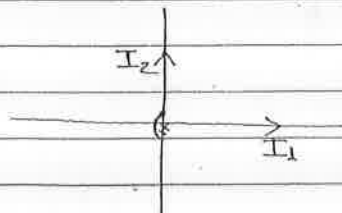
$y = \left(\frac{I_1}{I_2}\right)x \Rightarrow y = m(x) + c$

∴ "straight line" passing through origin (c=0).

∴ Passing through 1st & 3rd co-ordinates.

Ques > Two long wire is along 'x'-axis & 'y'-axis as shown; than Find magnetic field at Height 'd' from origin?

soln



∴ $B_1 \perp B_2$ (given)

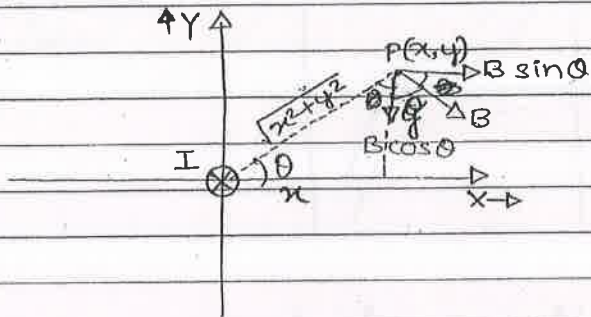
∴ $B = \sqrt{B_1^2 + B_2^2}$

$B = \frac{\mu_0}{2\pi d} \sqrt{I_1^2 + I_2^2}$

∴ $B_1 = \frac{\mu_0 I_1}{2\pi d}$ ∴ $B_2 = \frac{\mu_0 I_2}{2\pi d}$

Ques) A long wire placed at origin and the current "I" in " $-z$ " direction. Then magnetic field at point "P"(x,y) ?

soln:-



$$(i) B_p = \frac{\mu_0 I}{2\pi \sqrt{x^2 + y^2}}$$

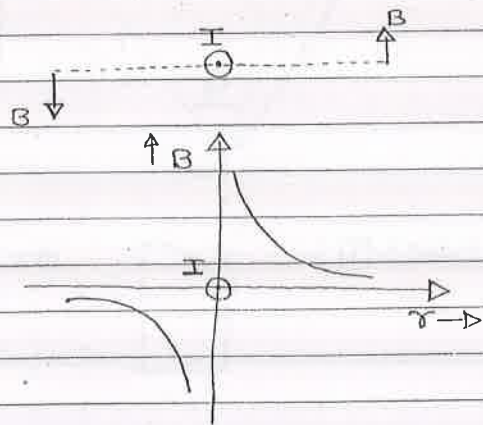
$$(ii) \vec{B}_p = B \sin \theta (\hat{i}) + B \cos \theta (-\hat{j})$$

$$= \frac{\mu_0 I}{2\pi \sqrt{x^2 + y^2}} \left\{ \frac{y}{\sqrt{x^2 + y^2}} \hat{i} - \frac{x}{\sqrt{x^2 + y^2}} \hat{j} \right\}$$

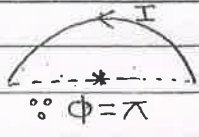
$$\vec{B}_p = \frac{\mu_0 I}{2\pi (x^2 + y^2)} (y\hat{i} - x\hat{j})$$

*** $\otimes \Rightarrow$ GRAPH:-

$$B \propto \frac{\mu_0 I}{2\pi r} \propto \frac{1}{r}$$

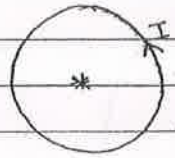


Case:- (II):



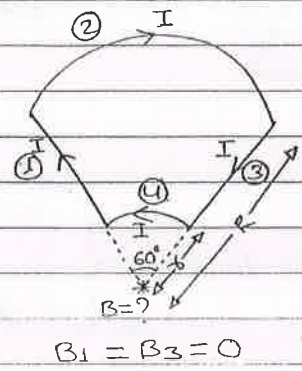
$$B = \frac{\mu_0 I}{4r} \downarrow$$

Case:- (III):



$$B = \frac{\mu_0 I}{2r} \downarrow$$

* Ques >



$$B_2 = \frac{\mu_0 I (\pi/3)}{4\pi R}$$

$$\vec{B}_2 = \frac{\mu_0 I}{12R} \otimes$$

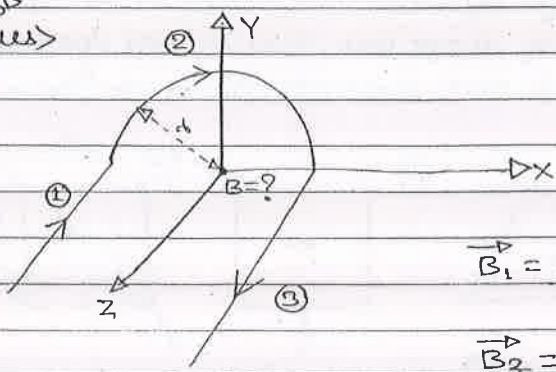
$$\vec{B}_4 = \frac{\mu_0 I}{12r} \odot$$

$$B_1 = B_3 = 0$$

$$\vec{B}_{center} = \frac{\mu_0 I}{12} \begin{pmatrix} 1 & -1 \\ r & R \end{pmatrix} \otimes \downarrow$$

$$= \frac{\mu_0 I}{12} \begin{pmatrix} l - l \\ R & r \end{pmatrix} \otimes \downarrow$$

AIPMT 2015
Ques >



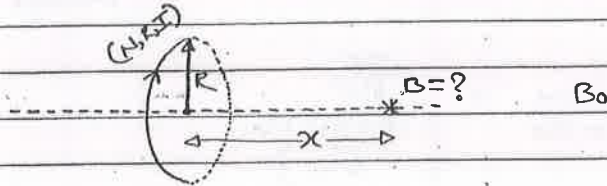
$$\vec{B}_1 = \frac{\mu_0 I}{4\pi r} (-\hat{j})$$

$$\vec{B}_3 = \frac{\mu_0 I}{4\pi r} (-\hat{j})$$

$$\vec{B}_2 = \frac{\mu_0 I}{4r} (-\hat{k})$$

$$\therefore \vec{B} = -\frac{\mu_0 I}{4r} \left(\hat{k} + \frac{2}{\pi} \hat{j} \right) \downarrow$$

© CIRCULAR CURRENT CARRIENG "RING" :-



$$B_{axis} = \frac{\mu_0 N I R^2}{2(R^2 + x^2)^{3/2}} \quad \because x \uparrow \Rightarrow B_{axis} \downarrow$$

$$B_{axis} = \frac{B_0}{(1 + x^2/R^2)^{3/2}}$$

case: (I) :- At centre ($x=0$) :-

$$B_0 = \frac{\mu_0 N I}{2R} = B_{max} \quad \because \text{By Binomial Theorem.}$$

case: (II) :- At nearby points ($x \ll R$)

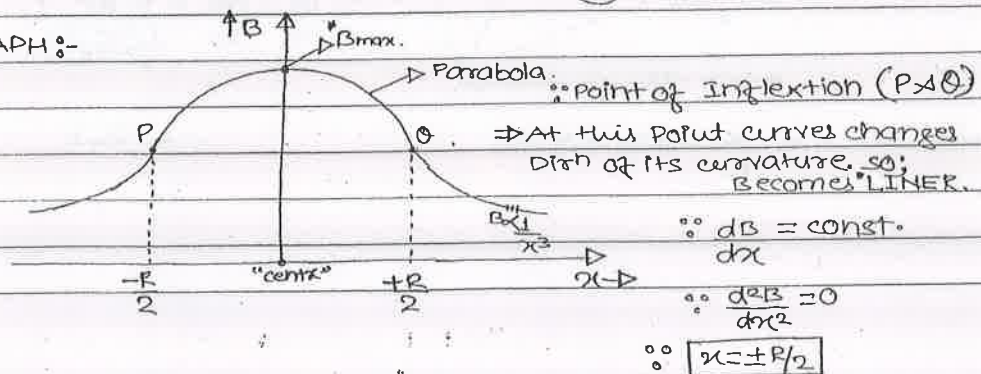
$$B_{axis} = B_0 \left(1 + \frac{x^2}{R^2}\right)^{-3/2}$$

$$B_{nearby} = B_0 \left[1 - \frac{3x^2}{2R^2}\right]$$

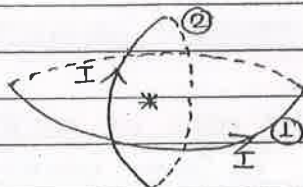
case: (III) :- For Far Away points ($x \gg R$)

$$B_{Far\ Away} = \frac{\mu_0 N I R^2}{2x^3} \propto \frac{1}{x^3}$$

\Rightarrow GRAPH :-



Ques) Two Ring (N, R, I) are \perp to each other, than
 $B_{\text{centre}} = ?$



Soln :-

$$B_2 = \frac{\mu_0 N I}{2R}$$

$$B_1 = \frac{\mu_0 N I}{2R}$$

$$B_{\text{centre}} = \sqrt{2} \left(\frac{\mu_0 N I}{2R} \right)$$

IMP

\Rightarrow If coil (N, R) is made of fix length of wire,

$$l = N(2\pi R)$$

$$\boxed{N \propto \frac{l}{R}}$$

Ques) Two circular coils same Radius and same current and turns are N_1 & N_2 ; than at the centre; $B_1 = ?$
 B_2

$$\text{Soln :- } B = \frac{\mu_0 N I}{2R} \propto N \Rightarrow \frac{B_1}{B_2} = \frac{N_1}{N_2}$$

Ques) If circular coil of N_1 turns is converted into N_2 turns and current's remains the same; than $B_1 = ?$
 B_2 at centre

$$\text{Soln :- } B = \frac{\mu_0 N I}{2R}$$

IMP

$$\text{Fix length of wire} \Rightarrow \boxed{N \propto \frac{l}{R}}$$

$$B \propto N \cdot N$$

$$\boxed{B \propto N^2}$$

$$\Rightarrow \boxed{\frac{B_1}{B_2} = \frac{N_1^2}{N_2^2}}$$

$$\textcircled{iii}^{**} \quad \begin{array}{c} H = B = B_{\text{vacuum}} \\ \mu \quad \mu_0 \end{array}$$

☆ \Rightarrow AMPERE'S CIRCUITAL LAW (ACL) :-

"LINE Integration" of magnetic field along a closed path is Equal to μ_0 -times of total current enclosed in that Path.

$$\therefore \oint \vec{B} \cdot d\vec{l} = \mu_0 \Sigma I \quad \xrightarrow{\text{1st FORM}} \quad \therefore \oint \vec{E} \cdot d\vec{s} = \frac{\Sigma q}{\epsilon}$$

$$\oint \mu_0 \vec{H} \cdot d\vec{l} = \mu_0 \Sigma I$$

$$\therefore \oint \vec{H} \cdot d\vec{l} = \Sigma I \quad \xrightarrow{\text{2nd FORM}}$$

E.M.F = work for Rotating "unit charge" in a "close loop".

$$= W_{\text{closed loop}}$$

q

$$= \oint \vec{F} \cdot d\vec{l} \Rightarrow \oint q \vec{E} \cdot d\vec{l}$$

q

q

$$E.M.F = \oint \vec{E} \cdot d\vec{l}$$

SO; FROM HERE :-

\Rightarrow "M.M.F" (Magneto motive Force)

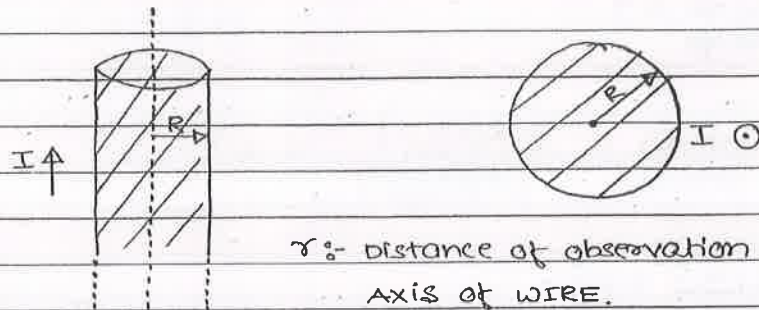
$$\textcircled{i} \quad M.M.F = \oint \vec{H} \cdot d\vec{l}$$

\textcircled{ii} UNIT \rightarrow Amperes.

$$\textcircled{iii} \quad E.M.F = \text{ohm.}$$

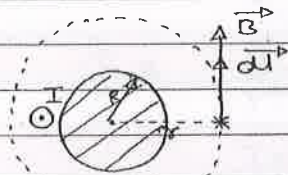
M.M.F

② SOLID CYLINDRICAL WIRE :-



r :- distance of observation point from axis of wire.

① case: ① $r > R$:-



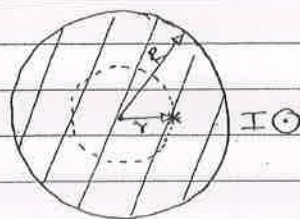
$$\oint B dl \cos 0 = \mu_0 \Sigma I$$

$$B (2\pi r) = \mu_0 I$$

$$B_{\text{outside}} = \frac{\mu_0 I}{2\pi r} \propto \frac{1}{r}$$

$$B_{\text{surface}} = \frac{\mu_0 I}{2\pi R}$$

② case: ② $r < R$:-

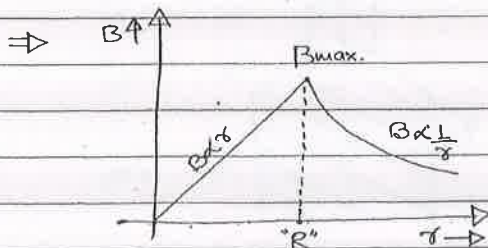


$$\oint B dl \cos 0 = \mu_0 \Sigma I$$

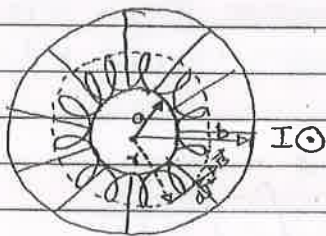
$$B (2\pi r) = \mu_0 \left\{ I \times \frac{\pi r^2}{\pi R^2} \right\}$$

$$B_{\text{inside}} = \frac{\mu_0 I r}{2\pi R^2} \propto r$$

$$B_{\text{axis}} = 0$$



Ques) cross section of cylindrical wire is shown.
Find magnetic field at "r" distance from axis?



soln:- (i) $r > b$:-

$$B = \frac{\mu_0 I}{2\pi r}$$

(ii) $r = b$:-

$$B = \frac{\mu_0 I}{2\pi b}$$

ATIEEE

(iii) $a < r < b$:-

$$\oint B \cdot dl \cos 0^\circ = \mu_0 \sum I$$

$$B(2\pi r) = \mu_0 \left[\frac{I}{\pi b^2 - \pi a^2} \right] [\pi r^2 - \pi a^2]$$

$$B = \frac{\mu_0 I}{2\pi r} \left\{ \frac{r^2 - a^2}{b^2 - a^2} \right\}$$

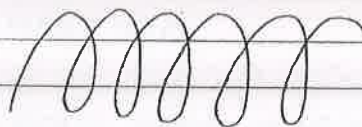
(iv) $r < a$:-

$$\sum I = 0 \Rightarrow B = 0$$

④ SOLENOID / ELECTROMAGNET :-



coll.

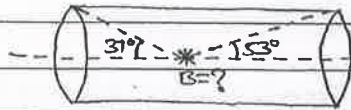


solenoid.

⇒ If Nothing given than considered as Infinite solenoid.

Date _____ Page _____

* Ques >



∴ Total Turns = 5000

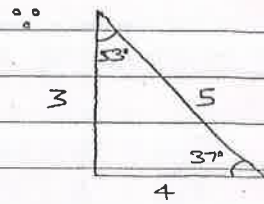
∴ Length of Frame = 50 cm.

∴ current = 1 A.

soln:-
$$B = 4\pi \times 10^{-7} \left\{ \frac{5000}{0.5} \right\} (1) [\cos 37^\circ - \cos(\pi - 53^\circ)]$$

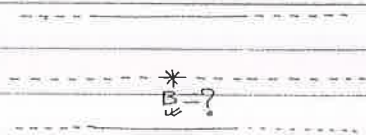
$$B = 2\pi \times 10^{-3} \left[\frac{4+3}{5} \right]$$

$$B = \frac{14\pi \times 10^{-3}}{5} \text{ T}$$



(B) LONG SOLENOID (INFINITE):-

(i) At AXIS:-



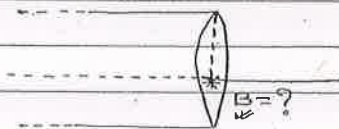
∴ $\alpha = 0$

∴ $\beta = 180^\circ$

IMP

$$B_{\text{axis}} = \mu_0 n I$$

(ii) At END:-



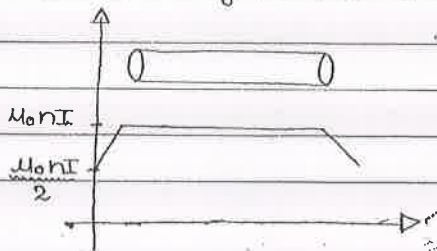
∴ $\alpha = 0^\circ$

∴ $\beta = 90^\circ$

IMP

$$B_{\text{end}} = \frac{\mu_0 n I}{2}$$

*** EX:- For long solenoid:-



$$* \textcircled{i} \quad F_m \perp V$$

\Rightarrow circular motion.

radius (r) :-

$$\frac{mv^2}{r} = qvB$$

$$r = \frac{mv}{qB}$$

$$r = \frac{p}{qB} = \frac{\sqrt{2m(k.E)}}{qB}$$

Momentum.

$$r = \frac{\sqrt{2m(q\Delta V)}}{qB}$$

Voltage.

Ques \rightarrow A proton \times α -particle \times Deuterium making circular motion in u.T.F. Find Ratio of their Radius :- $q \uparrow$

- (i) All have same velocity.
- (ii) Same Momentum.
- (iii) same kinetic Energy.

soln

Proton	Deuterium	α -particle
$\left(\begin{smallmatrix} +e \\ m_p \end{smallmatrix} \right)$	$\left(\begin{smallmatrix} +e \\ 2m_p \end{smallmatrix} \right)$	$\left(\begin{smallmatrix} +2e \\ 4m_p \end{smallmatrix} \right)$
r_p	r_d	r_α

$$\textcircled{i} \quad r = \frac{mv}{qB} \times \left(\frac{m}{q} \right) \Rightarrow \frac{m_p}{e} : \frac{2m_p}{e} : \frac{4m_p}{2e}$$

$$= 1 : 2 : 2$$

(P) (d) (α)

$$\textcircled{ii} \quad r = \frac{p}{qB} \propto \frac{1}{q} \Rightarrow \frac{1}{e} : \frac{1}{e} : \frac{1}{2e}$$

$$\Rightarrow 2 : 2 : 1$$

(P) (d) (α)

$$\Rightarrow \frac{1}{2} m v^2 = \text{const.}$$

$$\because v = \text{const.}$$

speed = const
velocity \neq const. \checkmark

$\otimes \Rightarrow$ Momentum (\vec{p}):-

$$\vec{p} = m\vec{v}$$

$$\vec{p} \neq \text{const.}$$

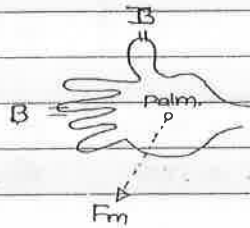
$$|\vec{p}| = \text{const.} \checkmark$$

$\otimes \Rightarrow$ POWER (P):-

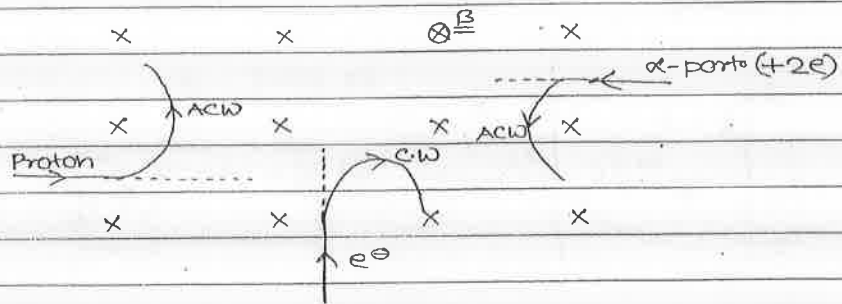
$$P = \vec{F}_m \cdot \vec{v}$$

$$P = 0 \checkmark$$

$\otimes \Rightarrow$ Tool's to Find F_m :-



Eg:-



Soln :- (i) $d \geq r$:-

$$(b-a) \geq \frac{mv}{qB}$$

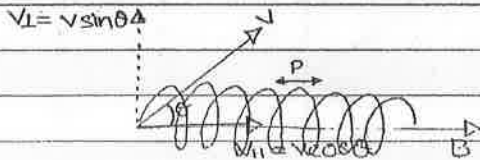
$$\therefore v \leq \frac{qB(b-a)}{m}$$

(ii) $d < r$:-

$$\therefore (b-a) < \frac{mv}{qB}$$

$$\therefore v > \frac{qB(b-a)}{m}$$

(3) $0^\circ < \theta < 90^\circ$



- (i) $v_{\parallel} = v \cos \theta \Rightarrow F_m \neq 0 \Rightarrow$ straight line. }
 (ii) $v_{\perp} = v \sin \theta \Rightarrow F_m \neq 0 \Rightarrow$ circular } **HELIX**

$$\text{radius } (r) = \frac{mv_{\perp}}{qB} = \frac{mv \sin \theta}{qB}$$

$$\text{Time Period } (T) = \frac{2\pi m}{qB}$$

Pitch :- (P) :- Horizontal distance covered by Particle during one Time Period.

$$P = T \times v_{\parallel} \Rightarrow \left(\frac{2\pi m}{qB} \right) v \cos \theta$$

Ques > A charge particle enters in uniform magnetic field at 45° , then find Ratio of Radius & Pitch of its Helical path?

$$\text{soln :- } \frac{r}{P} = \frac{mv \sin \theta / qB}{\frac{2\pi m v \cos \theta}{qB}} = \frac{\sin \theta}{2\pi \cos \theta} \Rightarrow \frac{1}{2\pi}$$

★ \Rightarrow LORENTZ FORCE (F_L):-

It is Net Force on charge particle due to E & B both

$$\begin{aligned} \vec{F}_L &= \vec{F}_e + \vec{F}_m \\ &= q\vec{E} + q(\vec{v} \times \vec{B}) \\ &= q[\vec{E} + (\vec{v} \times \vec{B})] \end{aligned}$$

Ques > A charge particles enter in a region having \vec{E} & \vec{B} and its velocity remains unchanged. Then find condition? (given:- $\vec{E}, \vec{v}, \vec{B}$ are mutually \perp)

soln :- \because velocity = constant.
 \because accⁿ = 0 \Rightarrow $F_{\text{net}} = 0$.

(i) $F_e = F_m$
 $qE = qvB \sin 90^\circ$

$$\boxed{v = \frac{E}{B}}$$

(ii) $\vec{F}_{\text{net}} = 0$

$$\therefore \vec{F}_e + \vec{F}_m = 0$$

$$\therefore q\vec{E} + q(\vec{v} \times \vec{B}) = 0$$

$$\therefore \vec{E} = -(\vec{v} \times \vec{B})$$

$$\boxed{\vec{E} = \vec{B} \times \vec{v}} \quad (Bv \sin \theta)$$

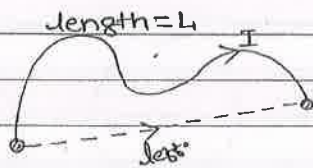
\because (only this Relatn only)

★ Ques > A charge particles enter in Region having \vec{E} and \vec{B} and its path remains straight line, then check various Possibility?

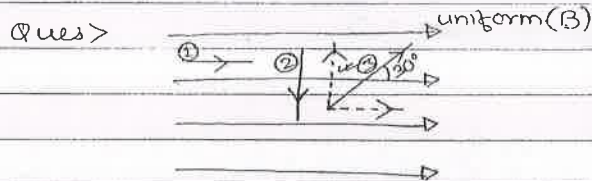
☆ ⇒ MAGNETIC FORCE ON CURRENT CARRYING WIRE :-

⊗ $F_m = I J_{eff} B \sin \theta$
 $\vec{F}_m = I (\vec{J}_{eff} \times \vec{B})$

⊗ J_{eff} :- Min^m distance b/w the ends of wire.
 *(dirⁿ :- From initial to Final Point)

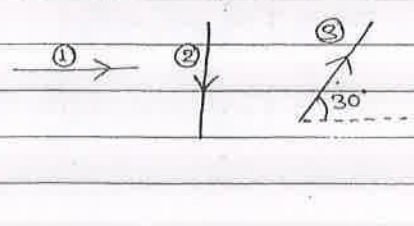


⊗ $F_m \perp J_{eff}$
 $F_m \perp B$



soln :- $F_1 = I l B \sin 0^\circ = 0$
 $F_2 = I l B \sin 90^\circ = I l B \odot$
 $F_3 = I l B \sin 30^\circ = \frac{I l B \otimes}{2}$

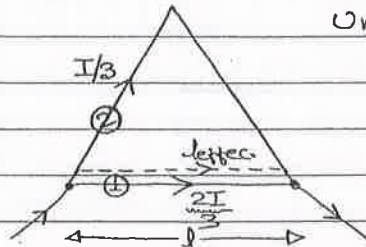
Ques > uniform 'B' ⊗



$F_1 = I l B \sin 90^\circ = I l B \uparrow$
 $F_2 = I l B \sin 90^\circ = I l B \rightarrow$
 $F_3 = I l B \sin 90^\circ = I l B$ (direction)
 ↓
 Angle b/w "I" & "B"

*** Ques > calculate Magnetic Force on Equilateral triangle of side l placed in uniform magnetic field " B " as shown

soln :-



Uniform " B " \otimes

$$\vec{F}_\odot = \left(\frac{2I}{3}\right)(l) B \sin 90^\circ$$

$$\vec{F}_\ominus = \frac{2I l B \uparrow}{3}$$

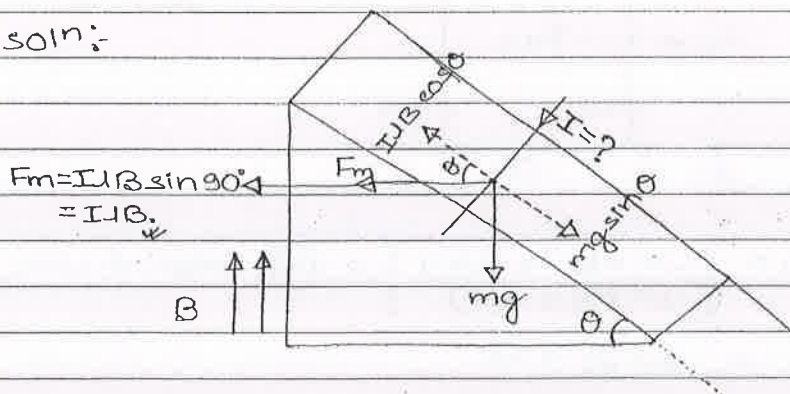
$$\vec{F}_\ominus = \left(\frac{I}{3}\right)(l) B \sin 90^\circ$$

$$\therefore F_{\text{net}} = I l B \uparrow$$

$$\vec{F}_\ominus = \frac{I l B \uparrow}{3}$$

** Ques > A wire (m, l) is placed on an inclined plane as shown. If magnetic field is vertically upward, then calculate current in wire, so that it is just in balance on the inclined plane?

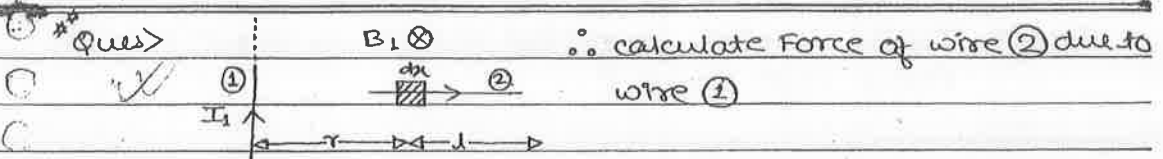
soln :-



At Balance :-

$$mg \sin \theta = I l B \cos \theta$$

$$\therefore I = \frac{mg \tan \theta}{l B}$$



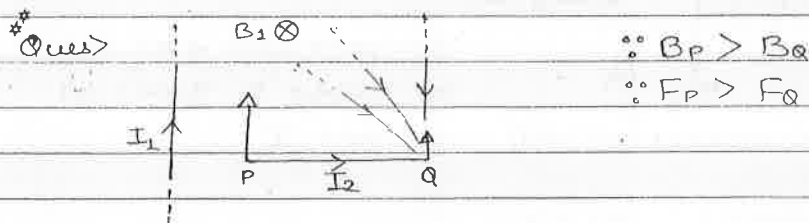
soln :- $F_{2,1} = I_2 \int \mu_0 I_1 \sin 90^\circ$

Force on element of wire (2)

$d F_{2,1} = (I_2)(dx) \left(\frac{\mu_0 I_1}{2\pi r} \right) \sin 90^\circ$

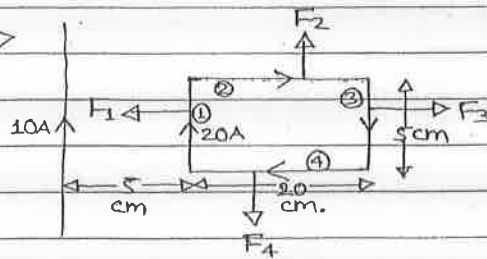
$F_{2,1} = \int_r^{r+l} \frac{\mu_0 I_1 I_2 \cdot dx}{2\pi r}$

$F_{2,1} = \frac{\mu_0 I_1 I_2}{2\pi} \log_e \left(\frac{r+l}{r} \right)$



soln :- Initially wire (2) perform Translatory and Rotation motion both and become Anti-Parallel; After that moves away making Translatory motion only.

Ques \rightarrow



$\therefore \vec{F}_2 = -\vec{F}_4$

$F_1 = \left\{ \frac{4\pi \times 10^{-7} \times 10 \times 20}{2\pi \times (5 \times 10^{-2})} \right\} (5 \times 10^{-2})$

$= 4 \times 10^{-5} \text{ N}$

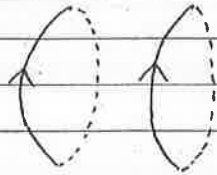
$F_3 = \left\{ \frac{4\pi \times 10^{-7} \times 10 \times 20}{2\pi \times (25 \times 10^{-2})} \right\} (5 \times 10^{-2})$

$= 0.8 \times 10^{-5} \text{ N}$

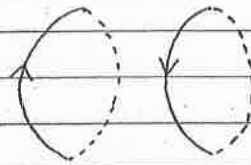
$(F_{net})_{loop} = 3.2 \times 10^{-5} \text{ N}$
[Toward wire (1)]

☆ ⇒ IMPORTANT POINTS:-

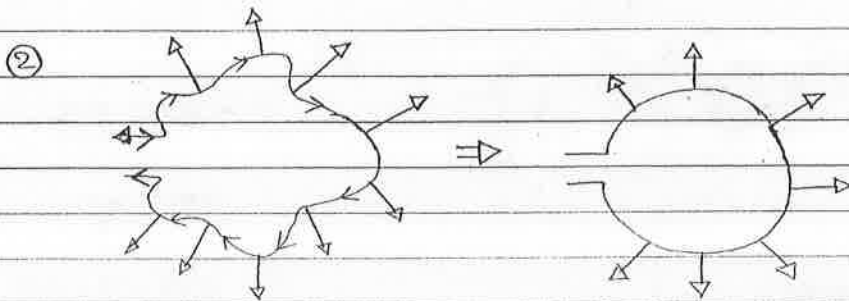
- ① There is magnetic attraction or repulsion between TWO PARALLEL current carrying loop as shown.



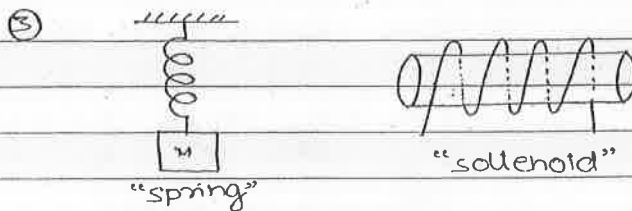
∴ Attraction.



∴ Repulsion.



If current is passed in irregular shape loop made up of flexible wire, then due to repulsion b/w every small section; it converts into circle.



⇒ When "DC" ^{current} is passed in spring or solenoid; then

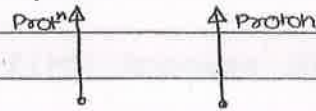
- ① Due to magnetic attraction b/w consecutive turns, it contracts; so length decreases.

$$\Rightarrow F_m = \frac{\mu_0}{4\pi} \frac{q_1 q_2 v_1 v_2}{d^2} \quad (\text{Attraction / Repulsion})$$

$$\Rightarrow \left[\frac{F_e}{F_m} = \frac{1}{\mu_0 \epsilon_0} \frac{1}{v_1 v_2} = \frac{c^2}{v_1 v_2} \right] \because F_e > F_m \text{ (always)}$$

effective.

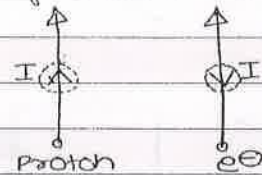
Ques > Two proton moving in same direction in parallel path; as shown.



Soln:- $F_e \neq 0$ (Repulsion)
 $F_m \neq 0$ (Attraction)

$F_{net} \neq 0$ (Repulsion)
 $\because F_e > F_m$

Ques > One proton and one electron moving in same direction in parallel path; as shown



Soln:- $F_e \neq 0$ (Attraction)
 $F_m \neq 0$ (Repulsion)

$F_{net} \neq 0$ (Attraction) $\because F_e > F_m$

★ \Rightarrow MAGNETIC BEHAVIOUR OF CURRENT CARRYING COIL:-

(1) It behaves like "magnetic dipole"; so magnetic poles (N & S) are developed at its faces.

\Rightarrow If I is clockwise \Rightarrow "S" pole
 If I is anticlockwise \Rightarrow "N" pole.

Ques >



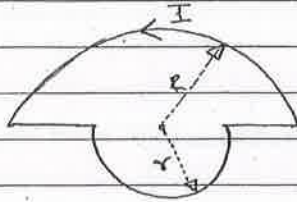
$$M = NIA$$

∴ Area trapped by loop = 0

$$\vec{M} = 0$$

AIPT

Ques >

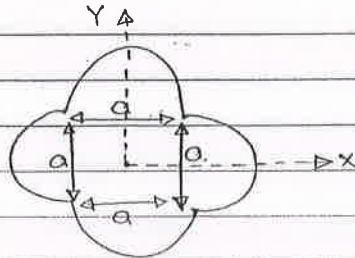


$$M = NIA$$

$$= (L)(I) \left\{ \frac{\pi R^2}{2} + \pi r^2 \right\}$$

$$\vec{M} = \frac{I \pi (R^2 + r^2)}{2} \hat{z}$$

IIT

Ques >
2013

$$M = NIA$$

$$(L)(I) \left\{ a^2 + 2 \left[\pi \left(\frac{a}{2} \right)^2 \right] \right\}$$

$$\vec{M} = I a^2 \left[1 + \frac{\pi}{2} \right] (-\hat{k})$$

Ques > For two circular coils $\frac{M_1}{M_2} = ?$; if(i) same current ; same Radius in term N_1, N_2

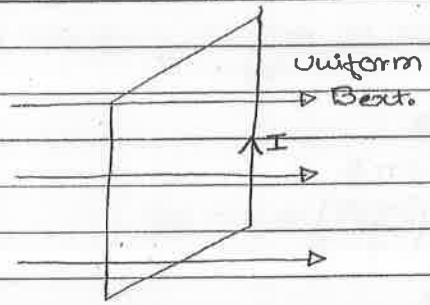
soln:- $M = NIA$

$$M = NI(\pi R^2)$$

$$M \propto N$$

$$\therefore \frac{M_1}{M_2} = \frac{N_1}{N_2}$$

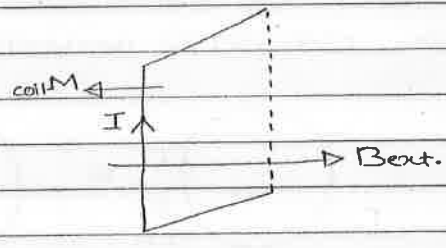
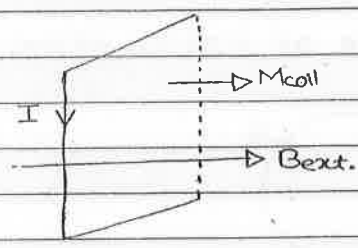
③ Behaviour in Uniform Ext. Mag. Field:-



- (i) $F_{net} = 0$
- (ii) $\tau = MB \sin \theta$
- (iii) $U = -MB \cos \theta$
- (iv) $W_{\theta_1 \rightarrow \theta_2} = MB(\cos \theta_1 - \cos \theta_2)$

Case:- I \Rightarrow If $\theta = 0^\circ$

Case:- II \Rightarrow If $\theta = 180^\circ$



$F = 0$
 $\tau = MB \sin \theta = 0$
 $U = -MB \cos \theta = -MB (\text{min})$

$F = 0$
 $\tau = MB \sin \theta = 0$
 $U = -MB \cos \theta = +MB (\text{Max})$

} stable equib^m } unstable equib^m

- (i) When coil is in equilibrium than its Plane is \perp to the Field.
- (ii) coil is in equilibrium for two configuration only, where; one is stable ($\theta = 0^\circ$) and another is unstable ($\theta = 180^\circ$)

Ques) An Equilateral triangle coil of side "l" and current "I" is placed in uniform field "B", where field is making 30° with plane of coil; than ?

① In same atom at high energy level :-

$$I = \frac{qV}{2\pi r} \propto \frac{L}{n} \cdot \frac{1}{n^2}$$

$$\frac{r}{a_0} = 0.529 \times \frac{n^2}{Z}$$

$$I \propto \frac{L}{n^3}$$

$$v = 2.18 \times 10^6 \frac{Z}{n}$$

Here; $n = \text{orbit no.}$

② $B_{\text{center}} :-$

$$\rightarrow B_{\text{center}} = \frac{\mu_0 I}{2r} = \frac{\mu_0 q f}{2r} = \frac{\mu_0 q \omega}{4\pi r} = \frac{\mu_0 q v}{4\pi r^2}$$

\rightarrow In first orbit of H-atom

$$B_{\text{center}} = \frac{4\pi \times 10^{-7} \times (1.6 \times 10^{-19}) (2.2 \times 10^6)}{4\pi (0.529 \times 10^{-10})^2} = \boxed{12.5} \text{ Tesla}$$

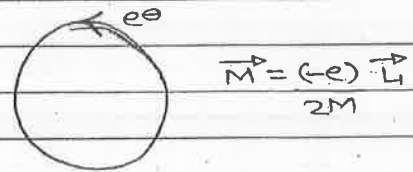
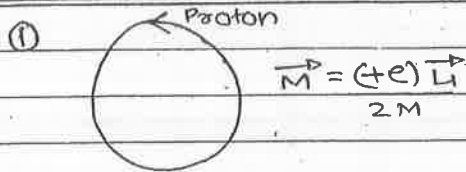
\rightarrow In some atom; upper level :-

$$B = \frac{\mu_0 q v}{4\pi r^2} \propto \frac{L}{n} \cdot \frac{1}{(n^2)^2}$$

$$B \propto \frac{L}{n^5}$$

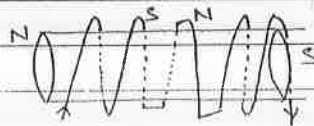
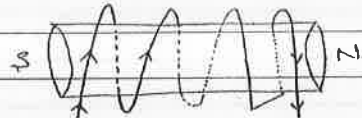
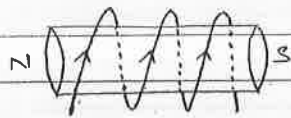
③ Magnetic Moment (M) :-

$$\begin{aligned} \rightarrow M &= NIA = I(\pi r^2) \\ &= \frac{q f \pi r^2}{2} = \frac{q \omega r^2}{2} = \frac{q v r}{2} \end{aligned}$$



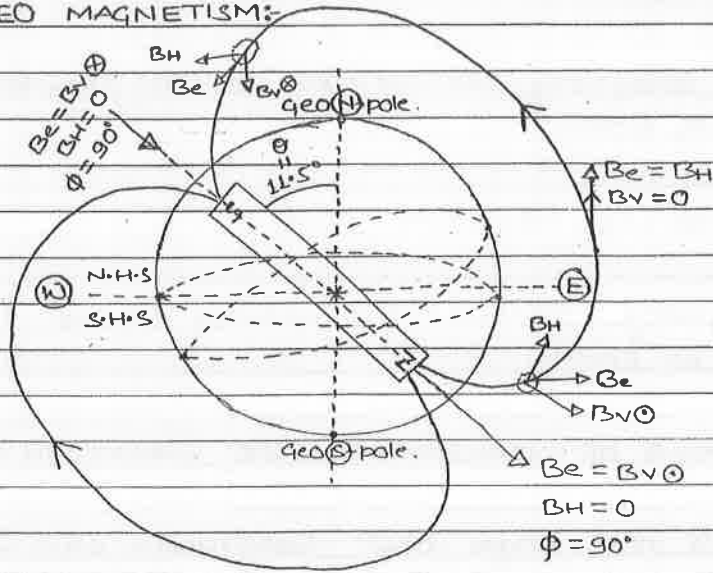
★ → IMPORTANT POINTS:-

More than 2 poles can be developed in solenoid by changing the binding pattern.



3-DAS 3-MD
MAGNETISM

★ ⇒ GEO MAGNETISM:-

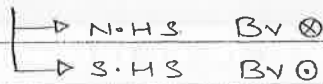


H.M.P.

⇒ Earth magnetic Field (B_e):-

(i) At Poles :- $B_H = 0$

$B_V = B_e$



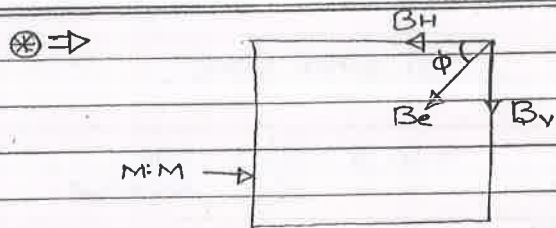
(ii) At center:- $B_V = 0$

$B_H = B_e$

∴ (|| to earth surface & south to north dirn)

(iii) At other place :- $B_H \neq 0$

$B_V \neq 0$



$$B_H = B_e \cos \phi$$

$$B_V = B_e \sin \phi$$

$$\tan \phi = \frac{B_V}{B_H}$$

$$B_e = \sqrt{B_H^2 + B_V^2}$$

Ques > If $B_H = 3 \times 10^{-5} \text{ T}$ and $\phi = 30^\circ$ then :-

- (i) $B_V = ?$ (ii) $B_e = ?$ (iii)

Soln :- (i) $\tan \phi = \frac{B_V}{B_H} \Rightarrow \tan 30^\circ = \frac{B_V}{3 \times 10^{-5}}$

$$B_V = \sqrt{3} \times 10^{-5}$$

(ii) $B_H = B_e \cos \phi$

$$3 \times 10^{-5} = B_e \cos 30^\circ$$

$$B_e = 2\sqrt{3} \times 10^{-5}$$

$\otimes \Rightarrow$ DIP ANGLE :- (ϕ)

(i) Real Dip Angle (ϕ) \Rightarrow Measured in M.M only.

(ii) Apparent Dip Angle (ϕ') \Rightarrow Measured in vertical Plane other than M.M.

Ques > If Real Dip = 35° ; then Apparent Dip = ?

- (i) 32° (ii) 38°
 (ii) 25° (iv) 28° $\because \phi' > \phi$

(ii) If $\alpha = 90^\circ$

$$\tan \phi' = \frac{\tan \phi}{\cos 90^\circ}$$

$$= \frac{\tan \phi}{0} \Rightarrow \tan \phi' = \infty$$

$$\boxed{\phi' = 90^\circ}$$

** \rightarrow In vertical plane \perp to M.M; Apparent Dip is Always 90° , irrespective of Real Dip.

$$\otimes \Rightarrow T = 2\pi \sqrt{\frac{I}{MB}}$$

(i) If Magnet vibrates in Horizontal Plane than;
 $B = B_H$

(ii) If Magnet vibrates in Magnetic Meridian than;
 $B = B_e$

(iii) If Magnet vibrates in vertical Plane \perp to M.M
 than; $B = B_v$

Ques > A Magnet vibrates in M.M; Time Period = 3 sec.
 If same Magnet is vibrated in Horizontal plane
 than Time Period = $3\sqrt{2}$ sec. Then Dip Angle = ?

☆ ⇒ TERMINOLOGIES :-

① Isoclinic Line → same ϕ .

② Aclinic Line → $\phi = 0^\circ$

③ Isogonic Line → same θ .

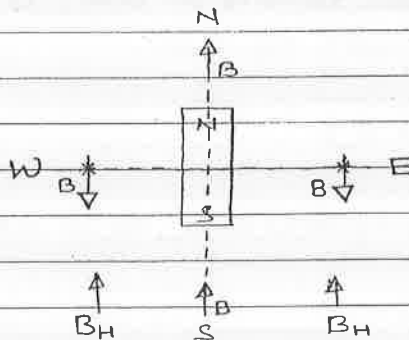
④ Agonic Line → $\theta = 0^\circ$

⑤ Isodynamic Line → same B_H

⑥ Adynamic Line → $B_H = 0$.

☆ ⇒ NEUTRAL POINT ($B_{net} = 0$) :-

① If Magnet is Placed in Horizontal Plane and its North Pole is toward North direction, then;



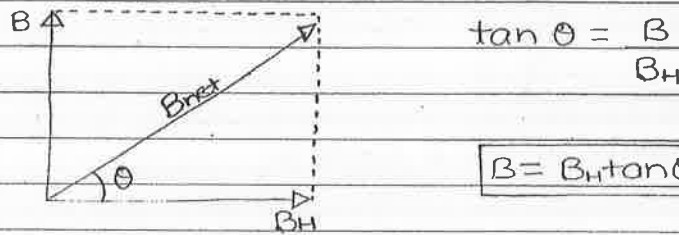
⇒ There are two Neutral Points at Equator. Each at different side ^A at same distance from the Magnet.

→ जिससे Angle बनेगा $\tan \theta$ इसके साथ चिपकेगा।

Date _____ Page _____

★ ⇒ TANGENT LAW :-

When Two Magnetic Fields B & B_H are \perp to each other and Net Magnetic Field makes angle θ with B_H than :-



★ ⇒ MEASURING DEVICE :-

① TANGENT GALVANOMETER :-

① Based on the Tangent Law.

② It is used to measure *small current.

③ Its scale is non-linear.

④ In this; coil remains stationary and Magnet Moves so; it is called "Moving Magnet Galvanometer."

⑤ It is "most sensitive" at the Deflection of 45° .

Ques > In a galvanometer ;

if current = $I \Rightarrow \phi = 30^\circ$

if current = $I' = ? \Rightarrow \phi = 60^\circ$

Soln :- (i) Moving coil (c) :-

$$I \propto \phi$$

$$\frac{I'}{I} = \frac{60}{30} \Rightarrow I' = 2I$$

$$\text{soln :- } \left. \begin{array}{l} M_1 + M_2 \Rightarrow T = 3 \text{ sec.} \\ |M_1 - M_2| \Rightarrow T' = 5 \text{ sec.} \end{array} \right\} \frac{M_1}{M_2} = ?$$

$$T = 2\pi \sqrt{\frac{I}{MBH}} \propto \frac{1}{\sqrt{M}}$$

$$\frac{3}{5} = \sqrt{\frac{M_1 - M_2}{M_1 + M_2}}$$

$$\frac{9}{25} = \frac{M_1 - M_2}{M_1 + M_2}$$

$$\therefore \frac{M_1}{M_2} = \frac{17}{8}$$

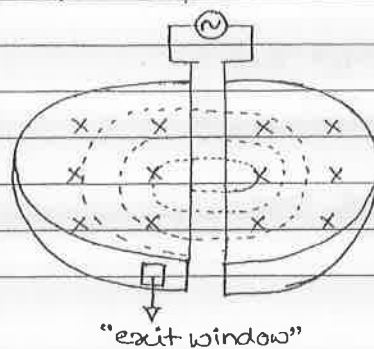
$$\textcircled{\otimes} \text{ "or" } \left. \begin{array}{l} M_1 + M_2 \Rightarrow T = 3 \text{ sec.} \\ |M_2 - M_1| \Rightarrow T' = 5 \text{ sec.} \end{array} \right.$$

$$\frac{3}{5} = \sqrt{\frac{M_2 - M_1}{M_1 + M_2}}$$

$$\therefore \frac{M_1}{M_2} = \frac{8}{17}$$

③ CYCLOTRON :-

⇒ It is used to produce highly energized \oplus ve ions for scientific purpose.



★ ⇒ COSMIC RAYS :-

cosmic Rays are High Energy Protons. so, when it Approaches Toward Earth :-

(i) AT POLES :-

$\therefore v \parallel B_v \Rightarrow F_m = 0$
 \Rightarrow so Reaches at Pole Easily.

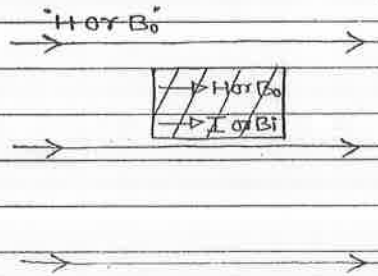
(ii) AT EQUATOR :-

$B_v = 0 \Rightarrow F_m \neq 0$
 $\therefore v \perp B_H$

\Rightarrow so cosmic Rays are deviated ; so can not Reach at the Equator.

④ MAGNETIC PERMEABILITY (μ) :-

It is Ability of material to allow the line of force to pass through it.



Magnetic Field inside Rod

$$B = B_0 + B_i$$

$$\mu H = \mu_0 H + \mu_0 I$$

$$\mu H = \mu_0 H \left(\frac{1 + I}{H} \right)$$

$$\frac{\mu}{\mu_0} = 1 + \frac{I}{H}$$

$$\mu_r = 1 + X$$

* μ_r = Relative Permeability.

* μ = Permeability.

$$\therefore \mu = \mu_0 \mu_r$$

** Qus > A substance of $X = 3 \times 10^{-4}$ is placed in $H = 4 \times 10^4 \text{ A/m}$ than calculate:-

- ① Intensity of Magnetisation.
- ② Relative Permeability of Material.
- ③ permeability of material.
- ④ Magnetic Field inside

"PROPERTY"

- ① $I \propto H$
- ② $\chi = \frac{I}{H}$
- ③ $\mu_r = 1 + \chi$
- ④ $I \propto \sqrt{H}$

⑤ $\chi \propto \frac{1}{T}$ (Curie Law)

"FERRO"

- $I \gg H$ (Along H)
- $\chi \gg 1$ (Positive)
- $(\chi \gg 1)$
- $\mu_r \gg 2$

$I \propto H$



Curie Weiss Law

$$\chi = \frac{C}{T - T_c}$$

$\chi \propto \frac{1}{T}$



* T_c : Curie Temp. After which ferro behavior like para.

- ⑥ state: only solid
- ⑦ Behaviour in Non-uniform Magnetic Field: Moves from weak to strong field (Rapidly)

"** VERY IMPORTANT FOR EXAM"

- "PARAMAGNETIC"
- $I < H$ (Along H)
- $\chi < 1$ (Positive)
- $(0 < \chi < 1)$

$I \propto H$

$I \propto H$



Curie Law

$$\chi \propto \frac{1}{T}$$

$\chi \propto \frac{1}{T}$



$I \propto H$

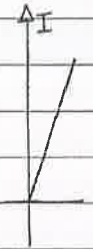
solid, Liquid, Gas

- Moves from weak to strong field (slowly)

"DIAMAGNETIC"

- $I < H$ (Opposite to H)
- $\chi < 1$ (Negative)
- $(-1 < \chi < 0)$
- $0 < \mu_r < 1$

$I \propto H$



$$\chi \propto \frac{1}{T}$$

$\chi \propto \frac{1}{T}$



$I \propto H$

solid, Liquid, Gas

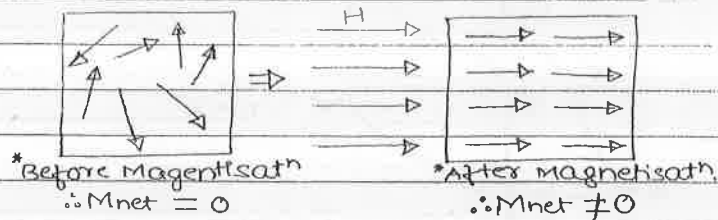
- Moves from strong to weak

☆ ⇒ DIAMAGNETICISM :-

- (i) Material of all paired electrons.
- (ii) Atomic Dipole Moment is zero.
- (iii) It is Inherent Property of each material.
- (iv) It is Explained by orbital motion of electron.

☆ ⇒ PARAMAGNETISM :-

- (i) Material Having un-paired electrons.
- (ii) Atomic Dipole Moment is Non-Zero.



- (iii) It is Explained by "SPIN MOTION" of electron.

☆ ⇒ FERROMAGNETISM :-

- (i) Material of Unpaired electrons.
- (ii) Atomic Dipole Moment is Non-Zero.
- (iii) It is Explained by Domain Theory.

→ correct measure of magnetic hardness of material ⇒ coercivity.

⊗ ⇒ coercivity :-

Date _____ Page _____

(i) It is opposite "H" for complete de-magnetisation.

(ii) Forward coercivity (O-R) = Reverse ^{coarsi} Retentivity (O-U)

⊗ ⇒ At saturation :-

(i) slope of I-H curve = $\frac{dI}{dH} = 0$.

$$\because B = \mu_0(H + I)$$

(ii) slope of B-H curve = $\frac{dB}{dH} = \mu_0(1 + 0) = \mu_0$

* (iii) Area of B-H curve = μ_0 (Area of I-H curve)

⊗ ⇒ Heat Produced in magnetisation & demagnetisation :-

Heat Produced in "t" sec. = $VAnjt$.

V = volume of Rod.

A = Area of "I-H" curve.

"n" = Frequency of magnetisation or demagnetisation.

t = second.

⊗ ⇒ On the basis of "coercivity"; Ferro-material are of 2 types:

SOFT FERRO.

HARD FERRO.

(i) Low coercivity & Retentivity. (ii) High coercivity & Retentivity.

(ii) small B-H area

(ii) Large B-H Area.

(iii) Use for making "Temporary" Magnet & Transformer.

(iii) Use for making Permanent Magnet & Transformer.

(iv) eg:- soft Iron, Perm Alloy.

(iv) eg:- cobalt-steel.

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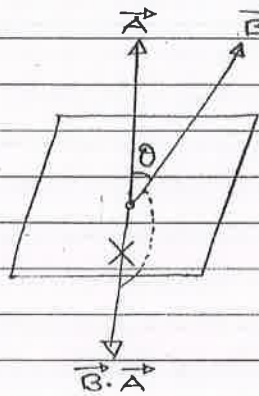
Lined writing area with horizontal lines and a vertical margin line on the left.

Date _____ Page _____

Handwriting practice lines consisting of multiple horizontal lines with a dashed midline. The page contains approximately 25 rows of these lines, starting from the top and ending near the bottom. The lines are evenly spaced and cover most of the page's width.

☆ ⇒ MAGNETIC FLUX (Φ) :-

(i) It is number of Line of Force, passing through surface placed normally in magnetic field.



$$\Phi = \vec{B} \cdot \vec{A}$$

$$\Phi = BA \cos \theta$$

$$\Phi = NBA \cos \theta$$

∴ θ = Angle b/w \vec{A} & \vec{B} (Acute Angle always)

(ii) scalar quantity.

(iii) Unit :- (i) M·R·S = weber (Wb)

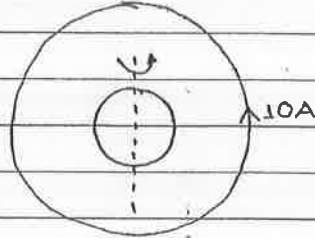
(ii) C·G·S = Maxwell.

∴ $1 \text{ Wb} = 10^8 \text{ Maxwell}$.

Ques > square coil of side 5cm ; turns = 1000, placed in uniform field 100 Tesla. If field is making 30° with loop than magnetic flux ?

Soln :-

$$\begin{aligned} \Phi &= NBA \cos \theta \\ &= (10^3) (10^2) (5 \times 10^{-2})^2 \cos 60^\circ \\ &= 125 \text{ Wb.} \end{aligned}$$

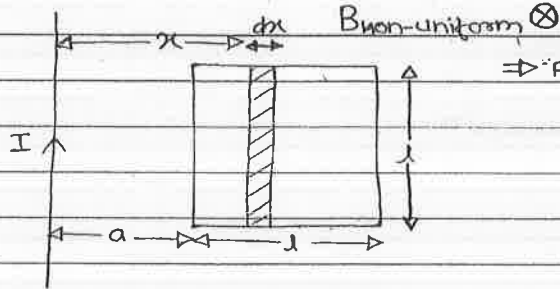


$$\phi_{\text{dot}} = N \text{dot} B \text{dot} A \text{dot} \cos \theta$$

$$= (1) \left(\frac{\mu_0 I}{2 \times 0.628} \times 10 \right) (10^{-4}) \cos \omega t$$

$$= 10^{-9} \cos \omega t$$

$\phi_{\text{wire}} \rightarrow$



\Rightarrow Flux with square coil?

soln: $\phi_{\text{loop}} = N \textcircled{\beta} A \cos \theta$ \times β variable.

\therefore Flux of element area:

$$= (1) \left(\frac{\mu_0 I}{2\pi x} \right) (l dx) \cos 0^\circ$$

$$\phi_{\text{loop}} = \int_a^{a+l} \frac{\mu_0 I}{2\pi} \cdot \frac{dx}{x} \Rightarrow \left[\frac{\mu_0 I l}{2\pi} \log_e \left(\frac{a+l}{a} \right) \right] \downarrow$$

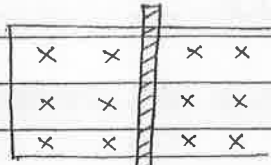
$$\textcircled{\times} \Rightarrow \phi = NBA \cos \theta$$

$$\phi = f(B, A, \theta)$$

(i) If $\phi = \text{const.} \Rightarrow \text{NO E.M.I.} \downarrow$

(ii) If $\phi \neq \text{const.} \Rightarrow \text{E.M.I.} \downarrow$

6



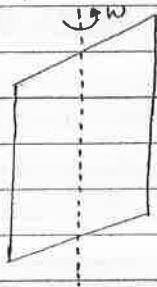
→ Moving Rod.

$\therefore A \neq \text{const.}$

$\therefore \phi \neq \text{const.}$

$\Rightarrow \text{E.M.I.}$

7

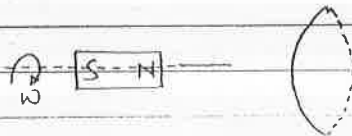


$\therefore \theta \neq \text{const.}$

$\therefore \phi \neq \text{const.}$

$\Rightarrow \text{E.M.I.}$

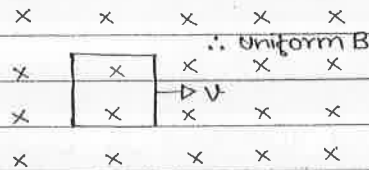
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$\therefore \phi = \text{const.}$

$\therefore \text{NO E.M.I.}$

9

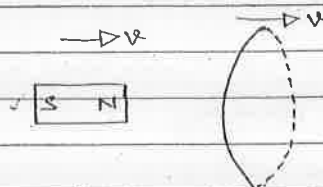


$\therefore \text{uniform B}$

$\therefore \phi = \text{const.}$

$\Rightarrow \text{NO E.M.I.}$

10



$\therefore \phi = \text{const.}$

$\Rightarrow \text{NO E.M.I.}$

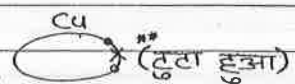
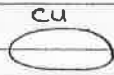
FORMULA'S FOR E.M.F :-

$$\textcircled{1} \quad e = -\frac{d\phi}{dt} \propto (R^0) \quad \therefore [R = \text{Resistance}]$$

$$\textcircled{2} \quad I_{\text{induced}} = \frac{e}{R} = -\frac{1}{R} \frac{d\phi}{dt}$$

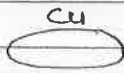
$$\textcircled{3} \quad q_{\text{induced}} = I_{\text{indu.}} dt = -\frac{d\phi}{R}$$

Ques > If $B \neq \text{const.} \Rightarrow \phi \neq \text{const}$



(i) E.M.F :-	✓	✓	✓
(ii) e :-	✓	✓	✓
(iii) I _{induced} :-	✓	X	X

Ques > Two identical loops ; same $\frac{d\phi}{dt} \neq 0$



$$R_{Ag} < R_{Cu}$$

soln :- (i) $e_{\text{ind}} \propto R^0$

$$\therefore e_{Cu} = e_{Ag}$$

$$(ii) I_{\text{induced}} \propto \frac{1}{R}$$

$$\therefore I_{Ag} > I_{Cu}$$

Ques > Flux with a coil;

$$\phi = 6t^2 - 5t + 1$$

than the Induced E.M.F (e) = ?

(i) at; $t = 1 \text{ sec.}$

(ii) at; $t = 0.25 \text{ sec.}$

Soln :- (i) $t = 1 \text{ sec}$

$$e = -\frac{d\phi}{dt}$$

$$e = -(12t - 5)$$

$$= -(12 \times 1 - 5)$$

$$= -7 \text{ volt.}$$

(ii) $t = 0.25 \text{ sec.}$

$$e = -\frac{d\phi}{dt}$$

$$e = -(12t - 5)$$

$$= -(12 \times 0.25 - 5)$$

$$= -2 \text{ volt.}$$

(i) -7v 3 volt

(ii) +7v 7 volt

(iii) +3v 2 volt

(iv) -3v Non of these

(i) -2v 3 volt

(ii) +2v 2 volt

(iii) +3v 7 volt

(iv) -3v Non of these

*Ques > Flux with a coil; $\phi = t^2 e^{-t}$

∴ find instant when induced E.M.F (e) become zero (0)?

Soln :- $\phi = t^2 e^{-t}$

$$e = -\frac{d\phi}{dt}$$

$$e = -[t^2(-e^{-t}) + e^{-t}(2t)]$$

$$0 = - (t) (e^{-t}) [-t+2] \quad \therefore (x, y, z = 0)$$

if $\Rightarrow t = 0 \Rightarrow$ than; $t = 0$

if $\Rightarrow e^{-t} = 0 \Rightarrow$ than; $t = \infty$

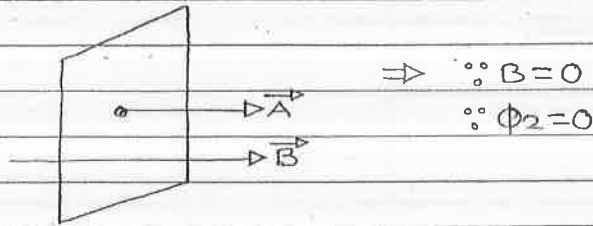
if $\Rightarrow (-t+2) = 0 \Rightarrow$ than; $t = 2$

$t = 2 \text{ sec.}$

$$e = -\frac{d\phi}{dt} \Rightarrow -\left(\frac{\phi_2 - \phi_1}{t}\right) = \frac{NBA}{t}$$

$$q_{\text{induc.}} = \frac{-d\phi}{R} = \frac{NBA}{R}$$

(ii) If coil removed from field in time 't' then:



$$\phi_1 = NBA \cos 0^\circ = NBA$$

$$e = -\frac{d\phi}{dt} = \frac{NBA}{t}$$

$$q_{\text{ind.}} = \frac{-d\phi}{R} = \frac{NBA}{R}$$

** Ques > A square loop is moving with constant velocity in a uniform magnetic field as shown (P.T.O) ?

$$= -B \cdot \pi \cdot 2r \frac{dr}{dt}$$

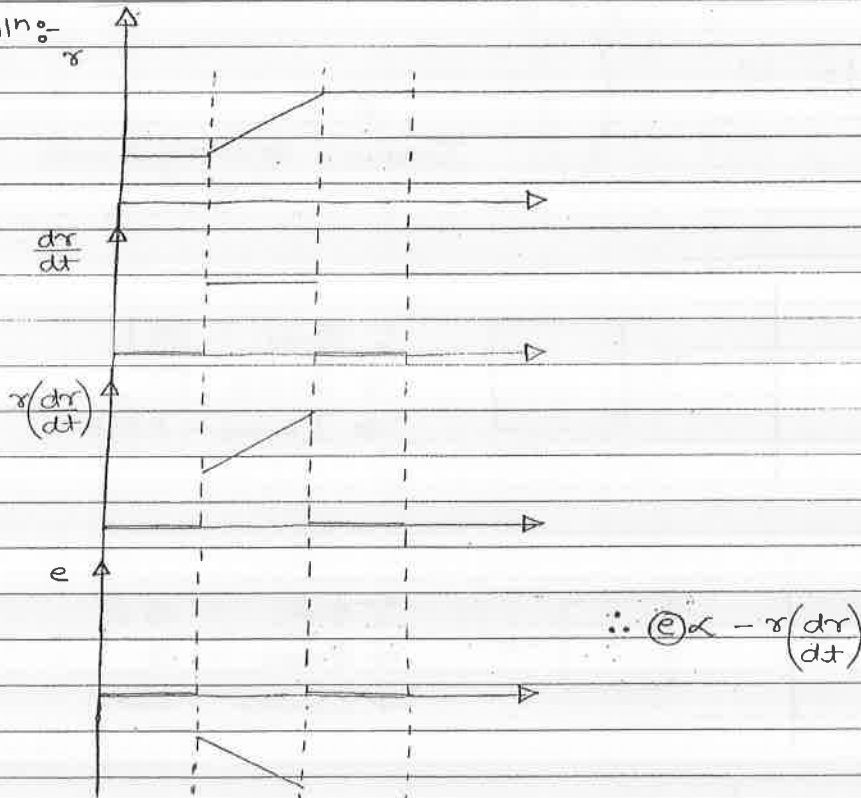
$$= -40 \times 10^{-3} \cdot \pi \cdot 2 \times 1 \times 10^{-2} \left(2 \times 10^{-3} \right)$$

$$= +16\pi \times 10^{-7} \text{ V}$$

$$= 1.6\pi \times 10^{-6} \text{ V} = 1.6\pi \mu\text{V}$$

* Ques > A circular coil placed in " \perp " magnetic field and its radius changes as shown, graph of Induced E.M.F?

soln:-



(i) case: I \Rightarrow of I wire \uparrow

P

Q

$$\phi_P = \odot \uparrow$$

$$\phi_Q = \otimes \uparrow$$

$$\phi_{\text{induc.}} = \otimes$$

$$\phi_{\text{induc.}} = \odot$$

$$I_{\text{induc.}} = \text{CW}$$

$$I_{\text{induc.}} = \text{ACW}$$

(ii) case: II \Rightarrow of I wire \downarrow

P

Q

$$\phi_P = \odot \downarrow$$

$$\phi_Q = \otimes \downarrow$$

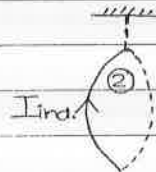
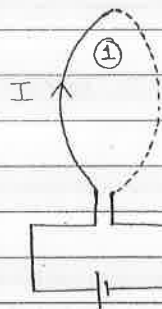
$$\phi_{\text{induc.}} = \odot$$

$$\phi_{\text{induc.}} = \otimes$$

$$I_{\text{induc.}} = \text{ACW}$$

$$I_{\text{induc.}} = \text{C.W.}$$

*4



\therefore of coil is heated (given)

$$\textcircled{5} \quad \therefore R \uparrow \Rightarrow I \downarrow$$

$$\phi \text{ (left)} \downarrow$$

\Rightarrow so Induced current in coil (2) is in same direction as I_1
so; they will be magnetic attract b/w them; so
Both coils come closer.

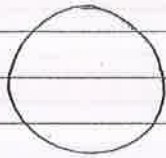
(ii) when moving away from "P" than;

$\therefore \phi_{coil} = \otimes \downarrow$

$\Rightarrow \phi_{indu.} = \otimes$

$\Rightarrow I_{induc.} = CW.$

(8)



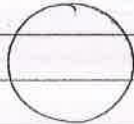
\Rightarrow it is equivalent to current carrying wire; which has constant current.

so; $\phi_{coil} \otimes = \text{const.}$

\Rightarrow NO E.M.I

\rightarrow e^- beam ($v = \text{const.}$)

(9)



\Rightarrow current carrying wire with increasing current continuously.

so;

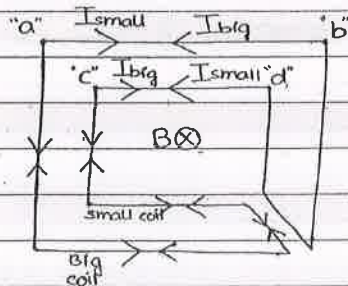
$\therefore \phi_{coil} = \otimes \uparrow$

$\Rightarrow \phi_{induc.} = \odot$

$\Rightarrow I_{induc.} = ACW.$

\rightarrow e^- beam (accelerated)

(10)



if $B \uparrow \Rightarrow (\phi_{indu.})_{small} = A.C.W.$

$(\phi_{indu.})_{big} = A.C.W.$

$$I = -L \frac{d\phi}{dt} = -L \cdot \frac{A}{R} \frac{dB}{dt}$$

$\therefore A_{big} > A_{small}$

$\therefore I < A \Rightarrow$ so; $I_{big} > I_{small}$

$\therefore I_{ab} = I_{big} - I_{small}$ ('b' to 'a')

$\therefore I_{cd} = I_{big} - I_{small}$ ('c' to 'd')

$$\Rightarrow \phi = f(B, A, \theta).$$

$$\text{If } \phi \neq \text{const.} \Rightarrow \text{E.M.F.}$$

(i) If $B \neq \text{const.} \Rightarrow$ static Induction. → SELF
→ MUTUAL

(ii) If $A \neq \text{const.} \Rightarrow$ Dynamic Induction.

(iii) If $\theta \neq \text{const.} \Rightarrow$ Periodic Induction.

★ \Rightarrow SELF INDUCTION :-

(i) When current in a coil changes with time and Induction takes place in same coil then it is called self Induction.

(ii) According to Lenz Law coil opposes the change of current, so it is called inertia of electricity.

\Rightarrow self Inductance (L) :-

In coils :-

$$\therefore \phi \propto I$$

$$\therefore \phi = LI$$

$$\therefore \boxed{L = \frac{\phi}{I}}$$

scalar Quantity.

Unit :- $\frac{\text{Wb}}{\text{A}}$, Henry (H).

∴ Total flux of solenoid :-

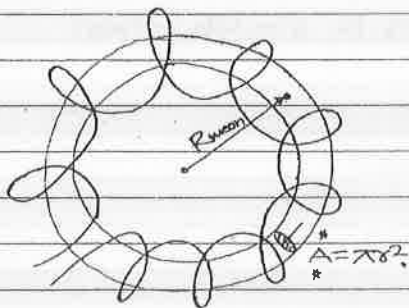
$$\begin{aligned}\phi &= NBA \cos \theta \\ &= N \left(\mu_0 \left(\frac{N}{l} \right) I \right) (A) \cos 0^\circ\end{aligned}$$

$$\frac{\phi}{I} = \mu_0 \frac{N^2 A}{l}$$

$$\begin{aligned}L_{\text{solenoid}} &= \frac{\mu_0 \mu_r N^2 A}{l} \times l \\ &= \mu_0 \mu_r \left(\frac{N}{l} \right)^2 (A \times l) \\ &= \mu_0 \mu_r n^2 (\text{volume})\end{aligned}$$

$$L_{\text{solenoid}} = \mu_0 \mu_r \frac{N^2 A}{l} = \mu_0 \mu_r n^2 (\text{volume})$$

© $L_{\text{toroid}} :-$



∴ Let current is I

$$B = \mu_0 n I = \mu_0 \left(\frac{N}{2\pi R_m} \right) I$$

∴ Total Flux of Toroid :-

$$\phi = NBA \cos \theta$$

$$= N \left(\frac{\mu_0 N I}{2\pi R_m} \right) (\pi r^2) \cos 0^\circ$$

Ques > If length and radius of frame of solenoid are doubled; then Find % change in its self Inductance :-

(i) Total turns remain constant.

(ii) Turn density remains constant.

$$\text{soln: (i) } L_{\text{solenoid}} = \frac{\mu_0 \mu_r N^2 A}{l}$$

$$= \frac{\mu_0 \mu_r N^2 (\pi r^2)}{l}$$

$$L_{\text{solenoid}} \propto \frac{r^2}{l}$$

$$L' = 2L$$

$$\% \text{ change} = \frac{L' - L}{L} \times 100$$

$$= 100\%$$

$$\text{(ii) } L_{\text{solenoid}} = \mu_0 \mu_r (n)^2 \times \text{volum}$$

$$= \mu_0 \mu_r (\frac{N}{l})^2 (\pi r^2 l)$$

$$L_{\text{solenoid}} \propto r^2 l$$

$$L' = 8L$$

$$\% \text{ change} = \frac{L' - L}{L} \times 100$$

$$= 700\%$$

Ques > $L_{\text{coil}} = 5\text{H}$. :- Find $e = ?$; gf :-

soln :- (i) Current is Increasing at the Rate of 2A/sec .

$$e = -L \frac{dI}{dt}$$

$$= -5(+2) \Rightarrow -10\text{V}$$

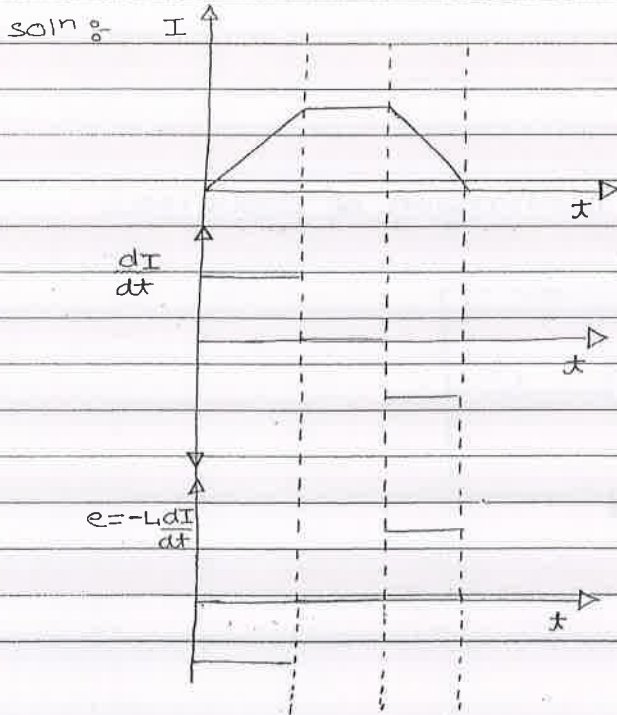
(ii) Current is Decreasing at the Rate of 2A/sec .

$$e = -L \frac{dI}{dt}$$

$$= -5(-2) \Rightarrow +10\text{V}$$

APMT

Ques > In a coil current is changing as shown in figure ;
then graph of Induced E.M.F with Time ?



CASE :- I :- GROWTH OF CURRENT (1-2) :-

$$\Rightarrow \quad t = 0 \qquad t = \uparrow \qquad t = \infty$$

$$I_{\text{ckt}} = 0$$

$$I_{\text{ckt}} = \uparrow$$

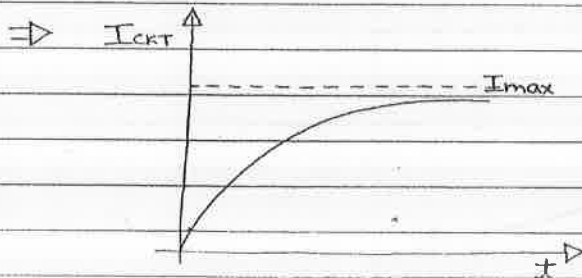
$$I_{\text{ckt}} = V_0/R = \text{Max.}$$

$$U_L = 0$$

$$U_L = \uparrow$$

$$U_L = \frac{L}{2} I_{\text{max}}^2 = \text{Max}$$

$$\Rightarrow \quad I_{\text{ckt}} = I_{\text{max}} (1 - e^{-\frac{R}{L}t})$$



⊗ \Rightarrow TIME CONST. (τ)

$$\tau = \frac{L}{R} \quad (63\% \text{ Growth of current.})$$

$$\Rightarrow \quad t = \tau \Rightarrow 63\%$$

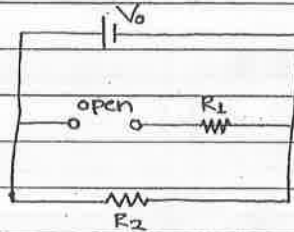
$$t = 3\tau \Rightarrow 95\%$$

$$t = 5\tau \Rightarrow 99.3\%$$

$$\Rightarrow \quad t = 0 \quad ; \quad L \equiv \text{OPEN CKT. } (I = 0)$$

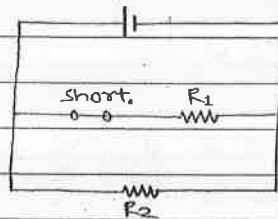
$$t = \infty \quad ; \quad L \equiv \text{SHORT CKT. } (I = \text{Max.})$$

soln :- (i) $t=0$



$$I_{\text{CKT}} = \frac{V_0}{R_2}$$

(ii) $t=\infty$



$$I'_{\text{CKT}} = \frac{V_0}{\left(\frac{R_1 R_2}{R_1 + R_2}\right)}$$

Ques \rightarrow In: L, R CKT :- $R = 50 \Omega$

\checkmark

$L = 2.5 \text{ H}$

Battery = 3V.

soln :- (i) $\tau = \frac{L}{R} = \frac{2.5}{50} \text{ sec.}$

$$= 50 \text{ m sec.}$$

(ii) Final current :-

$$I_{\text{max}} = \frac{V_0}{R} = \frac{3}{50} = 60 \text{ mA}$$

$$* \text{ (iii) } \frac{I_{\text{max}}}{2} = \frac{I_{\text{max}}}{2} (1 - e^{-\frac{R}{L}t})$$

$$\frac{1}{2} = 1 - e^{-\frac{R}{L}t}$$

Ques > Battery = 100 V, $R = 100 \Omega$, $L = 100 \text{ mH}$;

After steady state current discharging is started.

Find circuit current after one milli sec?

$$\text{soln :- } I_{\text{ckt}} = \frac{V_0}{R} e^{-R/Lt}$$

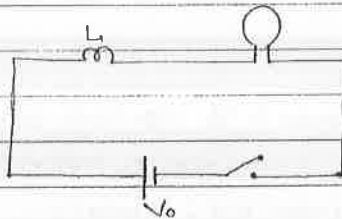
$$= \frac{100}{100} e^{-\frac{100}{100 \times 10^{-3}} \times 1 \times 10^{-3}}$$

$$= 1 \times e^{-1}$$

$$= \frac{1}{e} \text{ Amp.}$$

$$= 0.37 \text{ Amp.}$$

*Ques >



soln :- (i) when switch is made ON :-

$$\therefore \phi_{\text{cou.}} \uparrow \Rightarrow \frac{d\phi}{dt} = \oplus \text{ve.}$$

$$\therefore e = -\frac{d\phi}{dt} = \ominus \text{ve.}$$

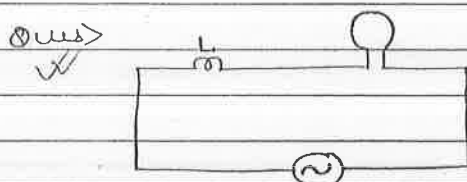
$$\therefore V_{\text{bulb}} = V_0 - e \Rightarrow \text{Less Bright.}$$

(ii) After Full Insertion :-

$$\phi = \text{maxm } \dot{\phi} \text{ const.}$$

$$\Rightarrow e = -\frac{d\phi}{dt} = 0$$

$\therefore V_{\text{bulb}} = V_0$ * (Bulb Regain its INITIAL and FULL BRIGHTNESS.)



* (phenomenon) of IRON ROD is inserted in INDUCTOR :-

Soln :- $\mu_r \uparrow$ \therefore (compare it while Reading A.C)
 $L \uparrow$
 $X_L \uparrow$
 $Z \uparrow$
 $I \downarrow$

(4) Battery Equivalent Model :-



(i) of "I" decreasing :-

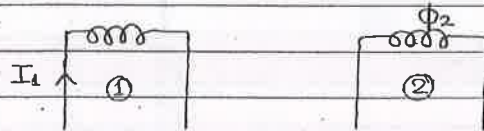


(ii) of "I" increasing :-



★ ⇒ MUTUAL INDUCTION (M) :-

When current in a coil changes with TIME then INDUCTION takes place in other coil. It is called Mutual Induction.



$$\therefore \Phi_2 \propto I_1$$

$$\Rightarrow \Phi_2 = M I_1$$

$$\therefore \boxed{M = \frac{\Phi_2}{I_1} = \frac{\Phi_1}{I_2}}$$

⇒ Unit :- HENRY (H), $\frac{\text{Wb.}}{\text{A}}$

⇒ Mutual Induction is Defined for Particular orientation of TWO COILS.

$$M = K \sqrt{L_1 L_2}$$

⇒ (K) ⇒ COUPLING COEFFICIENT.
($0 \leq K \leq 1$)

Ideal coupling; $K = 1$

⇒ coupling coeff. (K) represents the Flux Linkage b/w TWO COILS.

Ques > $L_1 = 2 \text{ mH}$ $L_2 = 8 \text{ mH}$ coupling = 30%
 than; $M = ?$

soln :- $M = K \sqrt{L_1 L_2}$
 $= 0.3 \sqrt{2 \times 8} \Rightarrow 1.2 \text{ mH.}$

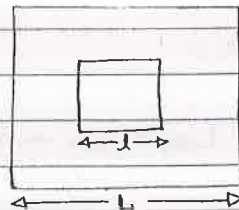
Ques > current in Primary coil is change from "5A" to
 "0A" in 0.1 sec and Induced E.M.F in secondary
 is 10 mV than; $M = ?$

soln :- $e_2 = -M \frac{dI_1}{dt}$

$$10 \times 10^{-3} = -M \left(\frac{0-5}{0.1} \right)$$

$$M = \frac{10 \times 10^{-3}}{50} = 0.2 \text{ mH.}$$

Ques >
 ✓



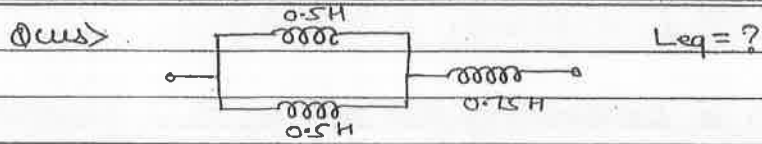
∴ given; $L \gg l$; than; $M = ?$

soln :- TEMP current is Always taken in the BIG COIL.
 Flux is Always taken in the SMALL COIL.

Let; I_{big}

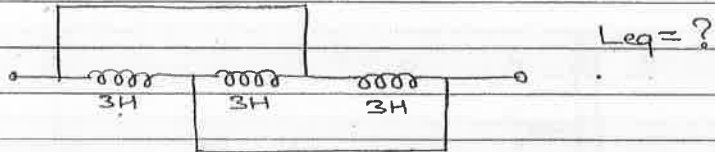
$$B_{\text{big}} = 2\sqrt{2} \left(\frac{\mu_0 I_{\text{big}}}{\pi L} \right)$$

$$\Phi_{\text{small}} = N_{\text{small}} B_{\text{big}} A_{\text{small}} \cos \theta$$

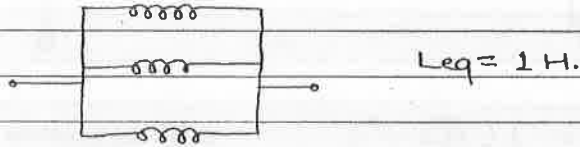


Soln :- $Leq = 0.25 + 0.75 = 1H.$

Ques >



Soln :-



Ques > If $L_1 = L_2 = 5H$; coupling = 10%
series Equivalent = ?

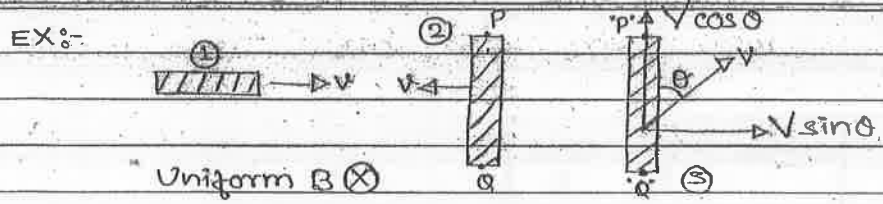
- (a) coil is in same sense.
(b) coil is in oppo. sense.

Soln :- $K = \frac{10}{100} = 0.1$

$M = 0.1 \sqrt{5 \times 5} = 0.5H$

(a) $L_1 + L_2 + 2M = 11H.$

(b) $L_1 + L_2 - 2M = 9H.$

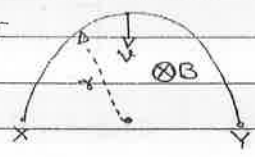


soln: (i) $l \parallel v$ so; "NO FLUX CUTTING"
 so; $\epsilon_{motional} = \text{zero}$.

(ii) "FLUX CUTTING" is there. so; $\epsilon_{motional} = Bv l$
 $\therefore P (-ve) = \text{LOW potential}$
 $\therefore Q (+ve) = \text{HIGH potential}$

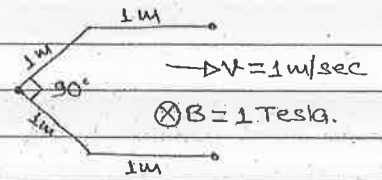
(iii) FLUX CUTTING is there. so; $\epsilon_{motional} = B(v \sin \theta) l$
 $\therefore P (+ve) = H.P. \therefore Q (-ve) = L.P. = Bv l \sin \theta$
 \Rightarrow so; (i) $V_P - V_Q = 0$ (ii) $V_P - V_Q = Bv l \sin \theta$ (iii) $V_P - V_Q = -Bv l \sin \theta$

Ques > A conducting half circular arc:-

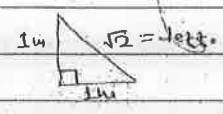


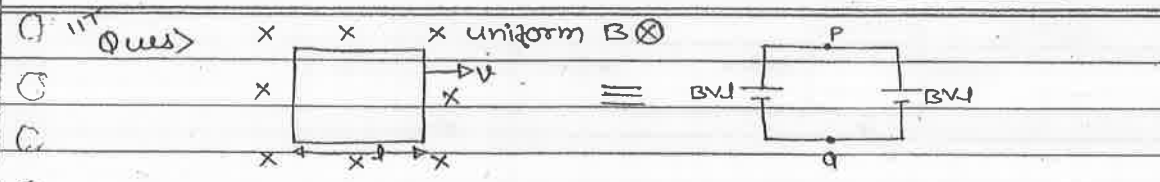
soln:- $\epsilon_{motional} = B v l$
 $= B v (2r) \Rightarrow 2 B v r$
 $X = -ve$
 $Y = +ve$
 $V_X - V_Y = -2 B v r$

Ques > \therefore Find P.D b/w Free Ends?

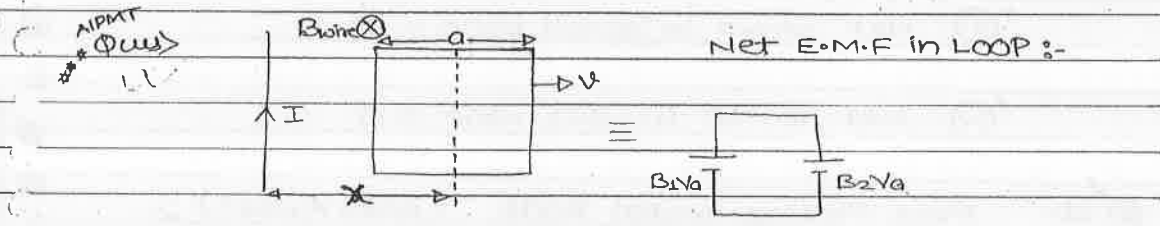


soln :- $e = B \cdot v \cdot l$
 $= 1 \times 1 \times \sqrt{2} = 1.414 \text{ volt}$





Soln :- (i) Net E.M.F in loop = 0 \therefore (cell in series; opposite Polarity)
 (ii) $V_P - V_Q = Bv$ \therefore (cell in parallel; same Polarity)



Soln :- Net E.M.F in Loop :-

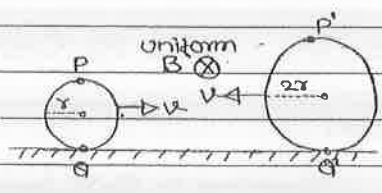
$$\therefore B_1 v a - B_2 v a \Rightarrow v a \left[\frac{\mu_0 I}{2\pi(x-a)} - \frac{\mu_0 I}{2\pi(x+a)} \right]$$

$$= \frac{\mu_0 I v a}{\pi} \left[\frac{1}{2x-a} - \frac{1}{2x+a} \right]$$

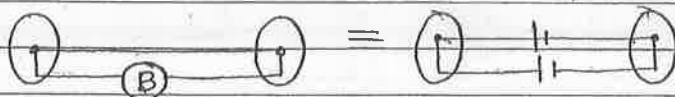
$$= \frac{\mu_0 I v a}{\pi} \left[\frac{2x+a - 2x+a}{(2x-a)(2x+a)} \right]$$

$\therefore E_{net} \propto \frac{I}{(2x-a)(2x+a)}$

III Ques > "Two" conducting Loop Moving on conducting Path ; as shown :-



(iii) If Bulb is connected across the Axle; then:-



\therefore Net E.M.F. in Loop = 0

\therefore so; Bulb will "NOT GLOW".

Ques) Aeroplane moving in horizontal plane at the same height; then:-

soln:- (i) $\nabla \parallel$ Aeroplane; so, P.D across length = 0.

(ii) Using's cut by lines;

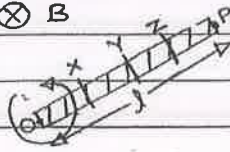
so. P.D across wing =

$$E_{\text{motional}} = B \times v \times \text{length of wings}$$

Ques >

⊗ B

P.D = ?

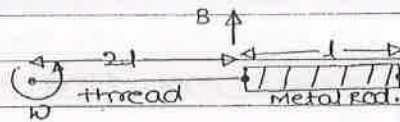


$$\text{soln :- (i) } \odot \text{ } X \text{ } P \Rightarrow e = \frac{1}{2} B \omega \left(\frac{l}{4}\right)^2$$

$$\begin{aligned} \text{(ii) } X \text{ } Z \Rightarrow e &= \frac{1}{2} B \omega \left[\left(\frac{3l}{4}\right)^2 - \left(\frac{l}{4}\right)^2 \right] \\ &= \frac{1}{4} B \omega l^2 \end{aligned}$$

$$\begin{aligned} \text{(iii) } Y \text{ } P \Rightarrow e &= \frac{1}{2} B \omega \left[l^2 - \left(\frac{l}{2}\right)^2 \right] \\ &= \frac{3}{8} B \omega l^2 \end{aligned}$$

* Ques >

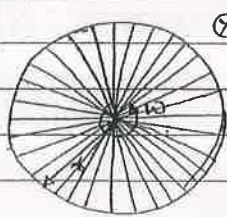


⇒ Find P.D b/w ends of metal Rod ?

$$\begin{aligned} \text{soln :- } e &= \frac{1}{2} B \omega \left[(3l)^2 - (2l)^2 \right] \\ &= \frac{5}{2} \omega l^2 \end{aligned}$$

⇒ If n identical Rod Rotates as shown; cutting Flux Lines n there Free ends are connected using conducting wire than it is Equivalent to Parallel Grouping of n identical cell Each $\frac{1}{2} B \omega l^2$; than

★ ⇒ DISC :-



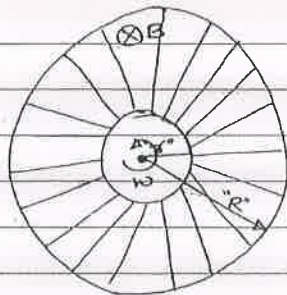
$$P.D = \frac{1}{2} B \omega r^2$$

∴ r ⇒ Radius.

→ If NO of Rod's become Infinite than it is like a Rotating Metal Disc in a Perpendicular magnetic Field, so there is P.D b/wⁿ periphery and centre.

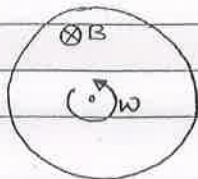
★ ⇒ ANULAR DISC :-

P.D b/wⁿ "Inner outer Edge"



$$P.D = \frac{1}{2} B \omega [R^2 - r^2]$$

★ ⇒ RING :-



$$P.D(r) = 0 \quad \because (R=r)$$



If Rotates like this than it will have Em

⊗ Flux with coil :-

$$\boxed{\phi = NBA \cos \omega t}$$

⊗ Induced E.M.F :-

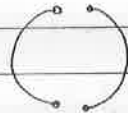
$$e = -\frac{d\phi}{dt} \Rightarrow -(NBA (-\sin \omega t) (\omega))$$

$$\boxed{e = NBA\omega \sin \omega t}$$

$$\begin{matrix} e_{\max} = NBA\omega = \omega \\ \phi_{\max} = NBA \end{matrix} \quad \text{⊗}$$

⇒ "FLUX" is leading from "E.M.F" by 90° . so when Flux is "0" than Induced E.M.F is Maximum and vice versa.

⇒ In D.C generator "commutator" is used in the place of "slip ring" which always ^{has} max^m lead current unidirectional.



commutator
Diagram.

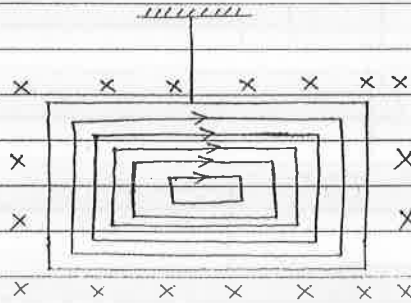
$$\oint \vec{E} \cdot d\vec{l} = -A \frac{dB}{dt}$$

$$\oint q\vec{E} \cdot d\vec{l} = -qA \frac{dB}{dt}$$

$$\therefore W_{\text{close loop}} = -qA \frac{dB}{dt} \neq 0.$$

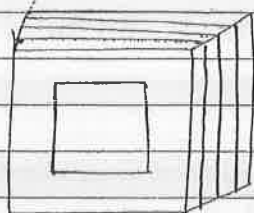
\Rightarrow so; Induced Electric Field is always non-conservative

$\star \Rightarrow$ EDDY CURRENT (FOCALT CURRENT):-

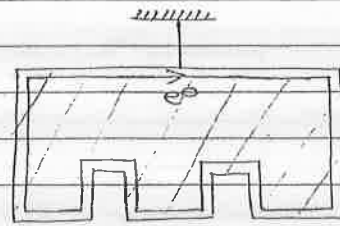


\rightarrow When Magnetic Field changes than Induced current in metallic structure is in the form of many concentric loop like Eddy's in water so it is called as EDDY CURRENT.

\rightarrow^{**} Eddy current produces large Amount of Heat called Eddy losses.



Laminated core.



Slotted structure.

⇒ When MOTOR is "SWITCHED ONN" :-

(i) At $t=0$; $\omega=0 \Rightarrow E_b=0 \Rightarrow I = \text{High} \times \text{Unsafe}$.

(ii) as $t \uparrow$; $\omega \uparrow \Rightarrow E_b \uparrow \Rightarrow I \downarrow$.

(iii) After SOME TIME; $\omega = \text{Max}^m \times \text{const}$.

$\Rightarrow E_b = \text{Max}^m \times \text{const}$.

$\Rightarrow I = \text{Normal} \times \text{safe}$.

★ ⇒ STARTER :-

It is a variable Resistant used to protect the motor from Initial high current, (at the time of switch ONN)

★ ⇒ POWER :-

(i) $P_{\text{input}} = E I_a$

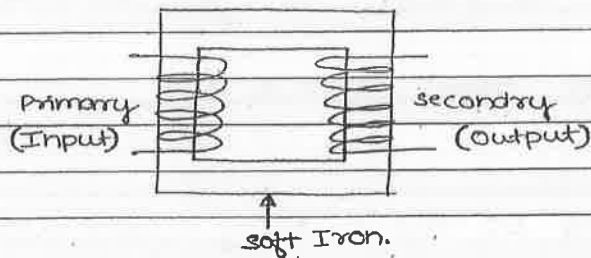
(ii) $P_{\text{loss}} = I_a^2 R_a$

(iii)
$$\begin{aligned} P_{\text{output}} &= P_{\text{input}} - P_{\text{loss}} \\ &= E I_a - I_a^2 R_a \\ &= I_a [E - R_a I_a] \end{aligned}$$

$$P_{\text{output}} = E_b I_a$$

(iv) $\% \eta = \frac{P_{\text{output}} \times 100}{P_{\text{input}}}$

$$\% \eta = \frac{E_b \times 100}{E}$$



⊗ Ideal Transformer :-

$$P = \text{const.}$$

$$\therefore VI = \text{const.}$$

$$\therefore V \propto \frac{1}{I}$$

$$P = \text{const.}$$

$$\therefore \frac{V^2}{R} = \text{const.}$$

$$\therefore V \propto \sqrt{R}$$

⊗ Turn Ratio (K) :-

$$K = \frac{N_s}{N_p} = \frac{V_s}{V_p} = \frac{I_p}{I_s} = \frac{\sqrt{Z_s}}{\sqrt{Z_p}}$$

⇒ step UP

step DOWN

$$\therefore V_s > V_p$$

$$\therefore N_s > N_p$$

$$\therefore I_s < I_p$$

$$\therefore Z_s \neq Z_p$$

$$\therefore K > 1$$

$$\therefore V_s < V_p$$

$$\therefore N_s < N_p$$

$$\therefore I_s > I_p$$

$$\therefore Z_s < Z_p$$

$$\therefore K < 1$$

$$\Rightarrow R = \frac{\rho l}{A} \propto \frac{l}{A}$$

$\therefore R_s \text{ High} \Rightarrow A_s \text{ small.}$

(5) HUMMING LOSS:-

Energy loss in the form of sound.

$$\oplus \Rightarrow \boxed{\% \eta = \frac{P_{\text{output}}}{P_{\text{input}}} \times 100}$$

*^vques> A Bulb of 100 watt is operated by supply 220 volt and 0.5A current using a Transformer. Then;

soln:- (i) $k = \frac{1}{2}$

$$(ii) \% \eta = \frac{100 \times 100}{220 \times 0.5} = 91\%$$

*^qques> Transformer of 90% Efficiency; works on 200V & 3 Kw.

gf; $I_s = 6A$; $I_p = ?$
 $V_s = ?$

soln:- $I_p = \frac{P_{\text{prim}}}{V_{\text{prim}}} = \frac{3 \times 10^3}{200} = 15A$

$$\boxed{\frac{V_s}{V_p} = \frac{I_p}{I_s}}$$

X \therefore Not use this bcz Not an case of "Ideal transformer"

Lined writing area with multiple horizontal lines.

Date _____ Page _____

Lined writing area with horizontal ruling lines and a spiral binding on the left side.

JMS JMD
"ALTERNATE CURRENT"

श्री नाथ जी बुक डिपो
ALLEN सत्यार्थ गेट नं. 2

के सामने शॉप नं. 2
Date _____ Page _____

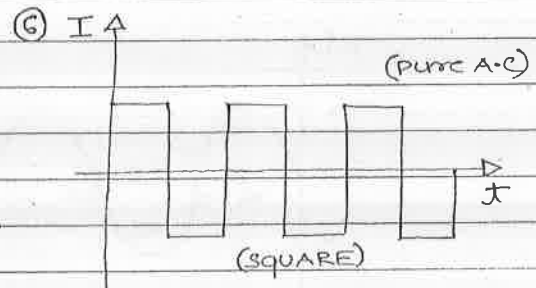
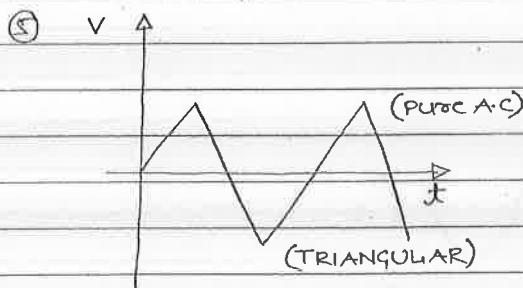
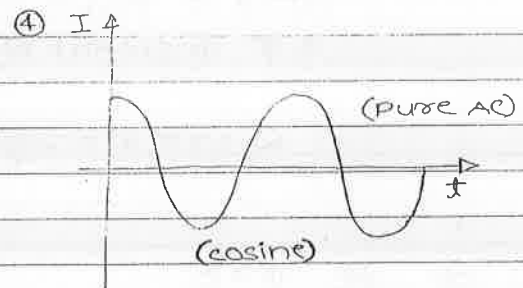
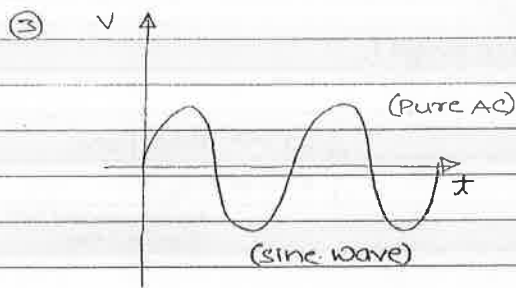
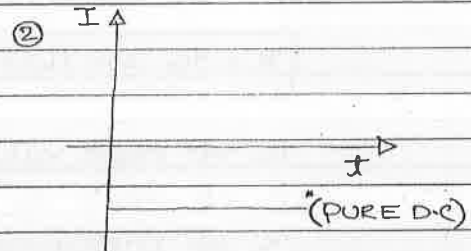
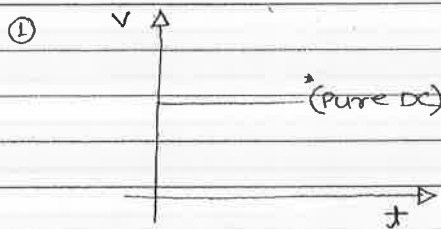
★ ⇒ Electric SIGNAL ⇒

(i) DIRECT :- Unidirectional and constant.

(ii) ALTERNATING :- (i) Bidirectional & PERIODIC,

(ii) Positive peak value = Negative peak value

★ ⇒ SOME BASIC GRAPHS FOR A.C & D.C :-



$$\Rightarrow \boxed{2\pi = T} \quad \text{eg:- (i) } 60^\circ = \frac{\pi}{3} = \frac{T}{6}$$

$$(ii) 45^\circ = \frac{\pi}{4} = \frac{T}{8}$$

$$(iii) 30^\circ = \frac{\pi}{6} = \frac{T}{12}$$

\Rightarrow In one cycle zero occurs "TWICE". so Direction changes "TWICE".

IMP.

\Rightarrow If Time Independent signal then PURE D.C. And if Time Dependent sin or cosine signal ^{than} ~~or~~ PURE A.C.

Ques \rightarrow An Electric voltage is $V = 10 \text{ volt}$ * (Time Independ. so pure D.C) \Rightarrow PURE D.C

Ques \rightarrow An Electric current ; $I = 50 \sin 30^\circ$ Applied than ;

soln :- (TIME \neq Not depends) \therefore Time Independent \Rightarrow so ; PURE D.C.

Ques \rightarrow $[V = \theta]$ An electric voltage is $V = 0.311 \sin(100\pi t + \frac{\pi}{4})$

soln :- (i) Pure A.C

(ii) Peak Voltage = 0.311 volt

(iii) Peak to peak voltage = $2 \times 0.311 \Rightarrow 0.622 \text{ volt}$

Ques An Electric current is:-

$$I = 100 \sin(100\pi t) \cos(100\pi t)$$

soln:-

$$I = 100 \sin(100\pi t) \cos(100\pi t)$$

$$= 50 [2 \sin(100\pi t) \cos(100\pi t)]$$

$$I = 50 \sin(200\pi t)$$

(i) pure A.C

(ii) Peak to Peak = $50 \times 2 \Rightarrow 100$ Amp.

(iii) $I_{\text{peak}} = 50$.

(iv) Initial Phase = 0.

(v) $\omega = 200\pi$ Rad./sec.

(vi) $f = \frac{\omega}{2\pi} = 100$ Hz.

(vii) $T = \frac{1}{f} = \frac{1}{100}$ sec. $\Rightarrow 10$ m sec.

Ques An Electric current is:- $I = I_0 \sin^2 \omega t$?

soln:-

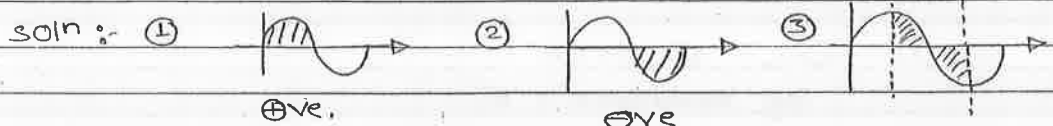
$$I = I_0 \sin^2 \omega t$$

$$= I_0 \left[\frac{1 - \cos 2\omega t}{2} \right]$$

$$I = \underbrace{\frac{I_0}{2}}_{\text{Pure D.C}} - \underbrace{\frac{I_0}{2}}_{\text{Pure A.C}} \cos 2\omega t$$

* Ques > For sinusoidal voltage; avg. for half cycle is :-

- ✓
- ① Always +ve.
 - ② Always -ve.
 - ③ Always zero.
 - ④ may be +ve, -ve, or zero.



② ROOT MEAN SQUARE VALUE (R.M.S) / Apparent / virtual Effective :-

$$X_{rms} = \left[\frac{1}{T} \int_0^T x^2 \cdot dt \right]^{1/2}$$

$$X_{rms} = \frac{x_0}{\sqrt{2}}$$

IMP * ① If Nothing is given; than given A.C value is considered R.M.S value.

* ② For Heat & POWER calculation R.M.S value is used.

eg:- ① Domestic supply \Rightarrow 220V; 50Hz

$$\Rightarrow V_{rms} = 220V$$

$$V_{peak} = 220\sqrt{2} = 311V$$

$$V_{supply} = V_0 \sin(2\pi ft)$$

$$= 311 (\sin(2\pi \times 50 \times t))$$

$$V_{supply} = 311 \sin(100\pi t) \checkmark$$

*Ques> $I = I_1 + I_2 \sin \omega t$; is one Electric current?
 ✓

soln:- (i) A.C + D.C

$$\begin{aligned} \text{(ii)} \quad \langle I \rangle_T &= \langle I_1 + I_2 \sin \omega t \rangle \\ &= I_1 + I_2(0) \\ &= I_1 \end{aligned}$$

$$\text{(iii)} \quad I_{\text{rms}} = \left\{ \langle I^2 \rangle_T \right\}^{1/2}$$

$$\begin{aligned} \therefore I_{\text{rms}} &= \sqrt{\frac{I_1^2 + I_2^2}{2}} = \left\{ \langle I_1^2 + I_2^2 \sin^2 \omega t + 2I_1 I_2 \sin \omega t \rangle \right\}^{1/2} \\ &= \left\{ I_1^2 + I_2^2 (1/2) + 2I_1 I_2(0) \right\}^{1/2} \end{aligned}$$

*Ques> An electric current is $I = \sqrt{t}$. Then find its RMS
 ✓ b/wⁿ 2 to 4 sec?

$$\text{soln:-} \quad I_{\text{rms}} = \left\{ \frac{1}{(4-2)} \int_2^4 I^2 dt \right\}^{1/2}$$

$$= \left\{ \frac{1}{2} \int_2^4 t \cdot dt \right\}^{1/2}$$

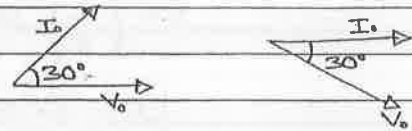
$$= \left\{ \frac{1}{2} \left[\frac{t^2}{2} \right]_2^4 \right\}^{1/2}$$

$$= \left\{ \frac{1}{4} (16-4) \right\}^{1/2}$$

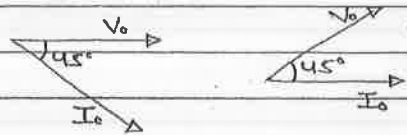
$$= \sqrt{3}$$

★ ⇒ PHASOR DIAGRAM :-

(i) $V = V_0 \sin \omega t$
 $I = I_0 \sin(\omega t + 30^\circ)$



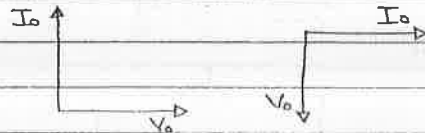
(ii) $V = V_0 \sin \omega t$
 $I = I_0 \sin(\omega t - 45^\circ)$



(iii) $V = V_0 \sin \omega t$
 $I = I_0 \sin \omega t$



(iv) $V = V_0 \sin \omega t$
 $I = I_0 \cos \omega t$



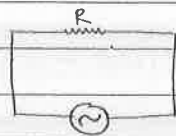
★ ⇒ PHASE DIFFERENCE (ϕ):-

It is difference of phase of voltage & current.

★ ⇒ POWER FACTOR (PF) ⇒ $\cos \phi$.

★ ⇒ A.C CIRCUITS :-

(1) Pure Resistive (R) circuit :-



∴ Let ; $V = V_0 \sin \omega t$.

By R.V.L :- $V - IR = 0$.

$$\Rightarrow I = \frac{V}{\text{Problem}}$$

$$I = \frac{V_0 \sin(\omega t - \frac{\pi}{2})}{X_L}$$

$$I = I_0 \sin(\omega t - \frac{\pi}{2})$$

* \Rightarrow Inductive resistance (X_L)

(i) $X_L = \omega L = 2\pi f L$

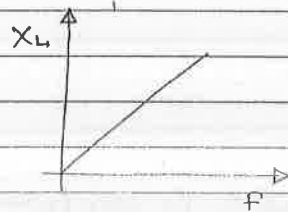
(ii) Unit \Rightarrow ohm.

(iii) $X_L \propto f$.

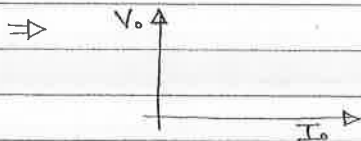
$$f=0 \Rightarrow X_L=0$$

$$f \uparrow \Rightarrow X_L \uparrow$$

$$f=\infty \Rightarrow X_L=\infty$$



\Rightarrow "V" leading by 90° .



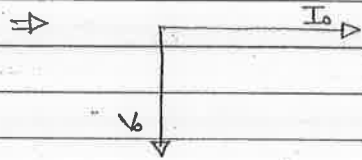
$$\Rightarrow \phi = 90^\circ$$

$\Rightarrow P \cdot F = \cos \phi = 0 \therefore$ (so, "L" does not consume power)

(3) PURE "C" CIRCUIT:-

\Rightarrow Practically pure (C) circuit is also not possible.

⇒ voltage is lagging by 90° .



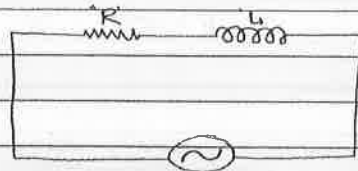
⇒ $\phi = 90^\circ$.

⇒ P.F. = $\cos \phi = 0$. ∴ [∴; 'C' does not consume power.]

④ SERIES "R-L" CIRCUIT :-

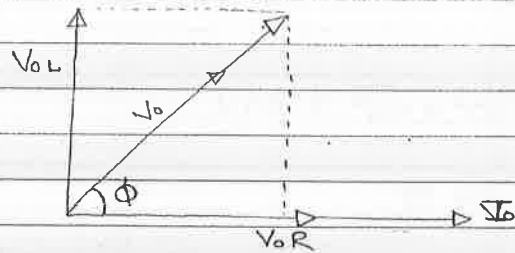
Let RKT current :-

$$I = I_0 \sin \omega t.$$

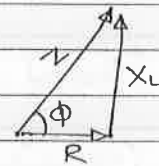


⇒ $V_R = V_0 R \sin \omega t$

$$V_L = V_0 L \sin (\omega t + \pi/2)$$



≡



∴ Impedance Triangle

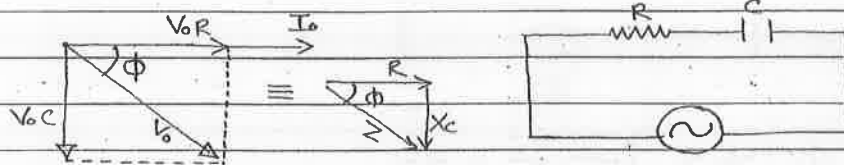
∴ Voltage Triangle.

$$\Rightarrow V_0 = \sqrt{V_0 R^2 + V_0 L^2}$$

⇒ (✓) Leading.

$$\Rightarrow \phi = \tan^{-1} \left(\frac{V_0 L}{V_0 R} \right) = \tan^{-1} \left(\frac{X_L}{R} \right)$$

(S) SERIES R-C CIRCUIT :-



(i) $V_0 = \sqrt{V_0R^2 + V_0C^2}$

(iv) \checkmark lagging.

(iii) $\phi = \tan^{-1} \left(\frac{V_0C}{V_0R} \right) \Rightarrow \tan^{-1} \left(\frac{X_c}{R} \right)$

(iv) P.F = $\cos \phi = \frac{V_0R}{V_0} = \frac{R}{Z}$

\checkmark Impedance (Z) :-

(a) $Z = \sqrt{R^2 + X_c^2}$

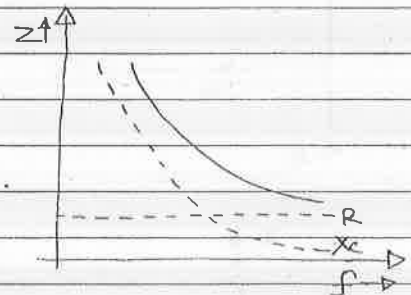
(b) unit $\Rightarrow \Omega$

(c) "Z" v/s "f"

$f = 0 \Rightarrow X_c = \infty \Rightarrow Z = \infty$

$f = \uparrow \Rightarrow X_c = \downarrow \Rightarrow Z = \downarrow$

$f = \infty \Rightarrow X_c = 0 \Rightarrow Z = R$

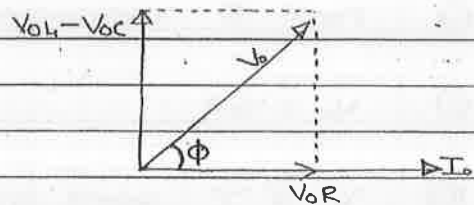


(A) case:- I \Rightarrow If $V_{oL} > V_{oC}$:-

\Rightarrow Behave as series R-L CKT.

(i) $V_o = \sqrt{V_oR^2 + (V_{oL} - V_{oC})^2}$

(ii) "V" leading



(iii) $\phi = \tan^{-1} \left(\frac{V_{oL} - V_{oC}}{V_oR} \right) = \tan^{-1} \left(\frac{X_L - X_C}{R} \right)$

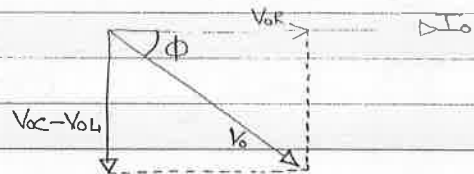
(iv) P.F = $\cos \phi = \frac{V_oR}{V_o} = \frac{R}{Z}$

(v) $Z = \sqrt{R^2 + (X_L - X_C)^2}$

(B) case:- II \Rightarrow If $V_{oL} < V_{oC}$:-

(i) Behave as series R-C CKT.

(ii) $V_o = \sqrt{V_oR^2 + (V_{oC} - V_{oL})^2}$

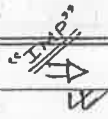


(iii) "V" lagging.

(iv) $\phi = \tan^{-1} \left(\frac{X_C - X_L}{R} \right) = \tan^{-1} \left(\frac{V_{oC} - V_{oL}}{V_oR} \right)$

(v) P.F = $\cos \phi = \frac{R}{Z}$

(vi) $Z = \sqrt{R^2 + (X_C - X_L)^2}$



Z v/s f :-

$$\therefore f \propto \frac{1}{X_c} \propto X_L$$

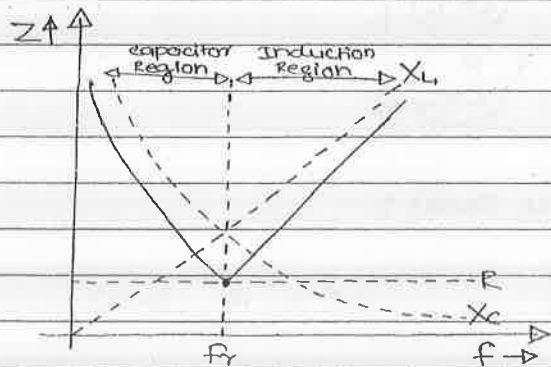
$$\textcircled{i} \quad f=0 \quad :- \quad \left. \begin{array}{l} R = R \\ X_L = 0 \\ X_c = \infty \end{array} \right\} \begin{array}{l} Z = \infty \\ = X_c \text{ (Pure 'C' CKT)} \end{array}$$

$$\textcircled{ii} \quad 0 < f < f_r \quad :- \quad \left. \begin{array}{l} R = R \\ X_L \uparrow \\ X_c \downarrow \end{array} \right\} \begin{array}{l} \text{(Series R-C CKT)} \\ X_c > X_L \end{array}$$

$$\textcircled{iii} \quad f = f_r \quad :- \quad \left. \begin{array}{l} R = R \\ X_L = X_c \end{array} \right\} \begin{array}{l} \text{(PURE 'R' CKT)} \\ \text{[Resonance condition]} \end{array}$$

$$\textcircled{iv} \quad f_r < f < \infty \quad :- \quad \left. \begin{array}{l} R = R \\ X_L > X_c \end{array} \right\} \text{(Series 'R-L' CKT)}$$

$$\textcircled{v} \quad f = \infty \quad :- \quad \left. \begin{array}{l} R = R \\ X_L = \infty \\ X_c = 0 \end{array} \right\} \begin{array}{l} Z = \infty = X_L \\ \text{(PURE 'L' CKT)} \end{array}$$



⊗ Fractional BW :-

$$\frac{\Delta F}{f_r} = \frac{\Delta \omega}{\omega_r}$$

$$\Rightarrow \frac{R/L}{1/\omega_r L C}$$

$$\Rightarrow \frac{R \sqrt{C}}{\omega_r L}$$

∴ Rajasthan ckt League

⊗ Quality Factor (Q) :-

⇒ It is measure of sharpness of I vs F curve.

⇒ ∴ SHARPNESS ↑ ⇒ Q ↑ ⇒ SOUND QUALITY BETTER.

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$$Q = \frac{1}{\text{Fractn BW}} = \frac{f_r}{\Delta F} = \frac{\omega_r}{\Delta \omega} \Rightarrow \frac{1}{R \sqrt{C}} = \frac{X_L}{R} = \frac{X_C}{R}$$

∴ The Above is used in communication system.

★ ⇒ V. IMPORTANT POINTS :-

① $V_{NET} =$

② $Z =$

③ $I_{ckt} = \frac{V}{Z}$

④ $\phi = \tan^{-1} \left(\frac{X}{R} \right)$

⑤ $P.F = \cos \phi = \frac{R}{Z}$

$$(9) P.F = \cos \phi \Rightarrow \frac{30}{50} = 0.6$$

$$(10) V_{\text{supply}} = 50\sqrt{2} \sin(\omega t - 53^\circ)$$

Ques) IN "SERIES RLC" CIRCUIT :-

$$\therefore V_L = V_C = 500 \text{ V}$$

$$\therefore R = 200 \Omega$$

$$V_{\text{supply}} = 200 \text{ V}, 50 \text{ Hz}$$

Soln:- (1) $V_L = V_C \therefore$ (Resonance condition)

(2) PURE R-CKT.

$$(3) V_{\text{supply}} = V_R = 200 \text{ V.}$$

$$(4) Z = R = 200 \Omega.$$

$$(5) I_{\text{CKT}} = \frac{V}{Z} = \frac{200}{200} = 1 \text{ Amp.}$$

$$(6) L = ? \Rightarrow V_L = I X_L$$

$$V_L = I (2\pi f L)$$

$$500 = (1) [2\pi \times 50 \times L]$$

$$L = \frac{5}{\pi} \text{ Henry.}$$

$$(7) C = ? \Rightarrow V_C = I X_C$$

$$V_C = I \left(\frac{1}{2\pi f C} \right)$$

$$500 = 1 \left(\frac{1}{2\pi \times 50 \times C} \right)$$

$$C = \frac{10^{-4}}{5\pi} \text{ F}$$

$$\begin{aligned} \text{③ } P_{\text{average}} &= V_{\text{rms}} I_{\text{rms}} \cos \phi \\ &= V_{\text{rms}} I_{\text{rms}} \cos 90^\circ \\ &= 0. \end{aligned}$$

*** Ques) In "SERIES R-L" CIRCUIT:-

$$E_{\text{supply}} = E_0 \cos \omega t.$$

$$\text{Given; } X_L = R.$$

$$\Rightarrow \text{Power} = ?$$

$$\text{Soln :- } V_{\text{rms}} = \frac{E_0}{\sqrt{2}} \text{ ----- ①}$$

$$Z = \sqrt{R^2 + X_L^2} = \sqrt{2} R.$$

$$I_{\text{rms}} = \frac{V_{\text{rms}}}{Z} = \frac{E_0/\sqrt{2}}{\sqrt{2} R} = \frac{E_0}{2R} \text{ ----- ②}$$

$$\cos \phi = \frac{R}{Z} \Rightarrow \frac{R}{\sqrt{2} R} = \frac{1}{\sqrt{2}} \text{ ----- ③}$$

Ist Meth.

$$\therefore P = V_{\text{rms}} I_{\text{rms}} \cos \phi \Rightarrow \frac{E_0^2}{4R}$$

IInd Meth.

$$\therefore P = I^2 R \Rightarrow \left(\frac{E_0}{2R}\right)^2 R = \frac{E_0^2}{4R}$$

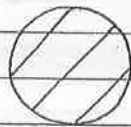
IIIrd Meth.

$$\therefore V_R = IR \Rightarrow \left(\frac{E_0}{2R}\right) R = \frac{E_0}{2}$$

$$\Rightarrow P = \frac{V_R^2}{R} \Rightarrow \frac{(E_0/2)^2}{R} = \frac{E_0^2}{4R}$$

★ ⇒ SKIN EFFECT :-

"A-c current" ^{flows} ~~flows~~ through outer surface of the conducting wire. so, it is called skin effect.



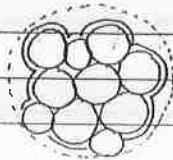
single strand wire

$$\therefore R = \frac{S}{A}$$

$$\therefore A_{\text{eff}} \downarrow \downarrow$$

$$\Rightarrow R_{\text{eff}} \uparrow \uparrow$$

$$\Rightarrow \text{LOSS} = I^2 R \uparrow \uparrow$$



$$\therefore A_{\text{eff}} \uparrow$$

$$\Rightarrow R_{\text{eff}} \downarrow$$

$$\Rightarrow I^2 R = \text{LOSS} \downarrow \downarrow$$

★ ⇒ CHOKE COIL :-

It is EXTRA INDUCTOR inserted in A-c circuit to control the current without extra Power Loss.

$$I \downarrow = \frac{V}{Z \uparrow}$$

$$\Rightarrow R \times (\text{POWER LOSS} \uparrow \uparrow)$$

$$\Rightarrow C \times (\text{पेक्षा शक्ति है} = \text{costly}).$$

$$\Rightarrow L \checkmark (\text{economic}).$$

⇒ Ideal choke coil ⇒ pure L ckt. (R=0).

choke coil ⇒ series R-L ckt.

choke coil based on wattless current.

$$\text{Potential :- } \frac{Q}{C} + L \frac{dI}{dt} = 0$$

$$\frac{Q}{C} + L \frac{d^2Q}{dt^2} = 0 \quad \therefore I = \frac{dQ}{dt}$$

$$\boxed{\frac{d^2Q}{dt^2} + \frac{Q}{LC} = 0} \quad \therefore \frac{d^2x}{dt^2} + \omega^2 x = 0$$

$$\therefore \omega^2 = \frac{1}{LC}$$

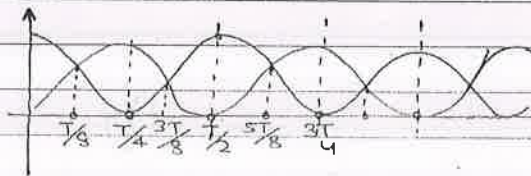
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$$\text{(i) } Q = Q_0 \cos \omega t$$

$$\text{(ii) } I = \frac{dQ}{dt} \quad \therefore I = I_0 \cos(\omega t + \pi/2)$$

$$\text{(iii) } U_{\text{max}} = \frac{1}{2} \frac{Q_0^2}{C}$$

$$\text{(iv) } U_{\text{max}} = \frac{1}{2} L I_0^2$$





Date _____ Page _____

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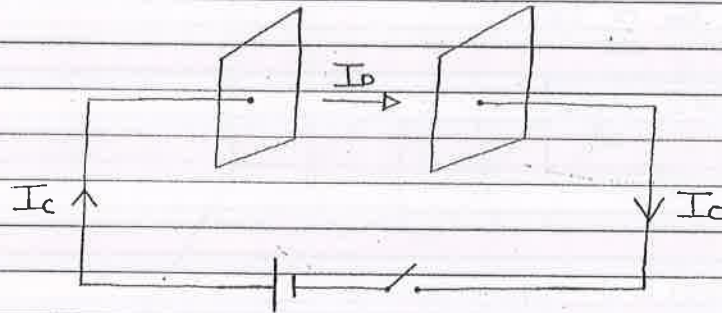
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"E.M.W"

Date _____ Page _____

⊗ ⇒ FARADAY'S LAW FOR E.M.I. :-

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d\phi}{dt}$$

⊗ ⇒ MAXWELL'S CONCEPT OF DISPLACEMENT CURRENT :-



⇒ during charging magnetic field is produced b/w the plates due to variable Electric Field.

⇒ imaginary current corresponding to this field is called displacement current.

$$\Rightarrow I_C = I_D$$

⇒ Both current's (I_C & I_D) are incomplete and making complete current jointly. so; these are supplementary of Each other.

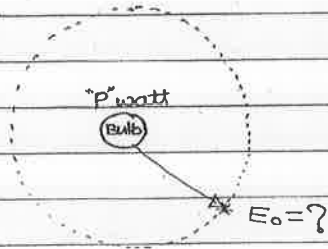
$$I_D = \frac{dq}{dt} = \frac{d(eV)}{dt}$$

$$I_D = c \frac{dv}{dt}$$

Ques > A Bulb of 'P' watt is emitting light. Find Peak Electric Field at 'r' distance ?

soln:- $I = \frac{P}{4\pi r^2} \Rightarrow \frac{1}{2} \epsilon_0 c E_0^2$

$$E_0 = \sqrt{\frac{P}{2\pi \epsilon_0 r^2}}$$



★ ⇒ EMW SPECTRUM :-

"VIBGYOR"						
γ	X	UV	visible	IR	μw	Radio wave
0-1Å	100Å	3900Å	7800Å			

→ λ ↑

→ $\left(E_{ph} = \frac{hc}{\lambda} \right) ↓$