

QATAR

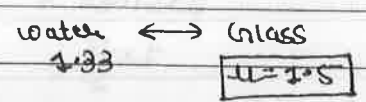
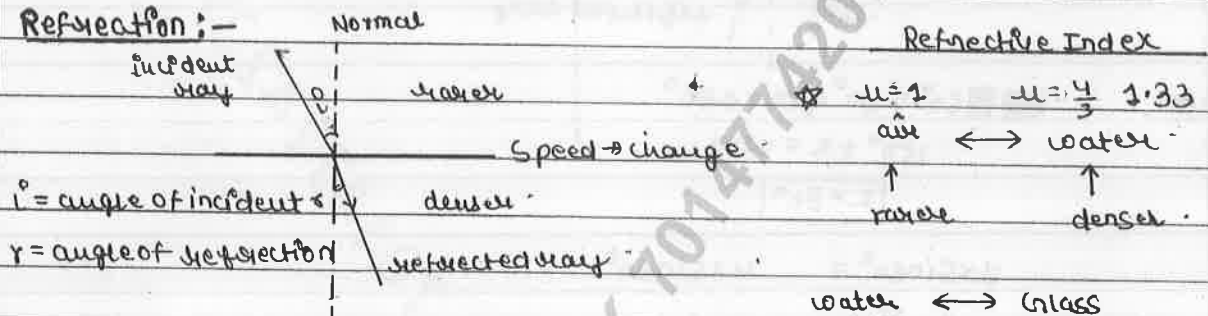
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Ray optics

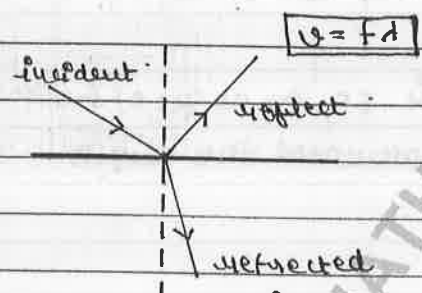
TOPICS :-

1. Reflection
2. Refraction
3. Prism
4. Lens
5. Optical instruments

Refraction :-



All angle measure From Normal

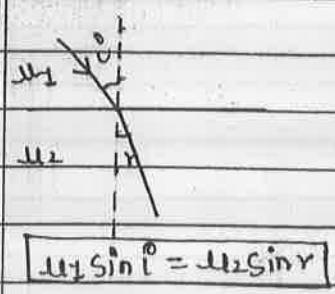


* Ref Index = $\frac{c}{v}$ = Speed of light vacuum / v in space

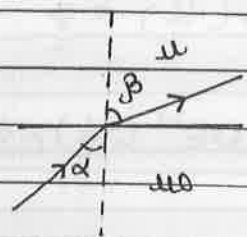
Refraction None of λ or f (property of source)

- * Frequency = constant
- Speed \rightarrow change
- wavelength \rightarrow change
- Intensity of light \rightarrow change (always decreases)

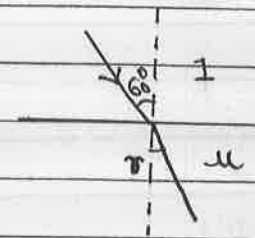
Snell's Law :-



$u_1 \sin i = u_2 \sin r$



$u \sin \alpha = u_0 \sin \beta$

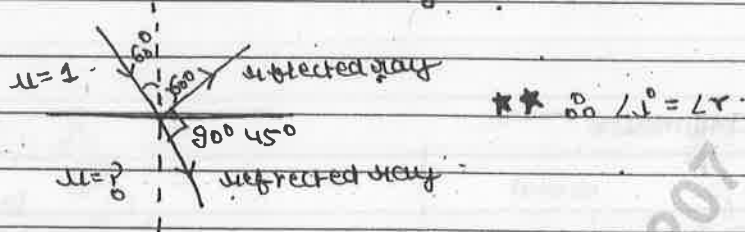


$1 \sin 60^\circ = u \sin r$

Incident ray, refracted ray and normal are in a same plane

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Q1 In a given situation light enters into oil having $\angle i = 60^\circ$. If 'reflected ray' and 'refracted ray' are mutually perpendicular then find out the ref. index of oil?



Solve: $60^\circ + 90^\circ + r = 180^\circ$
 $150^\circ + r = 180^\circ$
 $r = 30^\circ$

$$1 \times \sin 60^\circ = n \times \sin 30^\circ$$

$$1 \times \frac{\sqrt{3}}{2} = n \times \frac{1}{2}$$

$$n = \sqrt{3}$$

Q2 Light enters from denser medium n into air. If the angle of incidence is half of angle of refraction then calculate the angle of refraction?

$$n \sin \frac{\theta}{2} = 1 \times \sin \theta$$

* Important

$$n \sin \frac{\theta}{2} = \sin \theta$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$\sin \theta = 2 \sin \frac{\theta}{2} \cos \frac{\theta}{2} \quad n \sin \frac{\theta}{2} = 2 \sin \frac{\theta}{2} \cos \frac{\theta}{2}$$

$$\frac{n}{2} = \cos \frac{\theta}{2}$$

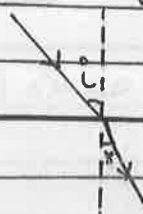
$$\cos^{-1} \left(\frac{n}{2} \right) = \frac{\theta}{2}$$

$$2 \cos^{-1} \left(\frac{n}{2} \right) = \theta$$

* Concepts -

Light ray

rarer to denser ray bend toward normal.



$n_1 > n_2$

rarer

denser

$n_2 < n_1$

$$n_1 \sin i = n_2 \sin r$$

Paraxial Rays:- rays having small angles.

optical Illusions:-

$$\frac{H_i}{H_o} = \frac{\mu_2}{\mu_1}$$

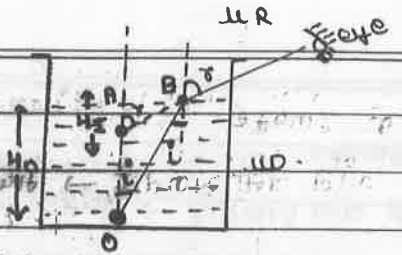
$$4 \times \frac{12}{3} = 16m$$

$$\frac{x}{12} = \frac{1}{4/3}$$

$$x = \frac{12}{4/3} = 9m$$

Article - 1

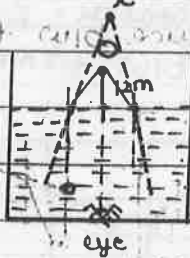
Apparent depth:-



$$\frac{H_i}{H_o} = \frac{\mu_2}{\mu_1}$$

→ $\mu_2 \rightarrow$ Refraction hone ke side jays jis medium me hai usi medium ka

refractive index

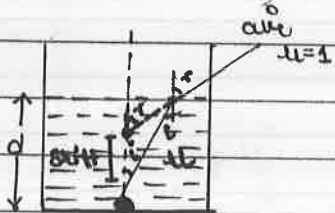


$$\frac{H_i}{H_o} = \frac{\mu_2}{\mu_1}$$

$$\frac{x}{12} = \frac{1}{3/4}$$

$$x = 4 \times 12 = 48m$$

AIMS → Refraction from plane surface se jab koi object usi side image -

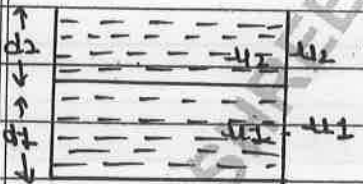


$$\frac{H_i}{H_o} = \frac{\mu_2}{\mu_1}$$

$$\frac{H_i}{d} = \frac{1}{\mu}$$

$$\star H_i = \frac{d}{\mu} \quad \mu \text{ medium must be air}$$

$$\text{shift} = \text{dactual} - \text{dapparent}$$

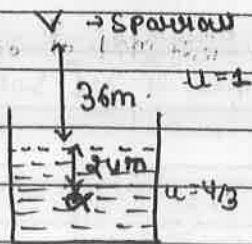


$$\text{dactual} = d_1 + d_2$$

$$\text{dapp} = \frac{d_1}{\mu_1} + \frac{d_2}{\mu_2}$$

Fish and Sparrow Question:-

Q1



$$\frac{x}{24} = \frac{1}{4/3}$$

$$\frac{x}{24} = \frac{3}{4}$$

$$x = \frac{24 \times 3}{4}$$

$$x = 18m$$

$$\frac{36}{20} = \frac{54}{54}$$

$$H = 36 + 18 = 54m$$

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पिछला → मछली की image

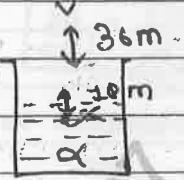
मछली की image गॉन बना सकता है → मछली [OBJECT]

$$\mu_R = 1$$

$$\mu = 4/3$$

$$H_o = 24m$$

$$36 + 18 = 54m$$



A fish at a depth of 30m below the surface of water. If RI of water = 4/3 then find out the distance b/w fish and its image?

$$\frac{H_i}{H_o} = \frac{\mu_R}{\mu}$$

$$\frac{x}{30} = \frac{1}{4/3}$$

$$\frac{x}{30} = \frac{3}{4}$$

$$\frac{30 \times 3}{4}$$

$$\frac{90}{4}$$

$$30m - \frac{90}{4}m$$

$$\frac{120 - 90}{4} = \frac{30}{4} = 7.5m$$

conceptual point:-

$$\vec{v}_{i/s} = \frac{\mu_R}{\mu} \vec{v}_{o/s}$$

velocity of image w.r. to surface

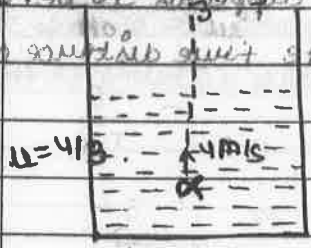
velocity of object w.r. to surface

μ_R → refraction hone ke bead jays iska med. me gadi usko RI

$$\vec{v}_{i/s} \times \mu = \mu_R \vec{v}_{o/s}$$

15/1/16

Q1. Find the velocity of image of bird as seen by fish.



bird \rightarrow object

$$\frac{v_{I/S}}{v_{O/S}} = \frac{\mu_R}{\mu^o}$$

$$\frac{x}{3} = \frac{4}{3}$$

$$3x = 4 \times 3$$

$$x = 4 \text{ m/s}$$

$$x = -4 \hat{j} \text{ m/s}$$

$$\frac{v_I - v_S}{v_O - v_S} = \frac{4}{3}$$

$v_S \rightarrow 20 \hat{i} 0$

$$v_{I/Fish} = v_I - v_F$$

$$= -4 \hat{j} - [+4 \hat{j}]$$

$$= -4 \hat{j} - 4 \hat{j}$$

$$v_{I/F} = -8 \hat{j} \text{ m/s}$$

$$\frac{x - 3 \hat{j} - 0}{-3 \hat{j}} = \frac{4}{3}$$

$$\frac{4x - 3 \hat{j}}{3}$$

$$v_I = -4 \hat{j} \text{ m/s}$$

Q2. Bird is at height 16m



हाइली की पिछला जहाँ दिखाई देगी?

$$\frac{H_I}{H_O} = \frac{\mu_R}{\mu^o}$$

$$\frac{x}{16} = \frac{4}{3}$$

$$3x = 4 \times 16$$

$$x = \frac{64}{3} \text{ m}$$

$$\frac{9 \text{ m} + 64}{3} = \frac{27 + 64}{3} = \frac{91}{3} \text{ m}$$

H.W

Module-6

Ex 1 = 27, 28, 33, 34, 35 ✓

Ex 2 → 1, 2 ✓

Ex 3 → 10, 11, 12, 13, 14 ✓

Date

Page No. 3 = 2, 3 ✓

22/09/2012

Saathi

Q4. To a fish in water, a bird in air appears to be at 30m from the surface. then calculate true distance of the bird from the surface?

Solve

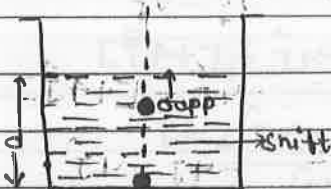
$$\frac{30}{x} = \frac{4}{3}$$

$$4x = 30 \times 3$$

$$x = \frac{90}{4}$$

$$x = 22.5 \text{ m}$$

Golden Key point :-



actual depth = d

$$\star \text{ app depth} = \frac{d}{\mu}$$

$$\star \text{ shift} = \text{actual} - \text{apparent}$$

Q1. A microscope focused on a mark in paper then a glass slab of thickness = 3cm and $\mu = 1.5$ is placed over the mark. How should the microscope is moved to get the mark in focus again?



$$\text{Shift} = \text{actual} - d_{\text{app}}$$

$$= 3 \text{ cm} - \frac{3}{1.5}$$

$$= 3 \text{ cm} - 2 \text{ cm}$$

$$= 1 \text{ cm}$$



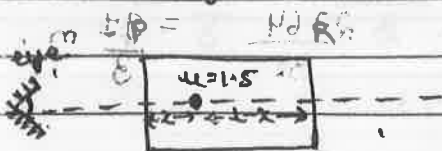
Q2. An Air bubble in glass slab with $\mu = 1.5$ is 5cm deep when viewed from top surface and 3cm deep when viewed from opp. face. Calculate the

(a) thickness of slab?

$$\frac{H_1}{H_0} = \frac{\mu R}{\mu}$$

$$\frac{5}{x} = \frac{1.5}{1.5}$$

$$x = 7.5 \text{ m}$$



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$$\frac{HI}{HO} = \frac{\mu R}{\mu_1}$$

$$\frac{3}{4.5} = \frac{1}{1.5} \quad \text{or } \frac{3}{4.5} = \frac{1}{1.5}$$

$$1 = 1.5 \times 2$$

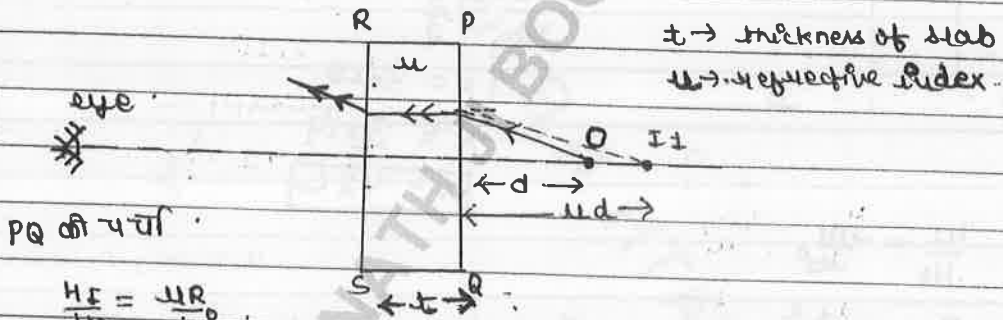
Concept:-



$$\text{Actual depth} = d_1 + d_2 + d_3$$

$$\text{apparent depth} = \frac{d_1}{\mu_1} + \frac{d_2}{\mu_2} + \frac{d_3}{\mu_3}$$

Normal shift:-



$$\frac{HI}{HO} = \frac{\mu R}{\mu_1}$$

$$\frac{HI}{d} = \frac{\mu}{1}$$

$$HI = \mu d$$

यदि \$RS\$ की:-

object की \$I1\$

$$\frac{HI}{HO} = \frac{\mu R}{\mu_1}$$

$$\frac{HI}{d+t} = \frac{1}{\mu}$$

$$HI = \frac{d+t}{\mu}$$

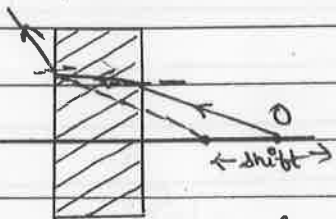
$$\text{shift} = (d+t) - (d + \frac{t}{\mu})$$

$$t - d - \frac{t}{\mu}$$

$$\text{shift} = t \left(1 - \frac{1}{\mu} \right)$$

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$$\text{Shift} = t \left(1 - \frac{1}{\mu} \right)$$



shift = +ve
always in the direction of light

Q1. The width of the slab is 6cm and $\mu = 3/2$. If the rear surface is silvered and the object is placed at a distance of 20cm from the front face then calculate the final position of image from the silvered surface.

$$\frac{\mu_1}{H_1} = \frac{\mu_2}{H_2}$$

$$\frac{x}{20} = \frac{3}{2}$$

$$2x = 3 \times 20$$

$$x = 3 \times 14$$

$$x = 42 \text{ cm}$$

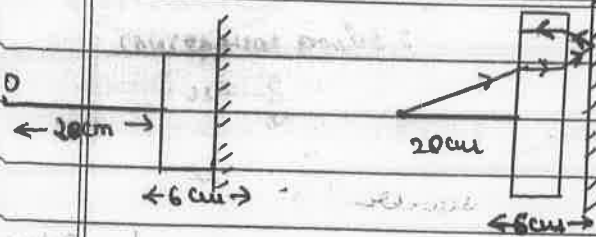
$$\frac{\mu_1}{H_1} = \frac{\mu_2}{H_2}$$

$$\frac{x}{42} = \frac{2}{3}$$

$$3x = 2 \times 42 = \frac{2 \times 14}{2}$$

$$34 - 2 = 32 \text{ cm}$$

$$3x = 20 \text{ cm} + 6 = 34 \text{ cm} \quad | \text{bu}$$



Shift = 6 cm

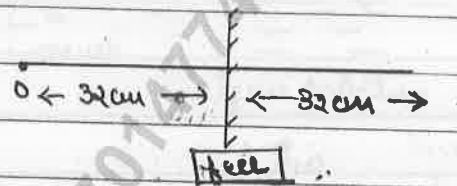
$$u \left(1 - \frac{1}{\mu} \right)$$

$$6 \left(1 - \frac{1}{3/2} \right)$$

$$6 \times \frac{1}{3} = 2 \text{ cm}$$

object की mirror से दूरी $20 + 6 = 34 \text{ cm}$

mirror की object = $34 - 2 = 32 \text{ cm}$



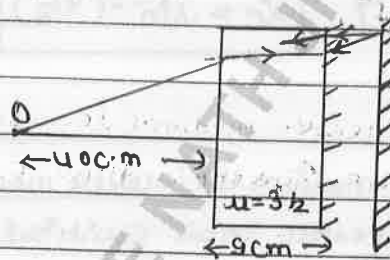
①

Shift = ②

30 cm

$$34 - 4 \text{ cm} = 30 \text{ cm}$$

Q3 In the given situation calculate the position of final image from the silvered surface?



$$40 + 9 = 49 \text{ cm}$$

$$40 - 3 = 37$$

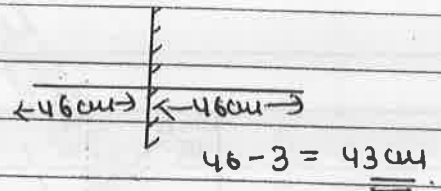
$$\text{appear} = 49 - 3 = 46 \text{ cm}$$

$$\text{Shift} = d - \frac{d}{\mu}$$

$$9 \left(1 - \frac{1}{3/2} \right)$$

$$9 \left(1 - \frac{2}{3} \right)$$

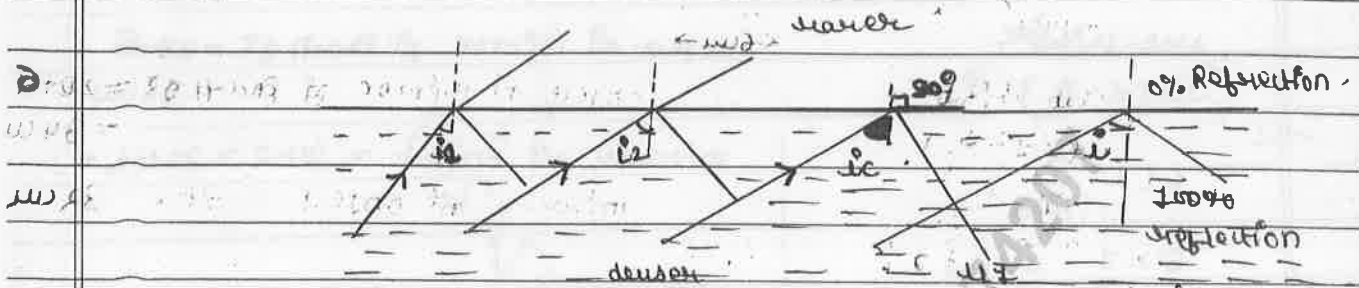
$$9 \times \frac{1}{3} = 3 \text{ cm}$$



$$46 - 3 = 43 \text{ cm}$$

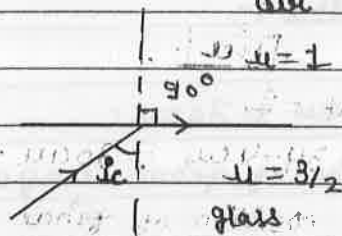
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Total Internal Reflection (TIR) :-



$i_c = \text{critical angle}$

$i > i_c$
TIR.



$$\frac{3}{2} \sin i_c = 1 \times \sin 90^\circ$$

$$\sin i_c = \frac{2}{3}$$

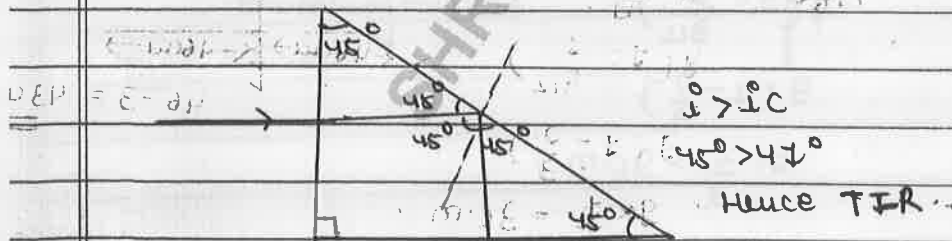
$$i_c = \sin^{-1}(\frac{2}{3})$$

NCERT

$$i_c = 42^\circ$$

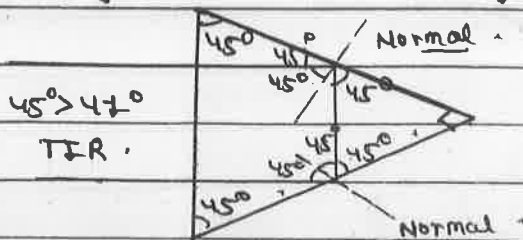
Conditions For TIR :-

- The ray must travel from denser medium to rarer medium.
- The angle of incidence must be greater than critical angle.



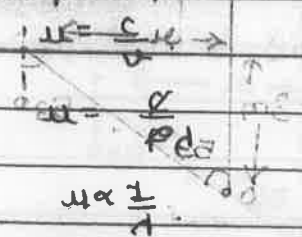
angle of incidence = 45°

If ray comes at 90° then it goes straight



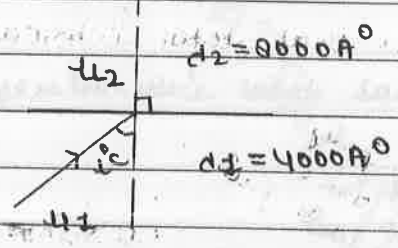
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Conceptual point :-

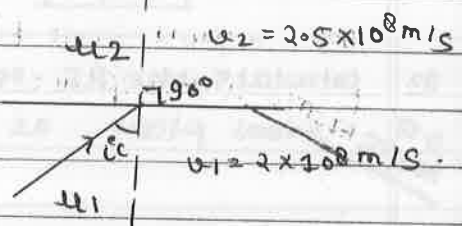


$v = f\lambda$
 $\mu = k/\lambda$
 $\mu \propto 1/\lambda$
 $\frac{\mu_1}{\mu_2} = \frac{v_2}{v_1}$

ex Q

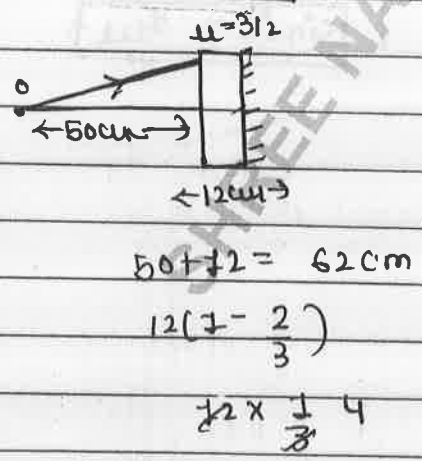


$\mu_1 \sin i_c = \mu_2 \sin 90^\circ$
 $i_c = \sin^{-1} \left(\frac{\mu_2}{\mu_1} \right)$
 $i_c = \sin^{-1} \left(\frac{8000}{4000} \right)$
 $\sin i_c = 1/2$
 $i_c = 30^\circ$

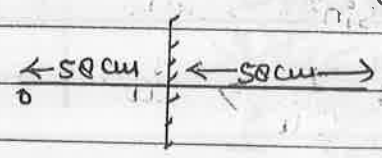


$\mu_1 \sin i_c = \mu_2 \sin 90^\circ$
 $i_c = \sin^{-1} \left[\frac{2 \times 10^8}{2.5 \times 10^8} \right]$
 $\sin i_c = 4/5$
 $i_c = 53^\circ$

Q1



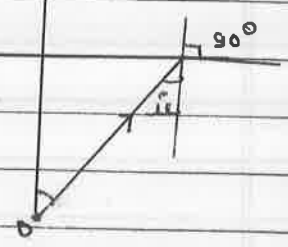
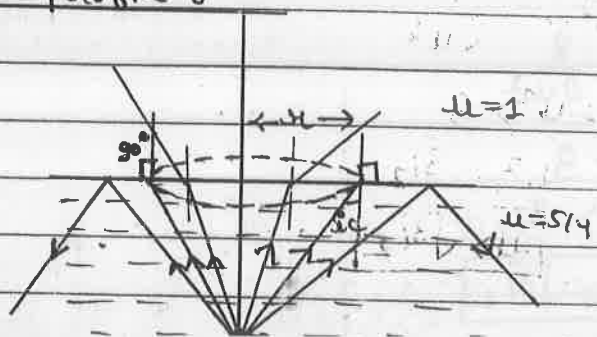
Final position of image = ?



$62 - 4 = 58 \text{ cm}$
 mirror or object
 50cm up above
 58cm

$62 - 8 = 54 \text{ cm}$

Most popular profile :-

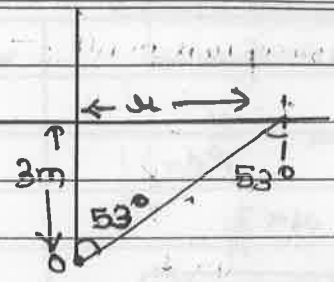


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$$\frac{5}{4} \sin i^{\circ} = 1 \times \sin 60^{\circ}$$

$$\sin i^{\circ} = \frac{4}{5}$$

$$i^{\circ} = 53^{\circ}$$



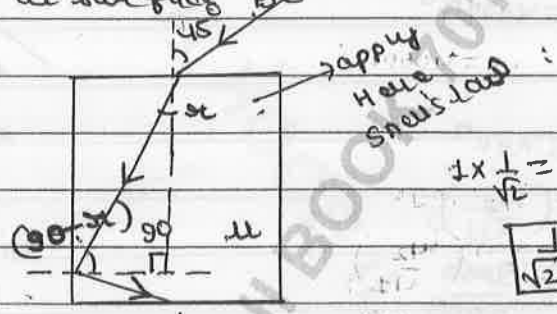
$$\tan 53^{\circ} = P/B$$

$$4/3 = u/8$$

$$u = 4m$$

I have asked them -
 $\pi r^2 = 16 \pi m^2$

Q2 Calculate the RI of material so that total internal reflection takes place at surface BC



$$1 \times \frac{1}{\sqrt{2}} = \mu \sin \alpha$$

$$\frac{1}{\sqrt{2} \mu} = \sin \alpha$$

First Basic requirement:-
 $90 - \alpha > i_c$

Snell's law

$$\mu \sin i^{\circ} = 1 \times \sin 90^{\circ}$$

$$\sin i^{\circ} = \frac{1}{\mu}$$

Sin both side

$$\sin(90 - \alpha) = \sin i_c$$

$$\cos \alpha > \sin i_c$$

$$\sqrt{1 - \sin^2 \alpha} > \sin i_c$$

$$\sqrt{1 - \frac{1}{2\mu^2}} > \frac{1}{\mu}$$

Square both side

$$1 - \frac{1}{2\mu^2} > \frac{1}{\mu^2}$$

$$1 > \frac{3}{2\mu^2}$$

$$2\mu^2 > 3$$

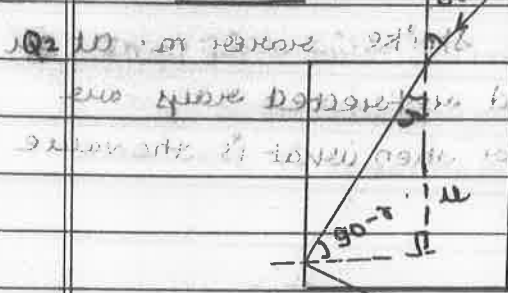
$$\mu^2 > \frac{3}{2}$$

$$\mu > \sqrt{\frac{3}{2}}$$



Neg Box = 3, 4
 solved eq = 25, 26, 27
 Ex I → 26, 28, 29, 32, 36, 37, 38, 39, 40
 Ex II → 5, 9, 11, 13, 41
 DAX III Homework → 4, 5, 6, 11

Saathi



$$1 \times \frac{\sqrt{3}}{2} = u \times \sin r$$

$$\frac{\sqrt{3}}{2} = \sin r$$

sin r c ni ugais

$$u \sin r = 1 \sin 90^\circ$$

$$\sin r = \frac{1}{u}$$

$90-r > r$

$$\sin(90-r) > \sin r$$

$$\cos r > \sin r$$

$$\sqrt{1-\sin^2 r} > \sin r$$

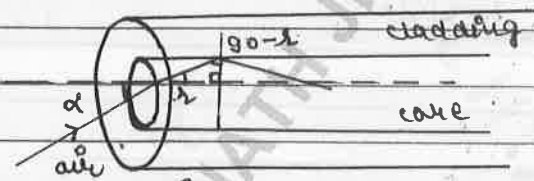
$$1 - \left(\frac{\sqrt{3}}{2u}\right)^2 \geq \left(\frac{1}{u}\right)^2$$

$$1 - \frac{3}{4u^2} > \frac{1}{u^2}$$

$$1 > \frac{1}{u^2} + \frac{3}{4u^2}$$

Q3 Popular $1 > \frac{1}{4u^2} + \frac{3}{4u^2} = 1 > \frac{4}{4u^2}$ $u = \frac{\sqrt{4}}{2}$

Optical Fiber :- Based on phenomenon on TIR.



$1 \times \sin \alpha = u_{\text{core}} \sin r$

$$\sin r = \frac{\sin \alpha}{u_{\text{core}}}$$

Left Basic aid

$90-r > r$

sin both side

$$\sin(90-r) > \sin r$$

sin r c ni ugais

$$u_{\text{core}} \sin r = u_{\text{cladding}} \sin \alpha$$

$$\sin r = \frac{u_{\text{cladding}} \sin \alpha}{u_{\text{core}}}$$

$\cos r > \sin r$

$$\sqrt{1-\sin^2 r} > \sin r$$

$$\frac{u_{\text{core}} - u_{\text{cladding}}}{u_{\text{core}}} > \frac{\sin^2 \alpha}{u_{\text{core}}}$$

$$\sqrt{1-\sin^2 \alpha} > \frac{u_{\text{cladding}}}{u_{\text{core}}}$$

$$\sin^2 \alpha < u_{\text{core}}^2 - u_{\text{cladding}}^2$$

$$1 - \frac{\sin^2 \alpha}{u_{\text{core}}^2} > \frac{u_{\text{cladding}}^2}{u_{\text{core}}^2}$$

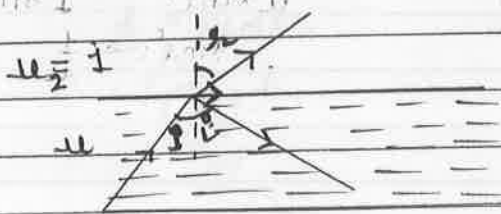
$$\sin \alpha = \sqrt{u_{\text{core}}^2 - u_{\text{cladding}}^2}$$

$$1 - \frac{u_{\text{cladding}}^2}{u_{\text{core}}^2} > \frac{\sin^2 \alpha}{u_{\text{core}}^2}$$

Learn

Date ___/___/___

Q. A ray of light from denser medium strike surface m . at an angle of i if the reflected and refracted rays are mutually perpendicular to each other then what is the value of critical angle?



$$i + r + 90 = 180$$

$$i + r = 90$$

$$\boxed{r = 90 - i}$$

$$\mu \sin i = 1 \sin r$$

$$\mu \sin i = \sin(90 - i)$$

$$\mu = \frac{\cos i}{\sin i} = \cot i$$

$\sin C$ on right side

$$\mu \sin C = 1 \times \sin 90$$

$$\mu \sin C = 1$$

$$\sin C = \frac{1}{\mu}$$

$$\sin C = \tan i$$

$$\boxed{C = \sin^{-1}(\tan i)}$$

Q. If light travels a distance S_1 in time t_1 in air and distance S_2 in time t_2 in a certain medium then calculate the critical angle for that medium?

Let velocity in air be $v_1 = \frac{S_1}{t_1}$

velocity in medium $v_2 = \frac{S_2}{t_2}$

$$v_2 = \frac{c}{\mu} = \frac{c \times \mu}{\mu}$$

$$\mu = \frac{c t_2}{S_2}$$

critical angle = $\mu_2 \sin C = \mu_1 \sin 90$

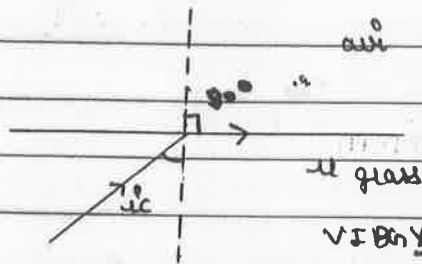
$$= \frac{c t_2}{S_2} \sin C = \frac{S_1}{S_2} \times 1$$

$$= \sin C = \frac{S_1 t_2}{S_2 t_1}$$

$$\boxed{C = \sin^{-1} \left(\frac{S_1 t_2}{S_2 t_1} \right)}$$

Date ___/___/___

Q6 In a given situation.



For colour of critical angle sabse μ wali angle Hoga?

$$\mu \sin i_c = 1 \times \sin 90^\circ$$

$$\sin i_c = 1/\mu$$

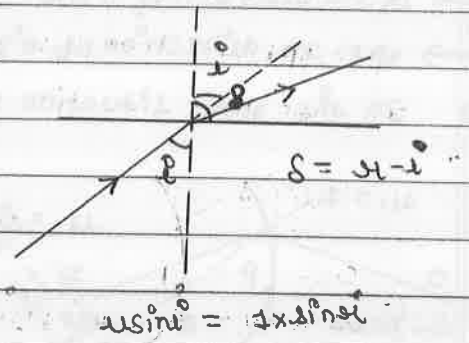
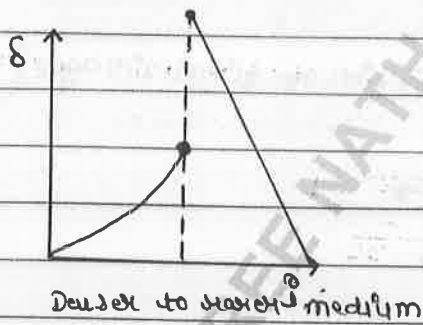
$\mu \propto d$

$$\text{Hence } \sin i_c \propto d$$

∴ For VIBGYOR $\rightarrow d$ increases
critical angle of Red colour is more.

Graph :-

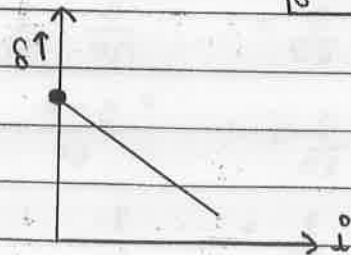
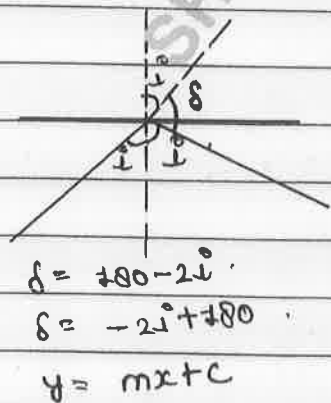
δ vs i :-



$$\sin^{-1}(\mu \sin i) = r$$

Now $f = \mu - i$

$$\delta = \sin^{-1}(\mu \sin i) - i$$



Q1 In the given situation find out the position of final image from the silvered surface?

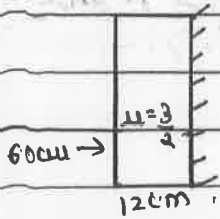
Date ___/___/___

$$\begin{array}{r} 20/30 \\ 10/15 \\ 5/15 \\ 5/15 \end{array}$$

$$\frac{3-2}{2} = \frac{1}{20} - \frac{1}{30}$$

$$\frac{\sin 53^\circ}{\cos 35^\circ} = \frac{6/12}{6/4}$$

$\tan 45^\circ = 1$
 $\theta = 53^\circ$
Saathi
 4/5



$$d = t \left(1 - \frac{1}{\mu} \right)$$

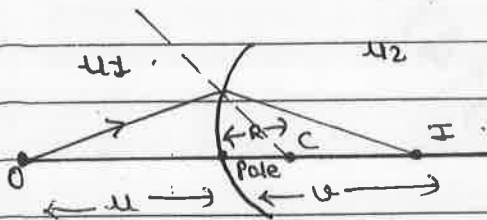
$$d = 12 \left(1 - \frac{1}{3/2} \right)$$

$$d = 12 \times \frac{1}{3} = 4 \text{ cm}$$

$$60 + 12 = 72 \text{ cm}$$

$$72 \text{ cm} - 8 \text{ cm} = 64 \text{ cm}$$

Refraction from curved surface :-



$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

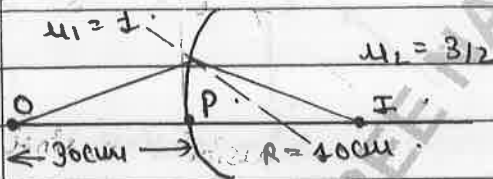
→ Always put u, v and R with their sign.

→ all the distance are measured from

→ In the direction of light = +ve pole

→ opp. to direction of light = -ve

Q2 In the given situation calculate the position of final image?



$$\frac{3}{2v} - \frac{1}{30} = \frac{3-1}{40}$$

$$\frac{3}{2v} - \frac{1}{30} = \frac{2}{40}$$

$$\frac{3}{2v} = \frac{1}{20} + \frac{1}{30}$$

$$\frac{3}{2v} = \frac{3-2}{60}$$

$$\frac{3}{2v} = \frac{1}{60}$$

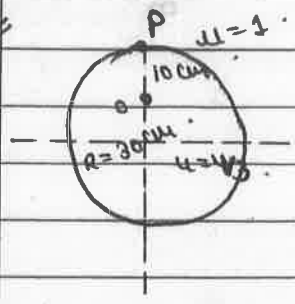
now solve for v to get $\frac{3 \times 60}{2} = v$

$$v = 90 \text{ cm}$$

Date ___ / ___ / ___

Q2

In the given situation Find out the apparent depth of bubble



$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$\frac{1}{v} + \frac{1}{30} = \frac{1 - 1.5}{30}$$

$$\frac{1}{v} = \frac{-1}{30} - \frac{1}{30}$$

$$\frac{1}{v} = \frac{-2}{30}$$

$$v = -\frac{30}{2}$$

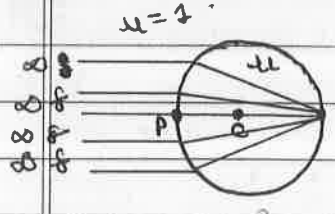
$$v = -15$$

$$v = -15$$

$$v = 15 \text{ cm}$$

Q3

In given situation find out μ



$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$\frac{\mu}{2R} - \frac{1}{\infty} = \frac{\mu - 1}{R}$$

$$\frac{\mu}{2R} = \frac{\mu - 1}{R}$$

$$\mu = 2\mu - 2$$

$$\mu = 2$$

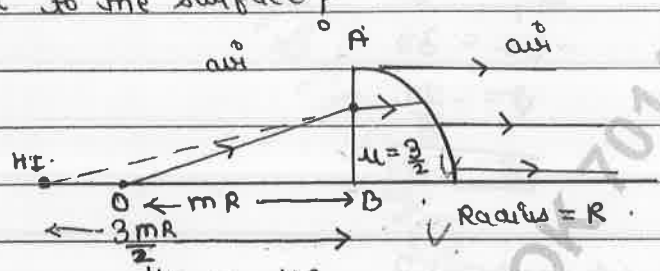
$$\frac{3mR + R}{2} = \frac{5mR}{2}$$

Saathi

Date ___/___/___

Solved

Q1. IIT Find out the value of m so that emergent ray becomes parallel to the surface?



Solve

$$\frac{\mu_i}{\mu_o} = \frac{\mu R}{R}$$

$$\frac{2}{mR} = \frac{3}{2}$$

$$2x = 3mR$$

$$x = \frac{3mR}{2}$$

Now wave surface -

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

Here $v \rightarrow \infty$ b/c ray becomes parallel

$$\frac{1}{\infty} + \frac{3}{\frac{2 \times 5mR}{2}} = \frac{1 - \frac{3}{2}}{R}$$

$$R \rightarrow -R$$

$$\frac{3}{5mR} = \frac{-1}{2R}$$

$$6R = -5mR$$

$$m = \frac{-6}{5}$$

Table :-

$$\mu_2 = 1$$

$$\mu_1 = 3/2$$

$$u = \mu_1 \mu_2 R \rightarrow (1 \cdot 5mR + R)$$

$n \rightarrow m$ check

H.W
 solved eg → 10, 19
 Beg Box → 5
 Ex 1 → 55, 56
 Ex 3 → Q7

Date / /

$7 = \frac{3}{4}x$

$\frac{3}{4}x = 21 - x$
 $3x = 4(21 - x)$
 $3x = 84 - 4x$
 $7x = 84$
 $x = 12$

21
 14
 7
 12
 Saathi

$\frac{1}{20} - \frac{3/2}{-(1.5mR + R)} = \frac{1}{-R}$

$\frac{3}{2(1.5mR + R)} = \frac{1}{2R}$

$\frac{3}{2(3mR + R)} = \frac{1}{2R}$

$\frac{3}{3mR + 2R} = \frac{1}{2R}$

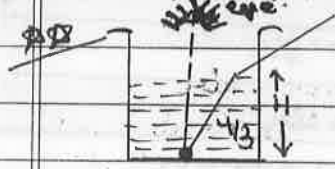
$\frac{3}{2R(\frac{3}{2}m + 1)} = \frac{1}{2R}$

$3 = \frac{3}{2}m + 1$

$3 - 1 = \frac{3}{2}m$

$2 = \frac{3}{2}m = \boxed{\frac{4}{3} = m}$

Conceptual points :-



$\frac{H_I}{H_O} = \frac{u_I}{u_O}$

$\frac{H_I}{H} = \frac{1}{4/3}$

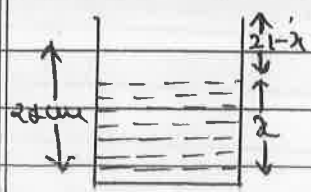
$H_I = \frac{3}{4}H$

$H_I = \frac{4}{3}H$

Optical → एवना नली
 H → बिनाई बिना
 रानी

Qa IIT :- Beaker → 24cm

किना 4नी भट, Half filled Half empty



$\frac{3x}{4} = 24 - x$

$x = 12cm$

$$\lambda = 15 + 45^\circ$$

$$\lambda = 60^\circ$$

$$\delta = i - \mu$$

$$\delta = 2 - 1$$

$$15 = 2 - 45$$

Saathi

Date: / /

Approach No = 2 [always work]

$$\frac{3x}{4-x} = \frac{50\%}{50\%} = 1$$

$$\frac{3x}{4-x} = 1$$

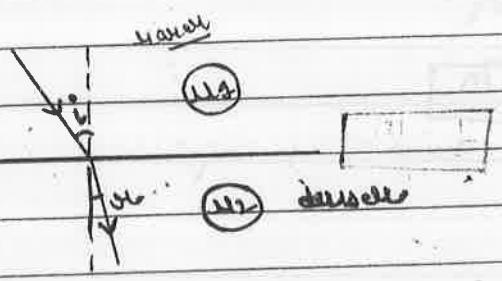
$$3x = 4 - 4x$$

$$7x = 4$$

$$x = \frac{4}{7} \text{ cm}$$

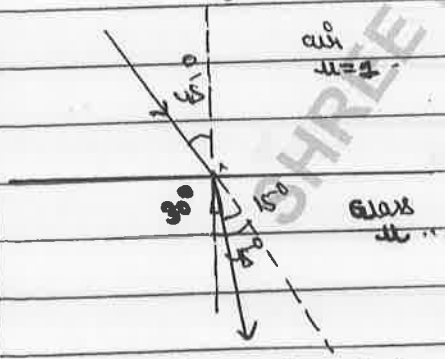
concept = 2

$$\mu_1 \sin i = \mu_2 \sin r$$



ex: air \rightarrow glass
 incident ray $\rightarrow 45^\circ$
 angle of deviation $\rightarrow 15^\circ$

$\mu_{\text{glass}} = ?$

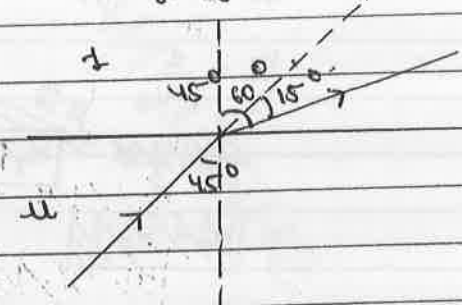


$$1 \sin 45^\circ = \mu \sin 30^\circ$$

$$\frac{1}{\sqrt{2}} = \mu \times \frac{1}{2}$$

$$\mu = \sqrt{2}$$

ex glass \rightarrow air
 incident ray $= 45^\circ$
 angle of deviation $= 15^\circ$



$$\mu \sin 45^\circ = 1 \sin 60^\circ$$

$$\mu \times \frac{1}{\sqrt{2}} = \frac{\sqrt{3}}{2}$$

$$\mu = \sqrt{\frac{3}{2}}$$

Date ___ / ___ / ___

concept = 3



गुणक $\frac{u}{v}$ eye	Quant $\frac{u}{v}$	गुणक $\frac{u}{v}$
		Here put $u = \frac{u}{v}$

Slab = $x \left(1 - \frac{1}{\mu} \right)$

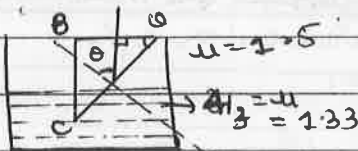
Both divide by $\frac{u}{v}$

Shift = $x \left(1 - \frac{1}{\mu} \right)$
 $\mu = \frac{u}{v}$

If 3 medium then derivation only can solve

Exercise-3

Q6



$\theta > \theta_c$
 $\sin \theta > \sin \theta_c$

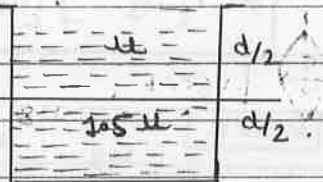
$\frac{3}{4} \times \sin \theta_c = \frac{4}{3} \sin 90^\circ$

$\sin \theta_c = \frac{4}{3} \times \frac{2}{3}$

$\sin \theta_c = \frac{8}{9}$

$\sin \theta > \frac{8}{9}$

Q6



Shift = d actual - d app

d app = $\frac{d \times 2}{1.5 \mu} + \frac{d}{\mu}$

$\frac{d}{2} = \frac{d}{3 \mu} + \frac{d}{2 \mu}$

$\frac{1}{2} = \frac{1}{3 \mu} + \frac{1}{2 \mu}$

$\frac{1}{2} = \frac{2 + 3}{6 \mu}$

$10 = 6 \mu$

$\mu = \frac{10}{6}$

$\mu = 5/3$

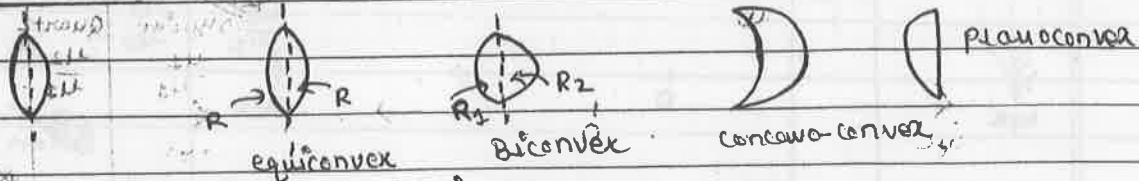
incident ray diverging then object is real.
 If convergent then object is virtual.

Saathi

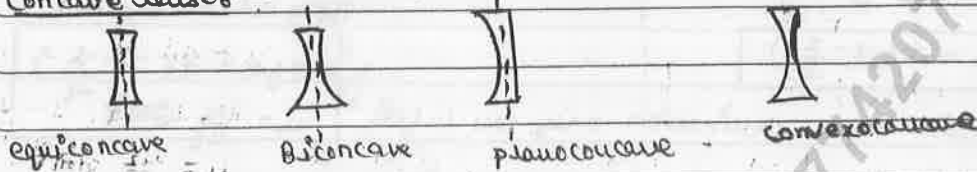
Date 07/08/2019

Lens

1. Convex lens :- lens which is thicker at center.



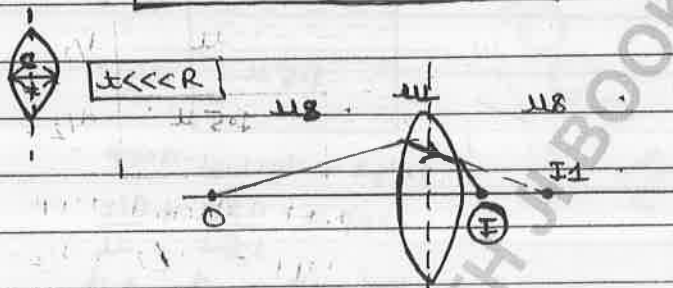
2. Concave lens :- lens which is thinner at center.



Lens maker formula :-

$$\frac{1}{f} = \left[\frac{\mu_l}{\mu_s} - 1 \right] \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

"all distance are measured from optical center C".

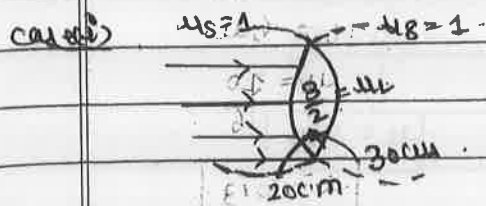


Step 1 :- $\frac{u_2}{v} = \frac{u_1}{u} = \frac{u_2 - u_1}{R}$

object $\rightarrow I_1$ Image $\rightarrow I_2$

Step 2 :- $\frac{u_1}{v} - \frac{u_1}{u} = \frac{u_2 - u_1}{R}$

Q In the given situation find out the focal length of lens?



$R_1 = +20 \text{ cm}$

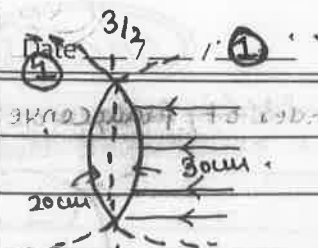
$R_2 = -30 \text{ cm}$

Sign of radii

$$\frac{1}{f} = \left(\frac{\mu_l}{\mu_s} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = \left[\frac{3}{2} - 1 \right] \left[\frac{1}{20} - \left(-\frac{1}{30} \right) \right]$$

$f = +24 \text{ cm}$



$R_1 = +30\text{cm}$
 $R_2 = -20\text{cm}$

$$\frac{1}{f} = \left(\frac{\mu_L}{\mu_S} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$f = +24\text{cm}$

NOTE → Focal length of lens does not depend on direction of incident ray.



$R_1 = +20\text{cm}$
 $R_2 = -30\text{cm}$
Sign की माकवाजी

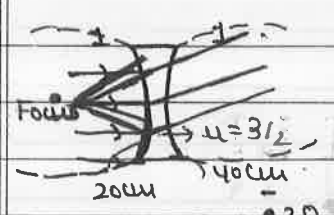
$$\frac{1}{f} = \left(\frac{\mu_L}{\mu_S} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$$= \left(\frac{3/2 - 1}{2}\right) \left(\frac{1}{20} + \frac{1}{30}\right)$$

$$\frac{1}{f} = -\frac{1}{4} \times \frac{1}{12}$$

$f = -48\text{cm}$

Q3 In the given situation calculate the focal length of the lens?



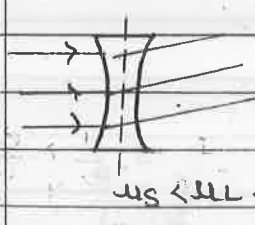
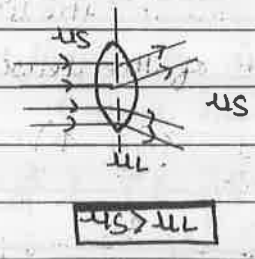
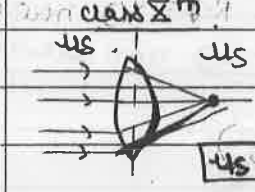
$$\frac{1}{f} = \left(\frac{\mu_L}{\mu_S} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

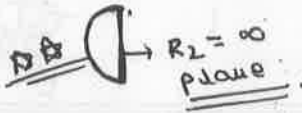
$$\frac{1}{f} = \left(\frac{3/2 - 1}{2}\right) \left[\frac{1}{20} - \frac{1}{40}\right]$$

$R_1 = +20$
 $R_2 = +40$
 $\frac{1}{f} = \left(\frac{1}{2}\right) \left(\frac{-2-1}{40}\right)$

$$\frac{1}{f} = -\frac{3}{80}$$

$f = -\frac{80}{3}\text{cm}$

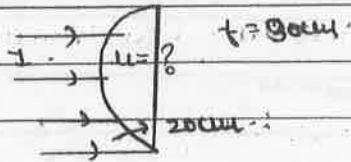




Saathi

Date ___/___/___

Q1 In a given situation find out refractive index of planoconvex lens if its focal length = 30cm?



$R_1 = +20\text{cm}$
 $R_2 = \infty$

$$\frac{1}{30} = (\frac{\mu}{1} - 1) \left(\frac{1}{20} - \frac{1}{\infty} \right)$$

$$\frac{1}{30} = \mu - 1 \times \frac{1}{20}$$

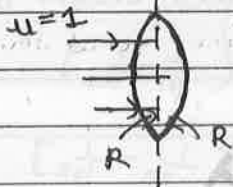
$$20 = 30\mu - 30$$

$$50 = 30\mu$$

$$\mu = \frac{5}{3}$$

equiconvex

Q2 The focal length of a biconvex lens is 40cm and R_1 of the lens is $\frac{3}{2}$ then calculate the radius of curvature?



$\mu = 1$

$\mu = \frac{3}{2}$

$R_1 = +R$

$R_2 = -R$

$f = 40\text{cm}$

$$\frac{1}{40} = \left(\frac{3}{2} - 1 \right) \left[\frac{1}{R} \right]$$

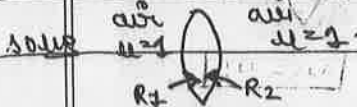
$$\frac{1}{40} = \frac{1}{2} \times \frac{1}{R}$$

$$\frac{1}{2} \times \frac{1}{4} = \frac{1}{8}$$

$$R = 40\text{cm}$$

Q3 The focal length of a biconvex lens ($\mu = \frac{3}{2}$) is 100cm when placed in air.

when the lens is immersed in the liquid have $R_1 = \frac{4}{3}$ now calculate the new focal length of the lens?



$\mu = \frac{4}{3}$ $\mu = \frac{4}{3}$



$$\frac{1}{100} = \left(\frac{3/2}{1} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = \left(\frac{3/2}{4/3} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1/100}{1/1} = \frac{1/2}{(3/2 - 1)}$$

$$\frac{1}{100} = \frac{1}{2} \times \frac{1}{1}$$

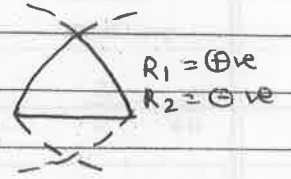
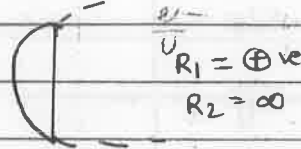
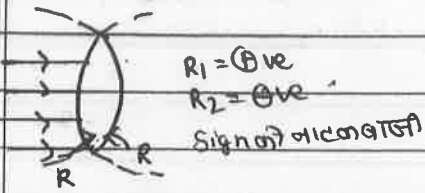
$$f = 8$$

focal length depend on Radius of curvature

Saathi

Date ___/___/___

conceptual points :-



$$\frac{1}{f} = \left(\frac{\mu}{\mu_s} - 1\right) \left[\frac{1}{R_1} - \frac{1}{R_2}\right]$$

$$f = \frac{R}{\mu - 1}$$

$$f = (\mu - 1) \times \frac{2}{R}$$

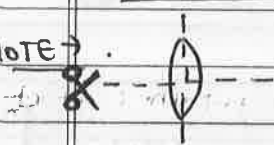
$$\frac{1}{f} = \left(\frac{\mu}{\mu_s} - 1\right) \left[\frac{1}{R_1} + \frac{1}{R_2}\right]$$

$$f = \frac{R}{2(\mu - 1)}$$

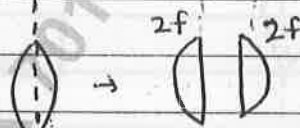
$$\frac{1}{f} = (\mu - 1) \times \left(\frac{2}{R}\right)$$

$$f = \frac{R}{2(\mu - 1)}$$

NOTE ->

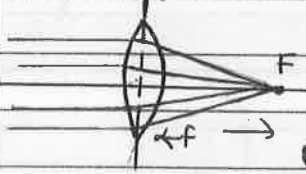


focal do not change



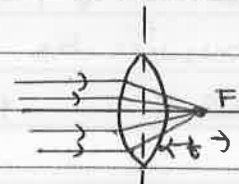
focal length increases

Power of lens :-



$$\text{Power} \propto \frac{1}{f}$$

power less



power more

unit of Power = dioptre (D)

always put f in meter [always remember]

magnification produced by lens :-

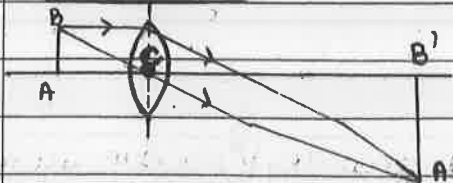
$$\frac{H_I}{H_O} = \frac{v}{u}$$

not for mirror

H_I -> Height of image

H_O -> Height of object

derivation :-



all distance are measured from optical center.

$$AB = CB$$

$$A'B' = CB'$$

$$\frac{+H_O}{+H_I} = \frac{+u}{+v}$$

$$\frac{H_I}{H_O} = \frac{v}{u}$$

$$\frac{H_I}{H_O} = \frac{v}{u}$$

* Convex (converging) $f = +ve$
 * Concave (diverging) $f = -ve$

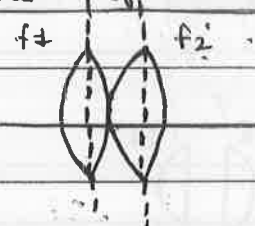
Ex I \rightarrow 74, 73, 72, 71, 70, 68, 66, 64, 63, 62, 60, 59, 58, 57

Date Ex II \rightarrow 1, 2, 3, 4, 5, 6, 9, 11, 13, 16, 19, 42, 57

saathi

$p = 1/f$	$p = -1/f$
$\frac{H_I}{H_O} = \frac{v}{u}$	$\frac{H_I}{H_O} = \frac{-v}{u}$
$\frac{1}{u} - \frac{1}{v} = \frac{1}{f}$ lens formula	$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$ mirror formula

Combination of Lenses - (Thin lenses in contact)



$$\frac{1}{f_{net}} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$P_{net} = P_1 + P_2$$

For. lens 2 the object's image made by lens 1

Question practice :-

Q1. 2 lenses having power: +2.5D and -3.75D are put in contact. then calculate the effective focal length of the combination?

solve \rightarrow $P_{net} = +2.5 + (-3.75)$
 $= -1.25D$

$$f = 1/p = \frac{100}{-1.25} = -80$$

$$f = -1/5 m$$



Q2. 2 lenses each having focal length 25cm are put in contact. out of them one is convex, another is concave. then calculate the eff. power of lenses?

solve $\frac{1}{f_{net}} = \frac{1}{25} - \frac{1}{25}$

$$\frac{1}{f_{net}} = 0 \quad f = \infty$$

Power $P = \frac{1}{f_{net}}$

$$P = \frac{1}{\infty} = 0$$



Q3. A Biconvex lens [$n=1.5$] having focal length 0.2m act as a divergent lens of power 1D when used in liquid. then calculate the RI of liquid?

solve ~~XXXXXXXXXX~~

$$\frac{1}{20} \times \frac{100}{1}$$

$$\frac{3}{2\mu} - 1 = \frac{3-2\mu}{2\mu}$$

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$$\frac{1}{20} = \left(\frac{3}{2} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right) \quad \text{--- (1) in air$$

Q. $P = -1D$ b/c it is diverging.

$$P = 1/f$$

$$= -1m = -100cm$$

$$-\frac{1}{100} \left[\frac{3}{2} - 1 \right] \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\frac{1}{20} = \frac{1/2}{3-2\mu}$$

$$\frac{1}{20} \times \frac{100}{1} \cdot -5 = \frac{3-2\mu}{2\mu}$$

$$-10\mu = 3 - 2\mu$$

$$9\mu = 15$$

$$\mu = 5/3$$

Q. An equiconvex lens has power = 5D if it is made of glass of $\mu = 3/2$. then calculate the radius of curvature of each surface?

soln

$$P = 5D$$

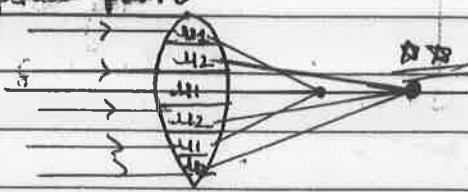
$$1/f = \frac{1}{50} \quad f = 1/P \quad f = 1/500$$

$$\frac{100}{50} = \left[\frac{3}{2} - 1 \right] \left[\frac{1}{R} + \frac{1}{R} \right]$$

$$\frac{20}{50} = \frac{1}{2} \times \frac{2}{R}$$

$$20 = R$$

NOTE . Conceptual point .



Q. 2 image will form .

- ①. $u > 2f$ = real
- ②. $f < u < 2f$ = real
- ③. $u = 2f$ = real
- ④. $u = f$ = no image
- ⑤. $u < f$ = virtual

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Exercise 3 Q7

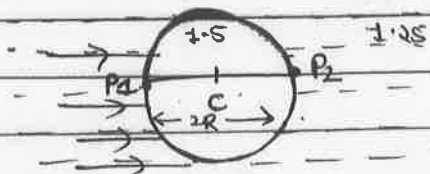


Table 1-

$u_2 \rightarrow 1.5$
 $u_1 \rightarrow 1.25$
 $u \rightarrow \infty$
 $v \rightarrow ?$
 $R \rightarrow +R$

$$\frac{u_2}{v} - \frac{u_1}{u} = \frac{u_2 - u_1}{R}$$

$$\frac{1.5}{v} - \frac{1.25}{\infty} = \frac{1.5 - 1.25}{R}$$

$$\frac{1.5}{v} = \frac{1}{4R}$$

$$\frac{3}{2v} = \frac{1}{4R}$$

$$v = 6R$$

Now $u_1 \times P_2$

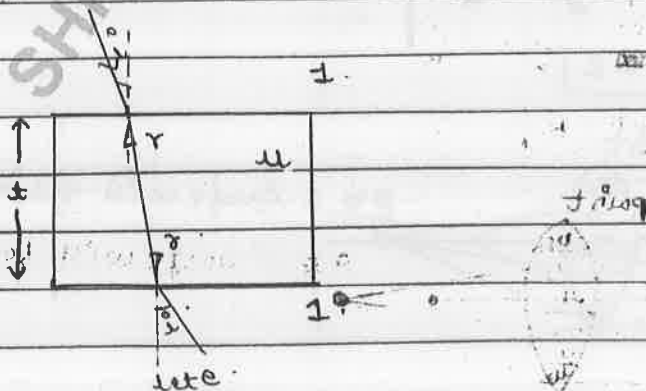
Table
 $u_2 \rightarrow 1.5$
 $u_1 \rightarrow 1.5$
 $u \rightarrow 4R$
 $v \rightarrow ?$
 $R \rightarrow -R$

on solving

$$v = 2R$$

but $v = 2R + R = 3R$

Concepts-



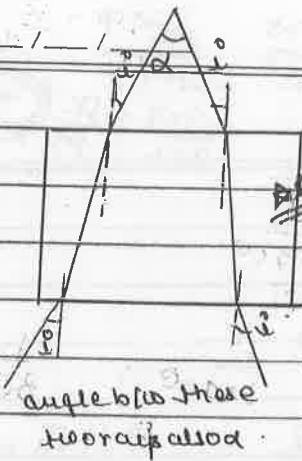
$$t \sin i = n \sin r \quad \text{--- (1)}$$

$$n \sin r = t \sin e \quad \text{--- (2)}$$

on comparing

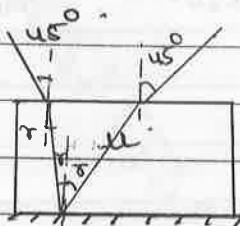
$$\sin i = \sin e$$

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~~no~~ zero deviation by glass slab.

Q2



- (i) find angle b/w incident ray and final emergent ray?
- (ii) deviation produced = ?

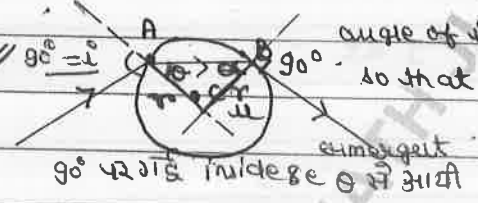
(i) angle b/w incident and final emergent ray = 45°



$$\delta + 90^\circ = 400^\circ$$

$$\delta = 90^\circ$$

Q3



angle of incidence = ?

so that grazing emergence will take place at B. B at 90° ray pass.

at A = $\mu \sin i = \mu \sin 90^\circ$

at B = $\mu \sin e = \mu \sin 90^\circ$

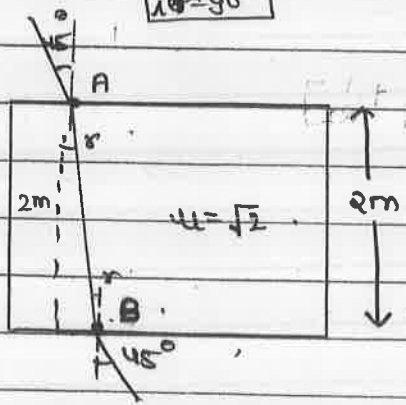
$$\mu \sin 90^\circ = 1$$

$$\mu \sin i = 1$$

$$\sin i = 1$$

$$i = 90^\circ$$

Q



$$\cos 30^\circ = \frac{2}{AB}$$

$$\frac{\sqrt{3}}{2} = \frac{2}{AB}$$

$$AB = \frac{4}{\sqrt{3}}$$

$$\mu \sin 45^\circ = \sin r$$

$$\sqrt{2} \times \frac{1}{\sqrt{2}} = \sqrt{2} \times \sin r$$

$$\sin r = \frac{1}{\sqrt{2}}$$

$$r = 30^\circ$$

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$$\frac{3 \times 10^8}{1.75}$$

$$\frac{1.75}{100}$$

$$\frac{1.75 \times 7}{100 \times 4}$$

$$\frac{3 \times 4}{3 \times 2} = \frac{12}{6} = 2$$

Saathi

If time of AB asked then

$$t = \frac{\text{distance}}{\text{Speed}} = \frac{4\sqrt{3}}{v}$$

$$u = \frac{c}{v}$$

$$\sqrt{2} = \frac{3 \times 10^8}{v}$$

$$v = \frac{3 \times 10^8}{\sqrt{2}}$$

$$\frac{4\sqrt{3}}{3 \times 10^8 \times \frac{1}{\sqrt{2}}}$$

$$\frac{4}{\sqrt{3}} \times \frac{\sqrt{2}}{3 \times 10^8}$$

$$= \frac{4\sqrt{2}}{3\sqrt{3}} \times 10^{-8} \text{ sec}$$

Q2.

$$\sqrt{2} \sin 45^\circ$$

$$u = 1$$

$$u = \sqrt{3}$$

$$u = \sqrt{2}$$

$$u = 2$$

$$u = 1.6$$

calculate the angle made by light ray with normal in the medium of $RI = \sqrt{2}$

★ Snell's law can applied directly b/w 2 RI

$$\text{b/c } \mu \sin i = \text{constant}$$

$$1 \times \sin 45^\circ = \sqrt{2} \sin r$$

$$1 \times \frac{1}{\sqrt{2}} = \sqrt{2} \sin r$$

$$\frac{1}{2} = \sin r \quad \boxed{r = 30^\circ}$$

Q3 A concave lens of glass $\mu = 1.5$ has both surface of same radius of curvature on emerging in medium of $\mu = 1.75$ then calculate its focal length?

soln



$$\frac{1}{f} = \left[\frac{3/2}{7} - 1 \right] \left[\frac{1}{R_1} + \frac{1}{R_2} \right]$$

$$\frac{1}{f} = \left[\frac{-1}{7} \right] \times \frac{2}{R}$$

$$\frac{1}{f} = \frac{-1 \times 2}{7 R}$$

$$\frac{1}{f} = \frac{-2}{7 R}$$

Focal length is $\frac{7R}{2}$ (Convergent)

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Q4. What is the RI of material of planoconvex lens if the radius of curvature of the curved surface is 20cm and focal length of lens = 30cm?

soln

$$\frac{1}{30} = \left[\frac{x}{f} - 1 \right] \left[\frac{+1}{10} - \frac{1}{\infty} \right]$$

$$\frac{1}{30} = (x-1) \times \frac{1}{10}$$

$$\frac{1}{3} = x-1$$

$$1 + \frac{1}{3} = x = \frac{4}{3}$$

$$x = \frac{4}{3}$$

Solving :-

lense $\rightarrow \frac{1}{f} = \left(\frac{\mu_l}{\mu_s} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$

$$P = \frac{1}{f}$$

$$P_{\text{eff}} = P_1 + P_2 + P_3 + P_4 + \dots$$

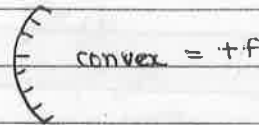
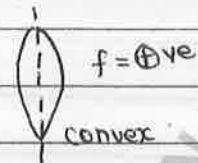
mirror :-

$$f = \frac{R}{2}$$

$$P = \frac{2}{-R}$$

Sign :-

Convex :-

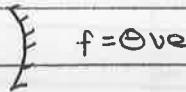
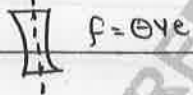


Concept :-

Convex = f = +ve

Concave = f = +ve

Concave :-



Q5. In the given situation and planoconvex lens have radius of curvature 20cm and its plane surface is silvered. The μ of material of lens = 3/2 then calculate the fnet of the system?

System :-

$$P_{\text{net}} = P_L + P_M + P_L$$

soln



$$\frac{1}{f_{\text{net}}} = \frac{1}{f_L} - \frac{1}{f_M} + \frac{1}{f_L}$$

$$R_1 = +20\text{cm}$$

$$R_2 = \infty$$

ray comes back

$$\frac{1}{f_{\text{net}}} = \frac{2}{f_L} - \frac{1}{f_M}$$

what i need? f_L and f_M

$$\frac{1}{f_L} = \left(\frac{\mu_l}{\mu_s} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f_L} = \left(\frac{3/2}{1} - 1 \right) \left(\frac{1}{20} \right) = \frac{1}{2} \times \frac{1}{20}$$

$$f_L = 40\text{cm}$$

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Now plane surface

$R \rightarrow \infty$

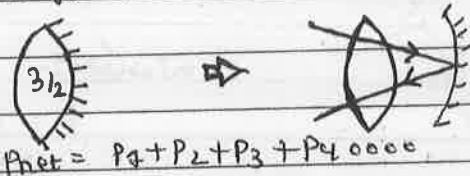
$$f_m = +\frac{R}{2} = \frac{\infty}{2} = \infty$$

$$\frac{-1}{f_{net}} = \frac{2}{40} - \infty$$

$$\frac{-1}{f_{net}} = \frac{1}{20}$$

$$f_{net} = 20 \text{ cm}$$

Q2 In the given situation calculate the f_{net} & the combination?



$$f_{net} = P_1 + P_2 + P_3 + P_4 \dots$$

$$\frac{1}{f_{net}} = \frac{1}{f_L} + \left(\frac{-1}{f_m}\right) + \frac{1}{f_L}$$

$$\frac{1}{f_{net}} = \frac{2}{f_L} - \frac{1}{f_m} \quad f_L = ? \quad f_m = ?$$

f_L की परी

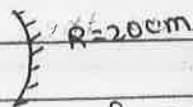


$$\frac{1}{f_L} = \frac{1}{2} \times \left[\frac{1}{20} - \left(\frac{-1}{20}\right) \right]$$

$$\therefore \frac{1}{f_L} = \frac{1}{2} \times \frac{1}{10}$$

$$f_L = 20 \text{ cm}$$

f_m की परी



$$f_m = \frac{R}{2}$$

$$f_m = \ominus 10 \text{ cm}$$

↳ concave

$$\frac{1}{f_{net}} = \frac{2}{20} - \frac{1}{10}$$

$$\frac{2}{20} + \frac{1}{10}$$

$$\frac{1}{f_{net}} = \frac{2}{10} - \frac{1}{10}$$

$$\frac{1}{f_{net}} = -\frac{1}{5}$$

$$f_{net} = -5 \text{ cm}$$

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$$\frac{2407}{20}$$

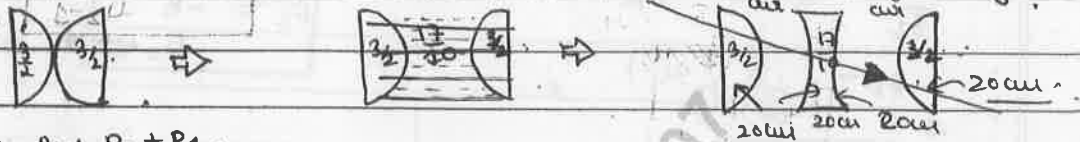
$$\frac{44000}{1400}$$

$$\frac{17}{10} - 1 = \frac{1707}{10} \cdot \frac{10}{10} = \frac{17}{10}$$



Q3. AIPMT 2015. 2 Identical thin planoconvex lenses $\mu = 1.5$ ($3/2$) each having radius of curvature 20cm are placed with their convex surface in contact at center. The space b/w the lenses is filled with oil ($\mu = 1.7$) then calculate the focal length of the combination?

Solve



$$P_{\text{net}} = P_1 + P_2 + P_3$$

$$\frac{1}{f_{\text{net}}} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3}$$

$$\frac{1}{f_{\text{net}}} = \frac{2}{f_1} + \frac{1}{f_3}$$

$$f_1 = ? \quad f_2 = ?$$

$$\frac{1}{f} = \left(\frac{\mu}{\mu_s} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$f_2 = \left(\frac{\mu}{\mu_s} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$f_2 = \left(\frac{17}{10} - 1 \right) \left(-\frac{1}{20} - \left(-\frac{1}{20} \right) \right)$$

$$\frac{1}{f} = \left[\frac{3}{2} - 1 \right] \left[\frac{1}{\infty} - \left(-\frac{1}{20} \right) \right]$$

$$f_2 = \frac{7}{10} \left(-\frac{1-1}{20} \right)$$

$$\frac{1}{f} = \frac{1}{2} \times \frac{1}{20}$$

$$\frac{1}{f_2} = \frac{7}{10} \times -\frac{2}{20}$$

$$f_1 = 40 \text{ cm}$$

$$\frac{1}{f_2} = \frac{7}{10} \times -\frac{1}{10}$$

$$f_2 = -\frac{100}{7}$$

$$\frac{1}{f_{\text{net}}} = \frac{2}{40} + \left(-\frac{7}{100} \right) = \frac{1}{20} - \frac{7}{100}$$

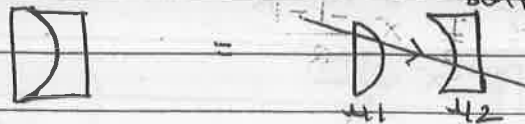
$$\frac{1}{f_{\text{net}}} = \frac{5 - 7}{100}$$

$$f_{\text{net}} = -50 \text{ cm}$$

$$f_{\text{net}} = -50 \text{ cm}$$

Q4. A planoconvex lens fit exactly into a planoconcave lens their plane surface are parallel to each other. If lenses are made of different materials having μ_1 and μ_2 . then calculate the focal length of the combination ($R =$ Radius of curvature of the curved surface).

Solve



$$\frac{1}{f_{\text{net}}} = \frac{1}{f_1} + \frac{1}{f_2}$$

Saathi

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$$\frac{1}{f_1} = (\mu_1 - 1) \left[\frac{1}{R} - \frac{1}{\infty} \right] \quad \frac{1}{f_2} = (\mu_2 - 1) \left[-\frac{1}{R} - \frac{1}{\infty} \right]$$

$$\frac{1}{f_1} = (\mu_1 - 1) \left(+\frac{1}{R} \right) \quad \frac{1}{f_2} = (\mu_2 - 1) \times -\frac{1}{R}$$

$$\frac{1}{f_1} = (\mu_1 - 1) \times \left(\frac{1}{R} \right)$$

$$f_2 = \frac{-R}{\mu_2 - 1}$$

$$f_1 = \frac{R}{\mu_1 - 1}$$

$$f_2 = \frac{R}{\mu_2 - 1}$$

$$\frac{1}{f_{net}} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$= \frac{1}{R} + \frac{1}{\left(-\frac{R}{\mu_2 - 1} \right)}$$

$$\frac{1}{f_{net}} = \frac{R(\mu_2 - 1) - R(\mu_1 - 1)}{R(\mu_1 - 1)(\mu_2 - 1)}$$

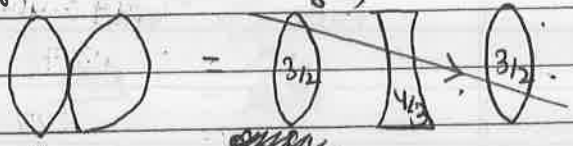
$$\frac{1}{f_{net}} = \mu_1 - \mu_2 + 1$$

$$f_{net} = \frac{R}{\mu_1 - \mu_2}$$

Q8 NEET=2016

Two identical equiconvex lens $[\mu = \frac{3}{2}]$ of focal length (f) each are kept in contact. space b/w lenses is filled with water ($\mu = \frac{4}{3}$) then calculate the focal length of the combination?

- (a) $3f/4$
- (b) $f/4$
- (c) $f/3$
- (d) $5f/4$



$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3}$$

$$\frac{1}{f} = \frac{2}{f} + \frac{1}{f_3}$$

$$= \frac{1}{f} = \frac{2}{f} + \frac{3R}{2} = ?$$

Solve

$$\frac{1}{f_3} = \left(\frac{3}{2} - 1 \right) \left[-\frac{1}{R} - \frac{1}{R} \right]$$

$$= \frac{1}{f} = \frac{1}{2} \times \frac{2}{R}$$

$$\frac{1}{f_3} = \frac{1}{3} \times \frac{-1-1}{R}$$

$$f = R$$

$$= \frac{3}{f} + \frac{3R}{2}$$

$$\frac{2}{f} + \frac{-2}{3R}$$

$$\frac{1}{f_3} = \frac{-2}{3R}$$

$$f_3 = \frac{3R}{2}$$

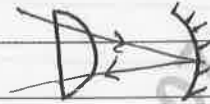
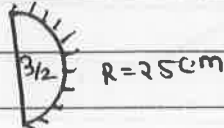
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$$\frac{1}{f_{\text{net}}} = \frac{2}{f} + \frac{1}{-3f/2}$$

$$= \frac{2}{f} - \frac{2}{3f}$$

$$= \frac{6-2}{3f} = \boxed{\frac{4}{3f} = f_{\text{net}}}$$

Q6. In the given situation calculate the Fnet of the system?



$$\frac{-1}{f_{\text{net}}} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3}$$

$$\frac{-1}{f_{\text{net}}} = \frac{2}{f_1} + \frac{1}{f_2}$$

$$f_m = -R/2 = -25/2$$

$$\frac{1}{f_1} = \frac{1}{4} \times \left[\frac{1}{\infty} - \frac{1}{25} \right]$$

$$\frac{1}{f_1} = \frac{1}{4} \times \frac{1}{25}$$

$$f_1 = \boxed{\frac{100}{50} \text{ cm}}$$

$$\frac{-1}{f_{\text{net}}} = \frac{1}{25} + \left(\frac{-3}{25} \right)$$

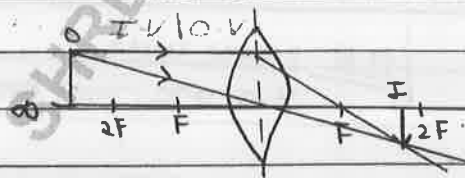
$$= \frac{1-3}{25}$$

$$= \frac{-2}{25}$$

$$f_{\text{net}} = \boxed{\frac{-25}{3}}$$

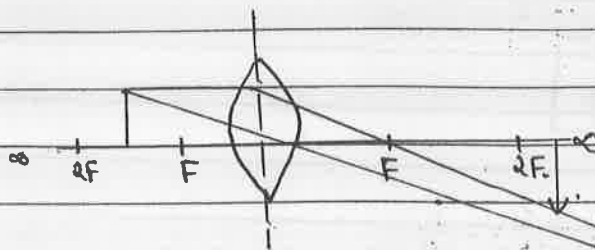
Ray tracing concept -

① Object is placed b/w ∞ and $2F$ -



- Real object
- Inverted
- F and 2F
- Diminished

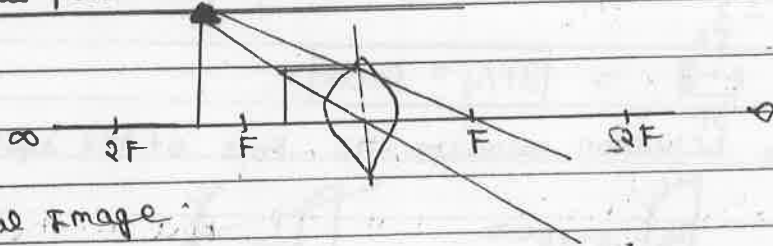
② B/w 2F and F



- Inverted
- Real
- b/w: 2F and ∞
- Enlarged

Date ___ / ___ / ___

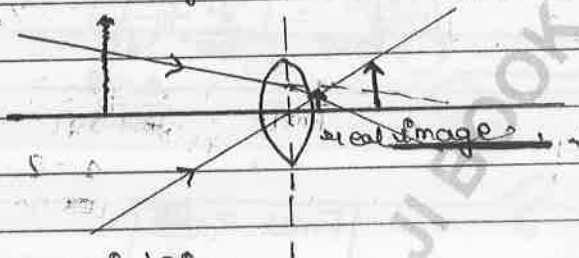
object is placed b/w F and C :-



- virtual image
- Enlarged
- Erect
- same-side

what about virtual object :-

If incidence rays are converging in nature = virtual object -



real image
diminished
Erect

Important points :-

- Real object or real image always inverted [RORI concept]
- Real object & real image (Focus) एका ही ओप. बाईले वरती ए.

For real object = $U = +ve$

- जेव्हा object वर वरि वी गुणे वी mention वरी एी वी Take as real object

~~R~~ convex lens
 $v.o/v.i$ not possible

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

- convex lens $f = +ve$
- concave lens $f = -ve$

Conceptual points :-

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{H_i}{H_o} = \frac{v}{u}$$

$$\frac{1}{f_{net}} = \left(\frac{1}{u_s} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

Date ___ / ___ / ___

Q1. A equi convex lens has a radius of curvature 20cm. An object is placed at a distance of 30cm from a lens and height of object is 2cm then describe the properties of image?

Soln

$$\frac{1}{f} = \left[\frac{1}{R_1} - \left(\frac{1}{R_2} \right) \right]$$

$$\frac{1}{f} = \frac{1}{R} \left[\frac{2}{20} \right]$$

$$f = 20 \text{ cm}$$

object $u = -30 \text{ cm}$ [real object]

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \left(-\frac{1}{30} \right) = \frac{1}{20}$$

$$\frac{30 + v}{30v} = \frac{1}{20}$$

$$600 + 20v = 30v$$

$$60v = 10v \quad \boxed{v = 60 \text{ cm}}$$

$$\frac{H_i}{H_o} = \frac{v}{u}$$

$$\boxed{H_i = -4 \text{ cm}}$$

inverted, Real image.

Q2. Lenses of dioptres 3D and -5 dioptres form compound lens. An object is placed at distance of 50cm from lens, then calculate the position of image?

Soln

$$P_{\text{net}} = P_1 + P_2$$

$$= 3D + (-5D) = -2D$$

$$\frac{1}{f} = P$$

$$f = -\frac{1}{2} \text{ cm}$$

$$f = \frac{100}{2}$$

$$\boxed{f = 50 \text{ cm}}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\boxed{v = -25 \text{ cm}}$$

$$\frac{1}{v} - \left(-\frac{1}{50} \right) = \frac{1}{50}$$

$$\frac{1}{v} + \frac{1}{50} = \frac{1}{50}$$

$$\frac{1}{v} = \frac{1}{50} - \frac{1}{50} = \frac{1}{v} = \frac{-1}{50}$$

Test Q
Q16, 19, 22, 21

Saathi

Date ___/___/___ Beg. Box = 6

Q3. A Convex lens of focal length of f produces a real image of ~~size~~ $\frac{1}{n}$ times the size of the object. calculate the position of object?

Solve object \rightarrow real \rightarrow real

Real object \rightarrow image \rightarrow inverted

$$H_I = \frac{1}{n} H_O$$

$$\frac{H_I}{H_O} = \frac{v}{u}$$

$$\frac{-1}{n} H_O = \frac{v}{u}$$

$$-\frac{1}{n} = \frac{v}{u}$$

$$v = -\frac{u}{n}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$-\frac{n}{u} - \frac{1}{u} = \frac{1}{f}$$

$$-\frac{n+1}{u} = \frac{1}{f}$$

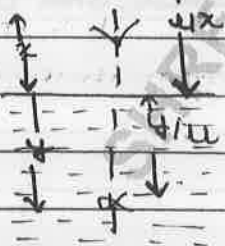
$$u = f(-n-1)$$

$$u = f(n+1)$$

object is placed at $(n+1)f$.

Question paper, Questions solution :-

Q16
Solve



$$\frac{H_I}{H_O} = \frac{11x}{\frac{11}{4}}$$

$$\frac{H_I}{2} = \frac{11}{4}$$

$$H_I = 11x$$

$$\frac{H_I}{H_O} = \frac{11}{4}$$

$$\frac{H_I}{4} = \frac{11}{4}$$

$$H_I = \frac{11}{4}$$

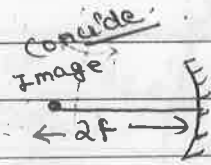
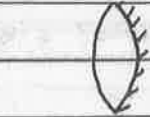
Q18 If an object put halfway of image of 2f वर ही बनीगी

Saathi

Date ___ / ___ / ___

Q19

Abhi



$$P_{net} = P_1 + P_2 + P_3$$

$$f_m = -\frac{R}{2}$$

$$D = 2f = \cancel{2f}$$

$$\frac{-1}{f_{net}} = \frac{1}{L} + \frac{1}{m} + \frac{1}{L}$$

$$\frac{-1}{f_{net}} = \frac{2}{\frac{R}{2(u-1)}} = \frac{1}{-R/2}$$

$$D = \frac{R}{(2u-1)}$$

$$\frac{-1}{f_{net}} = \frac{2}{L} + \frac{1}{m}$$

$$= \frac{4(u-1)}{R} + \frac{2}{R}$$

$$\frac{1}{f_L} = (u-1) \left[\frac{1}{R} + \frac{1}{R} \right]$$

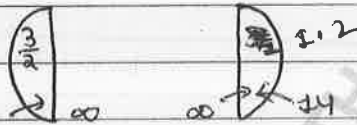
$$= \frac{4u-4+2}{R}$$

$$\frac{1}{f_L} = (u-1) \times \frac{2}{R}$$

$$f_L = \frac{R}{2(u-1)}$$

$$f_{net} = \frac{R}{2(2u-1)}$$

Q22



14

$$\frac{1}{f_1} = (1.5-1) \times \frac{1}{14}$$

$$\frac{1}{f_2} = (1.5-1) \times \frac{1}{14}$$

$$= \frac{0.5}{14}$$

$$\frac{1}{f_1} = 0.5 \times \frac{1}{14}$$

$$\frac{1}{f_2} = \frac{0.5}{14}$$

$$\frac{1}{f_1} = \frac{0.5}{14}$$

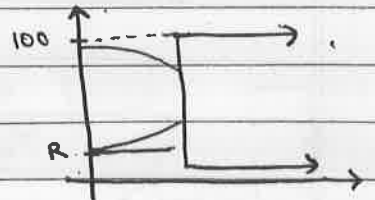
Q24

$v = 40 \text{ cm}$

$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\frac{1}{u} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{u} + \frac{1}{40} = \frac{1}{20}$$



$$\frac{0.5}{14} + \frac{0.5}{14}$$

$$\frac{1}{u} = \frac{1}{20} - \frac{1}{40}$$

$$\frac{1}{u} = \frac{2-1}{40}$$

$$f = \frac{14 \times 20}{0.7}$$

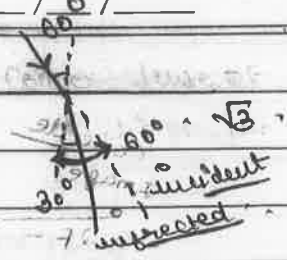
$$\frac{1}{u} = \frac{1}{40}$$

$$f = 20 \text{ cm}$$

$$u = 40 \text{ cm}$$

Date / /

Q8



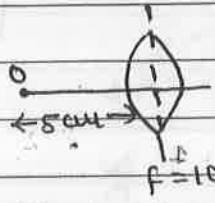
$$1 \sin 60^\circ = \sqrt{3} \sin r$$

$$\frac{\sqrt{3}}{2} = \sqrt{3} \sin r$$

$$\sin r = \frac{1}{2}$$

$r = 30^\circ$

Q5



$$\frac{H_I}{H_O} = \frac{v}{u}$$

$$= \frac{-20}{-5}$$

$H_I = 2H_O$

Q5) erect
virtual

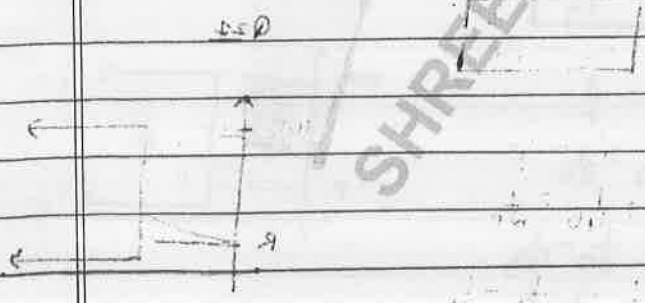
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{-5} = \frac{1}{10}$$

$$\frac{1}{v} = \frac{1}{10} - \frac{1}{5}$$

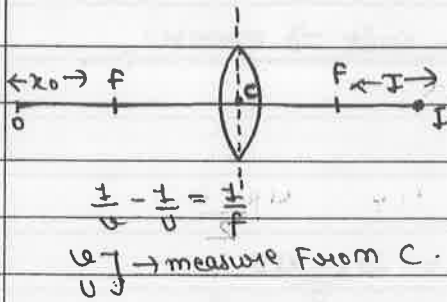
$$v = -10$$

$v = -10 \text{ cm}$



Date ___ / ___ / ___

Newton's Formula For Lense :-



$x_o \rightarrow$ distance of object from focus
 $x_i \rightarrow$ distance of image from focus

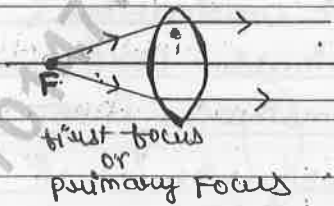
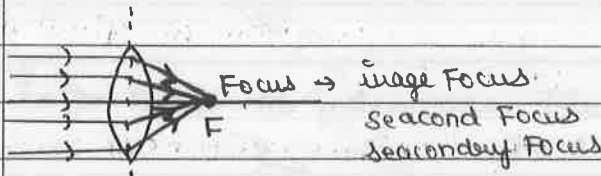
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$\frac{v}{U} \rightarrow$ measure from C.

$$x_o x_i = f^2$$

Newton's Formula

Object Focus and Image Focus :-



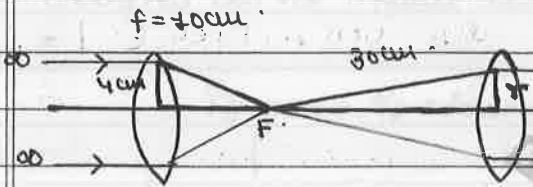
$v = \infty$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{\infty} + \frac{1}{f} = \frac{1}{f}$$

$$\frac{1}{u} = \frac{1}{f} - \frac{1}{f}$$

$$u = \infty$$

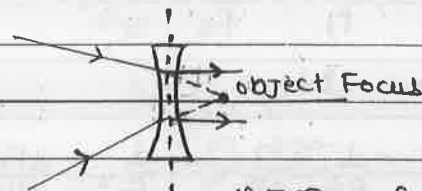
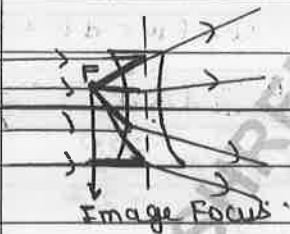


$$\frac{4}{70} = \frac{1}{30}$$

$$7 = 120 \text{ cm}$$

Object Focus :-

It is a point on principle axis where if the object is kept then light rays becomes parallel after refraction.



$v = \infty$ $f = -f$

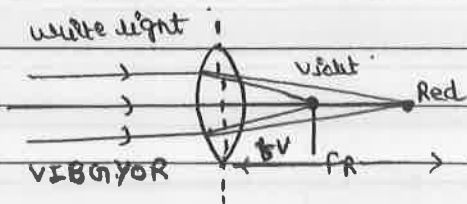
Concave

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{\infty} - \frac{1}{u} = \frac{1}{-f}$$

$$u = f$$

Chromatic Abberation :-



$$\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = (\mu - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$f \propto \frac{1}{\mu}$$

Cauchy's relation :-

$$\mu \propto \frac{1}{\lambda}$$

VIBGYOR

$\mu \rightarrow$ अलग अलग

μ_{Red} सबसे कम

$f \rightarrow$ अलग

$$f \propto \frac{1}{\mu} \propto \lambda = f_{red}$$

I. ST → 01

Date ___/___/___

Saathi

Chromatic (longitudinal) aberrations :- unit ⇒ meter.

$$L.C.A = f_R - f_V = f_w$$

f → focal length of mean colour

w → dispersive power

$$w = \frac{\mu_V - \mu_R}{\mu_y - 1}$$

$$\mu_y = \frac{\mu_R + \mu_V}{2}$$

Achromatic Combinations :-

1. ऐसा Combination जिसमें chromatic aberration की बीमारी नहीं होती।
2. ऐसा Combination जिसका L.C.A = 0
3. ऐसा Combination जिसमें Net focal length for all colour constant है।
4. ऐसा Combination जो chromatic aberration free है।

Chromatic combinations

$$\frac{w_1}{f_1} + \frac{w_2}{f_2} = 0$$

w₁ → dispersive power
w₂ →

f₁ → focal length
f₂ →

$$\frac{1}{f_{net}} = \frac{1}{f_1} + \frac{1}{f_2}$$

diff. both side

$$0 = -\frac{1}{f_1^2} \frac{df_1}{du} - \frac{1}{f_2^2} \frac{df_2}{du}$$

$$\mu_R - \mu_V = d\mu = f_w$$

$$\frac{d}{du} \left[\frac{1}{f} \right] = -\frac{1}{f^2}$$

$$0 = \frac{1}{du} \left[\frac{df_1}{f_1^2} + \frac{df_2}{f_2^2} \right]$$

$$0 = \frac{f_2 w_1}{f_1^2} + \frac{f_1 w_2}{f_2^2}$$

$$\frac{w_1}{f_1} + \frac{w_2}{f_2} = 0$$

$$\frac{1}{f} \times \mu$$

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Conceptual Notes

$$w_1 C_1 = f_1 R - f_1 = f_1 w_2$$

$$w = \frac{u_v - u_r}{f_{net}}$$

Achromatic Combination

$$\frac{w_1}{f_1} + \frac{w_2}{f_2} = 0$$

w_1, w_2 always positive.

Combination \rightarrow

one lens \rightarrow Convex

one lens \rightarrow Concave

Convex Concave

Combinations

$$P_{net} = P_1 + P_2$$

Possibility

$$P_1 = +4D$$

$$P_2 = -2D$$

$$P_{net} = P_1 + P_2$$

$$= 4 + (-2)$$

$$= +2D$$

Overall combination

Converging

Possibility

$$P_1 = +4D$$

$$P_2 = -4D$$

$$P_{net} = P_1 + P_2$$

$$= 4 + (-4)$$

$$= 0D$$

Overall comb.

Diverging

Q1 An Achromatic convergent doublet of 2 lenses in contact has a power of +2D.

The convex lens has a power +5D. Calculate the ratio of disp. Power of convergent and divergent lenses?

Solve

$$P_{net} = P_1 + P_2$$

$$+2 = 5 + (x)$$

$$2 - 5 = x \quad \boxed{x = -3D}$$

$$\frac{w_1}{f_1} + \frac{w_2}{f_2} = 0$$

$$\frac{w_1}{f_1} = -\frac{w_2}{f_2}$$

$$\frac{w_1}{w_2} = -\frac{f_2}{f_1}$$

$$\boxed{\frac{w_1}{w_2} = \frac{3}{5}}$$

$\frac{w_1}{w_2} = \frac{3}{5}$

0.012 / 10
0.024 / 20

Saathi

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Q. If the magnitude of dis. power of 2 lenses are 0.012 and 0.024 respectively then their focal length will be for Achromatic combination?

- (a) 10cm, -30cm
- (b) 5cm, -20cm
- (c) 10cm, -20cm
- (d) 20cm, -30cm

~~188~~ only by option method no other way of solⁿ.

$$P \frac{w_1}{f_1} + \frac{w_2}{f_2} = 0$$

Solⁿ:

$$0.012 + 0.024 = 0$$

$$\frac{f_1}{f_2} = -\frac{w_2}{w_1} = \frac{0.012}{0.024} = -\frac{1}{2}$$

Q. The dispersive power of material of 2 lenses are in the ratio 4/3. If the achromatic combination of these 2 lenses in contact is a convex lens of focal length 60cm then the focal length of component lenses are?

- (i) -20cm, 25cm = 4/5 (X)
- (ii) 20cm, -25cm = 4/5 (X)
- (iii) -20cm, +15cm = 4/3 (✓)
- (iv) +10cm, -25cm = 4/3 (✓)

$$\frac{w_1}{w_2} = -\frac{f_1}{f_2}$$

$$\frac{4}{3} = -\frac{f_1}{f_2}$$

60 f1

Solⁿ. $\frac{w_1}{f_1} + \frac{w_2}{f_2} = 0$

$$\frac{1}{f_{net}} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\frac{1}{60} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\frac{1}{60} = \frac{f_2 + f_1}{f_1 f_2}$$

$$60 = \frac{f_1 f_2}{f_2 + f_1}$$

$$\frac{w_1}{w_2} = -\frac{f_1}{f_2}$$

$$\frac{4}{3} = -\frac{f_1}{f_2}$$

$$\frac{1}{60} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$\frac{4}{3} = -\frac{f_1}{f_2}$$

$$\frac{4}{3} = -f_1 \times \frac{1}{60}$$

Now option (i) check on (ii)

(3) and (4)

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option ③

$-20\text{cm}, +15\text{cm}$

$$\frac{1}{f_{\text{net}}} = \frac{1}{f_1} + \frac{1}{f_2}$$

$$= \frac{-1}{20} + \frac{1}{15}$$

$$= \frac{-3+4}{60}$$

$$= \frac{1}{60} \text{ convex}$$

$f_{\text{net}} = +60\text{cm}$

option ③ is right

option -④

$20\text{cm}, -15\text{cm}$

$$\frac{1}{f_{\text{net}}} = \frac{1}{20} - \frac{1}{15}$$

$$= \frac{3-4}{60}$$

$$= -\frac{1}{60}$$

$f_{\text{net}} = -60\text{cm}$

lens displacement Method :-

This method is used to calculate focal length of the convex lens in the laboratory.

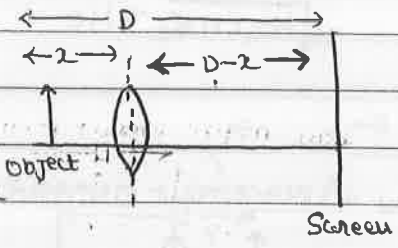
3 lines :-

$$f = \frac{D^2 - (\Delta x)^2}{4D}$$

$$D \geq 4f$$

$$H_o = \sqrt{H_f \times H_i}$$

APM → to calculate focal length of lens



object & screen fixed

Derivation

$$\frac{1}{u} - \frac{1}{v} = \frac{1}{f}$$

$$u \rightarrow -x \quad v = [D-x]$$

$$\frac{1}{(D-x)} - \frac{1}{-x} = \frac{1}{f}$$

on solving →

$$x^2 - xD + fD = 0$$

$$x^2 - xD + fD = 0$$

if we write

$$a=1 \quad b=-D \quad c=fD$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x_1 = \frac{D - \sqrt{D^2 - 4fD}}{2}$$

For real values of x

$$D^2 - 4fD > 0$$

$$D^2 > 4fD$$

$$D > 4f \text{ two values}$$

case #2

$$D^2 - 4fD = 0$$

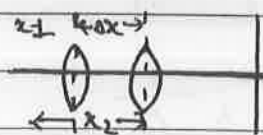
$$D = 4f$$

$$D = 4f$$

In this situation only one value of x is possible

APM → min separation

$$D = 4f$$

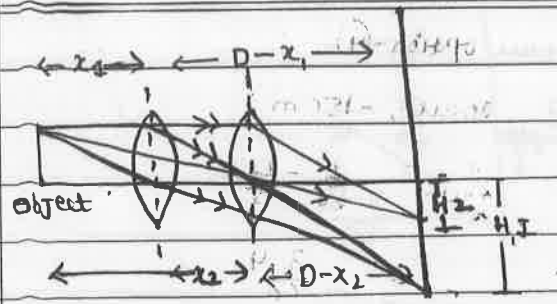


$$\Delta x = x_2 - x_1$$

$$x = \frac{D \pm \sqrt{D^2 - 4fD}}{2}$$

$$D = \frac{D^2 - 4fD}{2}$$

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Position-1

$$\frac{H_1}{H_0} = \frac{v}{u}$$

$$\frac{H_1}{H_0} = \frac{D-x_1}{-x_1}$$

Position-2

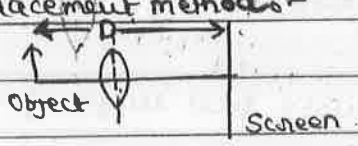
$$\frac{H_2}{H_0} = \frac{v}{u}$$

$$\frac{H_2}{H_0} = \frac{D-x_2}{-x_2} \quad \text{--- (2)}$$

$$\sqrt{H_1 \times H_2} = H_0$$

SHORT NOTES

New displacement method :-



Aim -> To calculate focal length

$$H_0 = \sqrt{H_{I1} \times H_{I2}}$$

$$D \geq 4f$$

$$f = \frac{D^2 - (\Delta x)^2}{4D}$$

Conceptual points :-



Intensity of image \propto area of aperture



Image is -ve
Brightness

Intensity of image

$$f = \frac{D^2 - (\Delta x)^2}{4D}$$



P.T.O

Ex I → Q57-81 all Discussed
 Ex II → 2, 3, 6, 7, 12, 17, 20, 24, 26, 28, 35, 42, 50, 63
 Ex III → Q12, Q15
 77 → 80, 79 → 81
 Date ___/___/___

Saathi

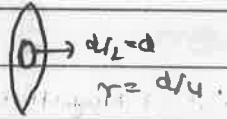
ATPMT →



$$r = d/2$$

$$\text{area} = \pi(r)^2 = \frac{\pi d^2}{4}$$

$$\text{Intensity} = I$$



$$\text{area} = \pi \frac{d^2}{16} = \frac{\pi d^2}{16}$$

$$\text{remaining} = \frac{\pi d^2}{4} - \frac{\pi d^2}{16}$$

$$\frac{4\pi d^2 - \pi d^2}{16} = \frac{3\pi d^2}{16}$$

$$\frac{I_1}{I_2} = \frac{A_1}{A_2}$$

$$\frac{I}{I_2} = \frac{\pi d^2/4}{3\pi d^2/16}$$

$$I_2 = \frac{3}{4} I$$

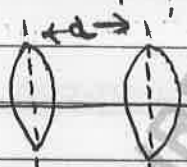
total length में निरंतर change नहीं आयेगा।

Conceptual point :-

Case 1 → when lens are in contact



$$\frac{1}{f_{\text{net}}} = \frac{1}{f_1} + \frac{1}{f_2}$$



d → separation b/w lenses

$$\frac{1}{f_{\text{net}}} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$

Ex I → Q75

$$x_o x_i = f^2$$

$$25(40) = f^2$$

$$f^2 = 1000$$

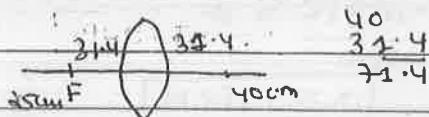
$$f = 10\sqrt{10}$$

$$f = 31.4 \text{ cm}$$

$$m = \frac{H_i}{H_o} = \frac{v}{u}$$

$$= \frac{71.4}{58.4} = 1.3$$

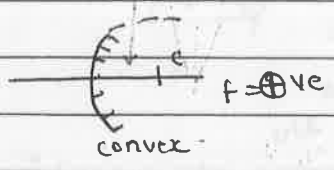
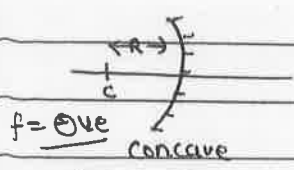
$$m = -1.3$$



$$25 + 31.4 = 56.4 \text{ cm}$$

Date ___ / ___ / ___

Mirror :-

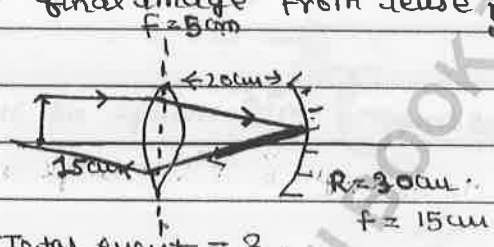


$$f = \frac{R}{2}$$

सबसे व दूर
mirror के सामने
front → Negative
U
v } → negative
f }

Q1. In the given situation, lens and mirror are 20cm apart and object is placed 15cm to left of the lens. determine the distance of final image from lens?

Solve



Solve

Total event = 3
→ Refraction from lens
→ reflection from mirror
→ Again Refraction from lens

event # 1

$$U = -15\text{cm}$$

$$f = +5\text{cm}$$

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$\frac{1}{-15} + \frac{1}{v} = \frac{1}{5}$$

$$\frac{1}{v} = \frac{1}{5} + \frac{1}{15}$$

$$\frac{1}{v} = \frac{3+1}{15}$$

$$\frac{1}{v} = \frac{4}{15}$$

$$v = \frac{15}{4} = 3.75\text{cm}$$

$$u = 7.5\text{cm}$$

event # 2

$$U = 20 - 7.5 = 12.5\text{cm}$$

$$v = ?$$

$$f = -15\text{cm}$$

mirror

$$\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$$

$$-\frac{1}{15} = \frac{1}{12.5} + \frac{1}{v}$$

$$-\frac{1}{15} - \frac{2}{25} = \frac{1}{v}$$

$$-\frac{2+6}{75} = \frac{1}{v}$$

$$-\frac{8}{75} = \frac{1}{v}$$

$$v = -\frac{75}{8} = -9.375\text{cm}$$

$$v = +75\text{cm}$$

2 40, 20, 60
 10, 15, 30
 5, 15, 15
 3, 11, 11
 1, 1, 1

20x5
 10x7 10x2
 10
 10
 10

5.27
 95
 95
 10

5.955
 29.19, 1

4 19x5
 95

Saathi

event = 3

$V = +0.75 + 20 = 95 \text{ cm}^{-1}$

$V = ?$

$f = 50 \text{ cm}$

$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$

$\frac{1}{5} = \frac{1}{v} + \frac{1}{95}$

$\frac{1}{5} - \frac{1}{95} = \frac{1}{v}$

$\frac{19-1}{95} = \frac{1}{v}$

$\frac{95}{18} = v$

2 40, 30, 60
 20, 15, 30
 10, 15, 15
 5, 15, 15
 5, 3, 3
 5, 1, 1

20x2
 10x2
 100x5
 900

Q2. 2 planoconcave lenses of glass ($\mu = 1.5$) have radius of curvature 20 cm and 30 cm . they are placed in contact with curved surface towards each other and space b/w them is filled with a liquid ($\mu = 1.3$) then calculate the focal length of the system?

Solve



$\frac{1}{8} - \frac{1}{20}$

$\frac{1}{f_{net}} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3}$
 $= -\frac{1}{40} + \frac{1}{30} + (-\frac{1}{60})$
 $= -\frac{1}{40} + \frac{1}{36} - \frac{1}{60}$
900

$\frac{1}{f} = (\frac{1}{2}) \times \frac{1}{10} [-\frac{1}{20}]$

$\frac{1}{f} = \frac{1}{2} \times (-\frac{1}{20})$

$\frac{1}{f} = \frac{1}{40} \quad f_1 = -40 \text{ cm}$

$\frac{1}{20} + \frac{1}{20}$
2

event 2

$\frac{1}{f} = (\frac{4}{3} - 1) (\frac{2}{R})$

$\frac{1}{f} = \frac{1}{3} \times \frac{2}{R}$

$f = \frac{3R}{2}$

$f = \frac{60 \times 36}{2}$

event 3

$\frac{1}{f} = \frac{1}{2} \times -\frac{1}{R}$

$f = -60 \text{ cm}$

$= \frac{-9 + 116 - 6}{360}$

$= \frac{380}{-8}$

$= -72.5 \text{ cm}$

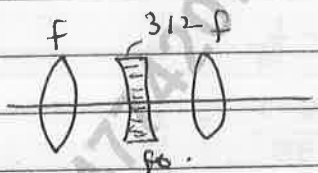
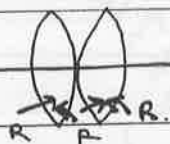
Date ___/___/___

Q3 NEET 2019 :-

Two similar thin equi-convex lens of focal length f of each are placed in contact such that focal length of comb. is F_1 when space b/w 2 lenses is filled with glycerine ($\mu = 1.5$) then eq. focal length is f_2

$$\frac{F_1 = ?}{F_2 = ?}$$

Solve.



$$\frac{1}{F_1} = \frac{1}{R} + \frac{1}{R}$$

$$\frac{1}{F_1} = \frac{1 \times 2}{R}$$

$$F_1 = R$$

$$\frac{1}{F_1} = \frac{1}{R} + \frac{1}{R}$$

$$f_{net} = \frac{1}{\frac{1}{f} + \frac{1}{f}}$$

$$f_{net} = f/2$$

$$f_1 = f/2$$

$$\frac{1}{f_0} = \frac{1}{2} \times \frac{2}{R}$$

$$f_0 = -R \quad f_0 = -f$$

$$\frac{1}{f_2} = 2 \times \frac{1}{2} + \frac{1}{f}$$

$$\frac{1}{f_{net}} = \frac{1}{f} + \frac{1}{f} + \frac{1}{f}$$

$$\frac{1}{f_2} = \frac{4}{f}$$

$$f_{net} = f$$

$$f_2 = f$$

$$\frac{f_1}{f_2} = \frac{R}{2f} = 1/2$$

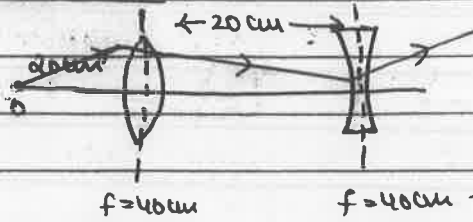
Date ___ / ___ / ___

2-40/60
20/30
10/15
5/15
1/3
1/11

40x3
120

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AIIMS = 2018



Position of Final image from O?

$$U = -40 + (-20) = -60 \text{ cm}$$

Solve

$$u = -20 \text{ cm}$$

$$v = ?$$

$$f = 40 \text{ cm}$$

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\frac{1}{40} = \frac{1}{v} + \frac{1}{20}$$

$$\frac{1}{40} - \frac{1}{20} = \frac{1}{v}$$

$$\frac{1-2}{40} = \frac{1}{v}$$

$$-\frac{1}{40} = \frac{1}{v}$$

$$\boxed{v = -40 \text{ cm}}$$

exit (2)

$$\frac{1}{p} = \frac{1}{v} - \frac{1}{u}$$

$$\frac{1}{40} = \frac{1}{v} + \frac{1}{60}$$

$$-\frac{1}{40} = \frac{1}{v} + \frac{1}{60}$$

$$-\frac{1}{40} - \frac{1}{60} = \frac{1}{v}$$

$$\frac{-3-2}{120} = \frac{1}{v}$$

$$\frac{-5}{120} = \frac{1}{v}$$

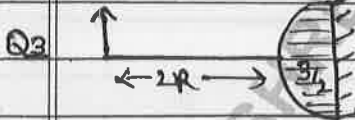
$$v = \frac{-120}{5} = -24$$

$$\boxed{v = -24 \text{ cm}}$$

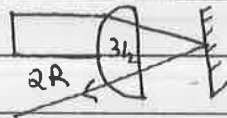
Overall magnification :-

$$m = m_1 \times m_2 \times m_3 \times m_4 \dots$$

Hemisphere of Radius R



A glass Hemisphere of radius R and material having $(\mu = 3/2)$ is silvered on its Flat Face then calculate the position of final image?



$$\frac{3}{2} - 1 = \frac{1}{2}$$

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Date ___ / ___ / ___

$$\frac{3}{2V} + \frac{1}{2R} = \frac{3-1}{2R}$$

$$\frac{3}{2V} = \frac{1}{2R} + \frac{1}{2R}$$

$$\frac{3}{2V} = \frac{2}{2R}$$

$$\boxed{\frac{3R}{2} = V}$$

$$\boxed{V = \infty}$$

event (2)

$$f = \frac{R}{2}$$

$$f = \infty$$

$$\frac{1}{f} = \frac{1}{R} + \frac{1}{R}$$

$$\frac{1}{\infty} = \frac{1}{R} + \frac{1}{R}$$

$$\frac{1}{\infty} = \frac{2}{R}$$

$$R = \infty$$

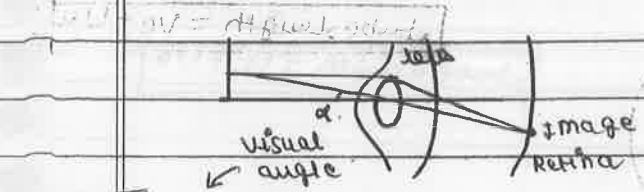
SHREE NATHJI BOOK 7014774207

20 (1) (a) point where the lens is placed is the focal point of the lens.

When the object is placed at the focal point of the lens, the rays of light become parallel and do not converge to form a real image.

Date ___ / ___ / ___

Optical Instruments :-



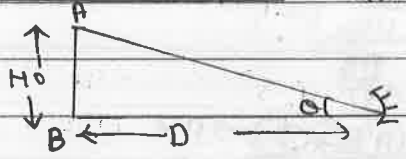
object α β α β
 वर α β α β angle.

$\text{magnifying Power} = \frac{\beta}{\alpha}$
 no unit

angle subtended by object at eye with the instrument

angle subtended by the object at eye without instrument

Eye microscope :- tiny objects

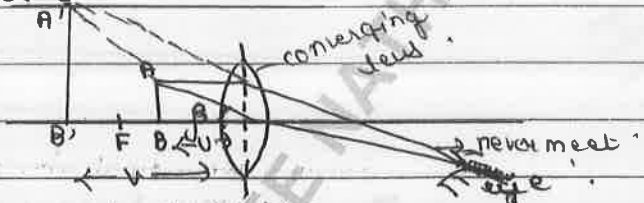


$D = 25\text{cm}$ least distance of distinct vision

$\tan \alpha = \frac{AB}{D} = \frac{H_0}{D}$

$\alpha = \frac{AB}{D}$

Simple Microscope :- (magnifying glass)



object's placed b/w F and C

$\Delta A'B'C$

$\tan \beta = \frac{A'B'}{U} = \frac{AB}{U}$

$\beta = \frac{AB}{U}$

case (i) final image formed at ∞

$v = \infty$ $u = 2f$

$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$

$m = \frac{\beta}{\alpha}$

$\alpha \rightarrow$ fixed

$\alpha = \frac{AB}{D}$

$m = \frac{D}{f}$

Normal adjustment
 mini magnifying power

$m = \frac{AB}{U} \cdot \frac{D}{AB}$

angular magnification case (ii) when image formed at 25cm.

$m = \frac{D}{U}$

$v = -D$ $u = -U$

$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$

$m = 1 + \frac{D}{f}$

max. magnifying power

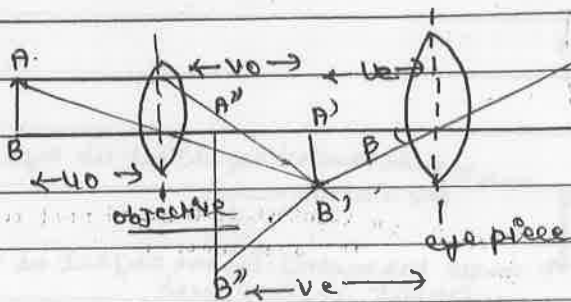
Final image is at 25cm of magnification and angular magnification same as 25cm

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Date ___ / ___ / ___

② Compound microscope :-

tube length = $v_o + v_e$



object AB

$$m_o = \frac{H I}{H O} = \frac{v_o}{u_o}$$

$$\frac{A'B'}{AB} = \frac{+v_o}{u_o}$$

magnification produced by objective lens

$$m_o = \frac{v_o}{u_o}$$

$$\text{tube } \beta = \frac{A'B'}{v_e}$$

$$\beta = \frac{A'B'}{v_e}$$

$$m = \frac{\beta}{\alpha}$$

$$= \frac{A'B'}{v_e} \times \frac{D}{AB}$$

$$M = \frac{A'B'}{v_e} \times \frac{D}{AB} \rightarrow m_e \times m_o$$

$$M = m_o \times m_e$$

Case 1 :-

when final image formed at ∞

$$M = m_o \times m_e$$

$$M = \frac{v_o}{u_o} \times \left[\frac{D}{f_e} \right]$$

Case 2 when final image formed at 25cm

$$m = m_o \times m_e$$

$$M = \frac{v_o}{u_o} \times \left[1 + \frac{D}{f_e} \right]$$

f_e = focal length of eye piece

Date ___ / ___ / ___

Short Notes :-

$M = \frac{D}{U}$ angular magnification

magnification :- $\frac{H_I}{H_O} = \frac{U}{U}$

[Transverse mag.]

Case 1 final image $\rightarrow \infty$

$m = \frac{D}{f}$ (min. magnifying power)

Case 2 final image $\rightarrow 25\text{cm}$

$m = 1 + \frac{D}{f}$ [max. magn. power]

Q18 :-

$f = 10\text{cm}$

$D = 25\text{cm}$

$m = \frac{H_I}{H_O} = \frac{U}{U}$

$\frac{1}{U} - \frac{1}{U} = \frac{1}{f}$

$\frac{1}{U} - \frac{1}{U} = \frac{1}{10}$ $U = -90\text{cm}$

$\frac{25}{90} = 10 = m$

Q19 Area of square = m^2 [area of object]

image = $10^2 [1\text{mm}^2]$

= 100mm^2

angular magnification = $\frac{D}{f} = \frac{25}{10} = 2.5$

Q20 $m = 1 + \frac{D}{f} = 1 + \frac{25}{10}$

$\frac{10+25}{10} = \frac{35}{10}$

$m = \frac{H_I}{H_O}$

$\frac{35}{10} =$

Q21 $v = -25\text{cm}$

$\frac{1}{U} - \frac{1}{U} = \frac{1}{f}$

$\frac{1}{25} - \frac{1}{U} = \frac{1}{10}$

$\frac{1}{25} - \frac{1}{10} = \frac{1}{U}$

$\frac{-2-5}{50} = \frac{1}{U}$

$\frac{-7}{50} = \frac{1}{U}$

$U = 50/7$ $U = -7.14\text{cm}$

Q22 $m = \frac{U}{U} = \frac{50}{7}$

$= \frac{50}{7} \times 2$

$= 7\frac{1}{2}$

21/11/20
 21/11/20
 21/11/20
 Date

$$\frac{1}{u_0} - \frac{1}{v_0} = \frac{1}{f}$$

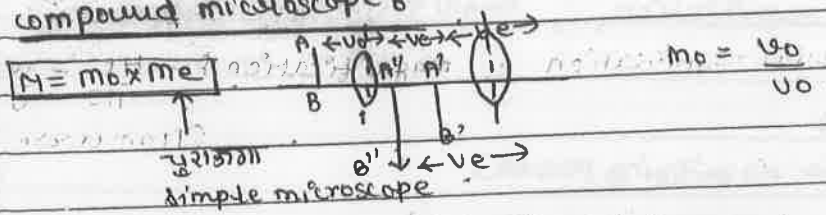
$$-\frac{1}{25} - \frac{1}{v_0} = \frac{1}{2}$$

$$-\frac{1}{25} - \frac{1}{2} = \frac{1}{v_0}$$

$$\frac{-2-25}{50} = \frac{1}{v_0}$$

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Compound microscope



Final image at ∞

$$M = m_o \times m_e$$

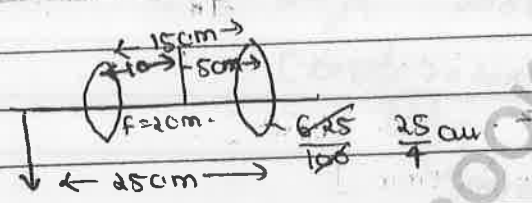
$$= \frac{v_o}{u_o} \left[\frac{D}{f} \right]$$

Final image at 25cm

$$M = m_o \times m_e$$

$$= \frac{v_o}{u_o} \left[1 + \frac{D}{f} \right]$$

Q12 tube length = 15cm
 $v_o + v_e = 15cm$



$$\frac{1}{10} - \frac{1}{v_o} = \frac{1}{10}$$

$$-\frac{1}{25} - \frac{1}{v_e} = \frac{1}{25}$$

$$\frac{1}{25} - \frac{4}{25} = \frac{1}{v_e}$$

$$\frac{-3}{25} = \frac{1}{v_e}$$

$$v_e = -5cm$$

$v_o = 10cm$
 $f_o = 10cm$

$$\frac{1}{v_o} - \frac{1}{u_o} = \frac{1}{f}$$

$$= \frac{1}{10} - \frac{1}{u_o} = \frac{1}{10}$$

$$= \frac{1}{10} - \frac{1}{u_o} = \frac{1}{10}$$

$$= \frac{10 - u_o}{10u_o} = \frac{1}{10}$$

$$= \frac{10 - u_o}{10u_o} = \frac{1}{10}$$

$$u_o = 20cm$$

Date ___ / ___ / ___

Q23: $f_e = 25 \text{ cm}$ final image = ∞

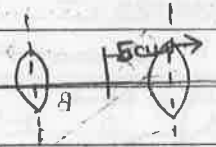
$f_e = 5 \text{ cm}$

$m = 30$

$m = 30$

$\frac{1}{u_e} - \frac{1}{v_e} = \frac{1}{f_e}$

$\frac{1}{\infty} - \frac{1}{v_e} = \frac{1}{5}$ $v_e = -5 \text{ cm}$



$m = m_o \times m_e$

$30 = \frac{v_o}{u_o} \left[\frac{25}{5} \right]$

$30 = \frac{v_o \times 5}{u_o} = \boxed{v_o = 6u_o}$ $u_o = u_o/6$

$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$

$\frac{1}{v} - \frac{1}{u_o/6} = \frac{1}{5}$
 $\frac{1}{v} - \frac{6}{u_o} = \frac{1}{5}$
 $\frac{1}{v} = \frac{1}{5} + \frac{6}{u_o}$

$\frac{1}{6u_o} + \frac{6}{u_o} = \frac{100}{125} \frac{1}{5}$

$\frac{7}{u_o} = \frac{4}{5}$

$\frac{7 \times 5}{4} = u_o$ $\frac{35}{4} = 8.75 = u_o$

tube length = $8.75 + 5 = 13.75 \text{ cm}$

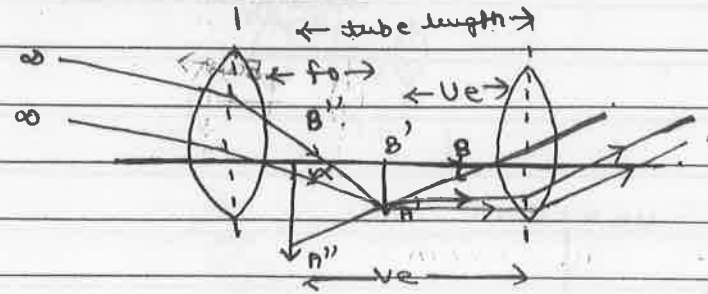
$\left[\frac{1}{u} + \frac{1}{v} \right]$

Ex → 82, 84, 87, 88 ✓
 II → 28, 30 ✓
 III →

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Date ___ / ___ / ___

Astronomical Telescope :- It is used to see distant objects.



$\tan \alpha = \frac{p}{B}$

objective
 Image → A'B'
 object → ∞

eye-piece
 $\tan \beta = \frac{A'B'}{u_e}$

$\tan \alpha = \frac{A'B'}{f_o}$

$M = \beta / \alpha$

$M = \frac{A'B'}{u_e} \cdot \frac{f_o}{A'B'}$

$M = \frac{f_o}{u_e}$

Case 1

Final image → ∞
 Normal adjustment

$u_e \rightarrow \infty \quad u_e \rightarrow -u_e$

$\frac{1}{u_e} - \frac{1}{u_e} = \frac{1}{f_e}$

$\frac{1}{\infty} - \frac{1}{-u_e} = \frac{1}{f_e}$

$u_e = f_e$

$\frac{f_o}{u_e} = \frac{f_o}{f_e} = M$

Case 2

Final image → 25 cm

$u_e = -D \quad u_e \rightarrow -u_e$

$\frac{1}{u_e} - \frac{1}{u_e} = \frac{1}{f_e}$

$\frac{1}{-D} - \frac{1}{-u_e} = \frac{1}{f_e}$

$\frac{1}{u_e} = \frac{1}{f_e} + \frac{1}{D}$

to multiply

$\frac{f_o}{f_e} + \frac{f_o}{D} = \frac{f_o}{u_e}$

$M = f_o \left[\frac{1}{f_e} + \frac{1}{D} \right]$

Date ___ / ___ / ___

Show a note on astronomical telescope :-

Final image is at infinity

Normal adjustment

Distance between objective and eyepiece

$$m = \frac{f_o}{f_e}$$

$$\text{Tube length} = f_o + f_e$$

sep. b/w lenses

angular magnification

Final image at 25 cm

$$m = m_o \left[\frac{1}{f_e} + \frac{1}{D} \right]$$

Q24

$$f_o = 140 \text{ cm}$$

$$f_e = 5 \text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

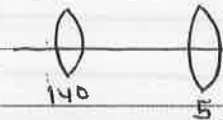
$$\frac{1}{\infty} - \frac{1}{u} = \frac{1}{5}$$

$$u = 5 \text{ cm}$$

$$m = \frac{f_o}{f_e}$$

$$= \frac{140}{5}$$

$$= 28$$



Q25

$$f_o \left[\frac{1}{f_e} + \frac{1}{D} \right]$$

$$140 \left[\frac{1}{5} + \frac{1}{25} \right]$$

$$\frac{140 \times 6}{25}$$

$$= 33.6$$

$$\frac{5 \times 2}{33.6}$$

Q26

$f_o + f_e = \text{tube length}$

$$140 + 5 = 145 \text{ cm}$$

Q27

$$m_o = \frac{H_i}{H_o}$$

$$= 20 = \frac{H_i}{H_o}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{\infty} - \frac{1}{u} = \frac{1}{140}$$

$$u = 140$$

$$\frac{x}{140} = \frac{140}{30000}$$

$$\frac{14}{3} = x$$

$$\frac{H_i}{H_o} = \frac{v}{u}$$

$$= \frac{x}{100} = \frac{140}{30000}$$

$$x = 7 \text{ cm}$$

$$\frac{x}{100} = \frac{140}{30000}$$

$$x = 7 \text{ cm}$$

Date ___/___/___

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Q27

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

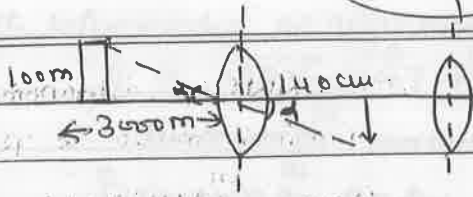
$$\frac{1}{v} - \frac{1}{3000 \times 100} = \frac{1}{140}$$

$$v = 140 \text{ cm}$$

उत्तर

$$\frac{20 \text{ cm}}{3000 \text{ m}} = \frac{HI}{140 \text{ cm}}$$

$$\frac{14}{3} = HI$$



Q28

$$\frac{1}{6} - \frac{1}{6} = \frac{1}{f_e}$$

$$-\frac{1}{25} - \frac{1}{u} = \frac{1}{5}$$

$$-\frac{1}{25} - \frac{1}{5} = \frac{1}{u}$$

$$-\frac{1-5}{25} = \frac{1}{u}$$

$$u = \frac{25}{-6}$$

$$H_o = \frac{14}{3}$$

$$\frac{HI}{H_o} = \frac{v}{u}$$

$$3HI = \frac{+25 \times 6}{+25}$$

$$14 \times \frac{6}{3} = HI$$

$$HI = 28 \text{ cm}$$

Q29

Q4

$$f_e = 5 \text{ cm}$$

$$m = 14$$

Tube length = ?

$$m = \frac{f_o}{f_e}$$

$$14 = \frac{f_o}{5}$$

$$14 \times 5 = f_o$$

$$70 + 5 = 75 \text{ cm}$$

Q30

$$50 = f_o + f_e$$

$$50 - f_e = f_o$$

$$g = \frac{f_o}{f_e}$$

$$g = \frac{f_o}{f_e} \Rightarrow 50 - f_e = g f_e$$

$$f_o = 45$$

$$g f_e = 50 - f_e$$

$$2 f_e = 50$$

$$f_e = \frac{50}{2} \Rightarrow f_e = 25 \text{ cm}$$

EX I → Q2-93 EX II → Q14, 22, 37

94-100

EX III → Q9

Ques → Q7-6, Q10, 11, 12, 13, 16, 17, 18-28

magnification = \ominus ve more accurate b/c image is inverted

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Date ___/___/___

Q13

$f_o = 144 \text{ cm}$

$f_e = 6 \text{ cm}$

$$m = \frac{f_o}{f_e} = \frac{144}{6} = 24$$

$f_o + f_e = 144 + 6 = 150$

Eye-defect [Myopia]

इसमें दूर के object साफ दिखाई ना देते हैं

For Normal eye :-

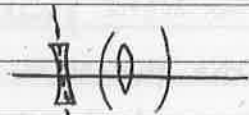
Near point = 25 cm

Far point = ∞

Myopic patient का Far point ∞ से कम है।



दूर के object को



Ex:-

Q1 A person cannot see beyond 2m. In order to see distant objects

lense used = ?

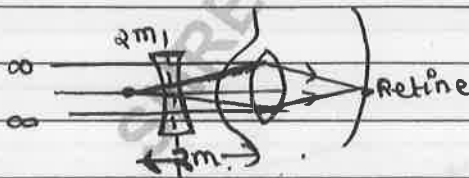
Power = ?

Focal length = ?

Soln

Cannot see beyond 2m होता है myopic patient है।

दूर के चीज नहीं दिखाई



$u = \infty$

$v = -2m$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{-2} - \frac{1}{\infty} = \frac{1}{f}$$

$f = -2m$

Power = $\frac{1}{-2} = -0.5 \text{ D}$ (concave)

Date / /

$$\frac{4 \times 3}{-12} = \frac{5}{300}$$

$$\frac{6 \times 5}{300} = \frac{4 \times 5}{300}$$

$$\begin{array}{l} 25, 60 \\ 25, 30 \\ 25, 15 \\ 25, 5 \\ 5, 1 \end{array}$$

Saathi

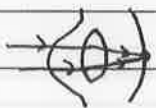
Hypermetropia :- इसमें पास के object को देखना नहीं है।

For normal eye -

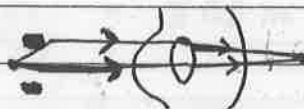
$$\text{Near point} = 25 \text{ cm}$$

$$\text{far point} = \infty$$

Hypermetropic Patient का Near point 25 से है।



normal eye

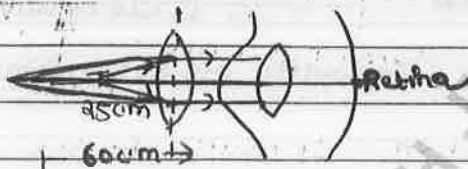


Hypermetropic eyes

इसमें Retina के बाद फोकस होता है।

Q. A far sight person has a near point 80 cm away. what should be the power of lens, he should use for eye glasses, so that he can read a book at distance of 25 cm?

Solve



$$u = -25 \text{ cm}$$

$$v = -80 \text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{-80} - \frac{1}{-25} = \frac{1}{f}$$

$$\frac{-5 - (-12)}{300} = \frac{1}{f}$$

$$\frac{-5 + 12}{300} = \frac{1}{f}$$

$$\frac{300}{7} = f = 300 \text{ cm}$$

$$\frac{1}{\infty} - \frac{1}{400} = \frac{1}{f}$$

$$f = 400$$

$$-4m = \frac{v}{-0.25}$$

200, 40
100, 20
50, 10
25, 5
5, 1

Saathi

Date ___/___/___

Ex. 1
Q89

$$M = \frac{F_o}{F_e} = \frac{100}{2} \quad M = 50$$

$$M = \beta/\alpha$$

$$50 = \frac{\beta}{0.5^\circ} \quad \boxed{\beta = 25^\circ}$$

Q89 $f_o = 400 \text{ cm}$

$$f_e = 4 \text{ cm}$$

$$v = 200 \text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{-200} = \frac{1}{400}$$

$$\frac{1}{v} + \frac{1}{200} = \frac{1}{400}$$

$$v = \frac{1}{\frac{1}{400} - \frac{1}{200}}$$

$$v = \frac{5-1}{200}$$

$$v = \frac{400}{4}$$

$$\boxed{v = 50 \text{ cm}}$$

कुछ नहीं है रश्मि

$$v = \infty$$

$$\frac{1}{\infty} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{\infty} - \frac{1}{u_c} = \frac{1}{4}$$

$$u_c = -4 \text{ cm}$$

$$50 + 4 = 54 \text{ cm}$$

Q84

angular magnification

$$m = \frac{f_o}{f_e} = \frac{15}{1} = 1500 \times$$

Q85

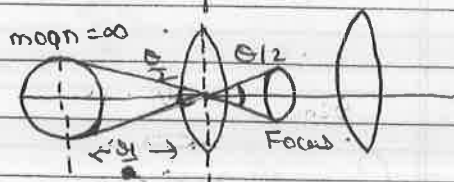
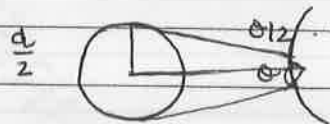
$$v = 3.8 \times 10^8 \text{ m}$$

$$\theta = \frac{d}{r}$$

$$\theta = \frac{d}{2r}$$

$$\theta = \frac{d}{r}$$

$$\theta = \frac{3.48 \times 10^6}{3.8 \times 10^8}$$



$$\frac{d_{\text{object}}}{r} = \frac{d_{\text{image}}}{f_o}$$

$$\frac{3.48 \times 10^6}{3.8 \times 10^8} = \frac{d_{\text{image}}}{1500 \text{ cm}}$$

$$\frac{3.48 \times 10^6 \times 15}{3.8 \times 10^8} = d_{\text{image}}$$

$$9.7 \times 15 \times 10^8 \times 10^{-3}$$

$$1.3 \times 10^5$$

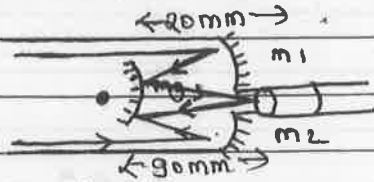
$$13.74 \text{ cm}$$

Date ___/___/___

2 | 70,90
 8 | 45,35
 3 | 9,7
 3 | 3,7
 9 | 1,7

Saathi

Casagrain telescope :-



Large mirror

object $\rightarrow \infty$

Image \rightarrow focus

focus $\frac{e}{f}$

$$f = 110 \text{ cm}$$

Large mirror

$$f = \frac{220}{2} = 110 \text{ mm}$$

Small mirror

$$f = \frac{R}{2} = \frac{140}{2} = 70 \text{ mm}$$

$$u = +90 \text{ cm}$$

$$f = 70 \text{ cm}$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} + \frac{1}{90} = \frac{1}{70}$$

$$\frac{1}{v} = \frac{1}{70} - \frac{1}{90}$$

$$= \frac{90 - 70}{90 \times 70}$$

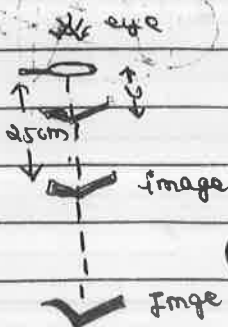
$$= \frac{20}{6300}$$

$$\frac{6300}{20} = 315$$

$$v = 315 \text{ mm}$$

$$v = 31.5 \text{ cm}$$

Q36



$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} + \frac{1}{25} = \frac{1}{5}$$

$$\frac{1}{v} = \frac{1}{5} - \frac{1}{25}$$

$$= \frac{5-1}{25}$$

$$v = \frac{25}{4}$$

$$= 6.25$$

Date ___ / ___ / ___

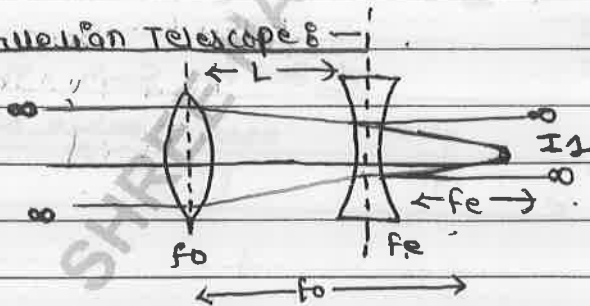
Q6. $\frac{1}{25} + \frac{1}{100} = \frac{1}{f}$
 $f = -200 \text{ cm}$

Q7. $-\frac{1}{75} - \frac{1}{\infty} = \frac{1}{f}$
 $f = -75$
 $P = \frac{100}{-75} = -\frac{4}{3} = -1.33$

Q8. $-\frac{1}{3} + \frac{1}{12} = \frac{1}{f}$
 $\frac{-4+1}{12} = \frac{1}{f}$
 $f = -4 \text{ m}$

Q9. $\frac{1}{-25} + \frac{10}{5} = \frac{1}{f}$
 $-\frac{1}{25} + 2 = \frac{1}{f}$
 $f = 50$
 $P = \frac{100}{50} = 2D$

Galilean Telescope

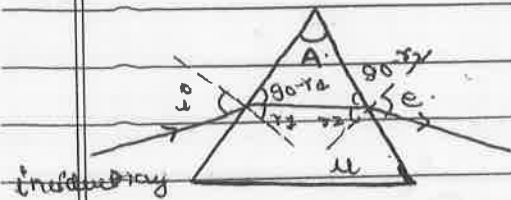


concave
 $u = +f_e$
 $f = -f_e$
 $\frac{1}{v} - \frac{1}{u} = \frac{1}{f_e}$
 $\frac{1}{v} + \frac{1}{f_e} = \frac{1}{f_e}$
 $v = \infty$

length of telescope = $f_o + f_e$ in magnitude

Date ___/___/___

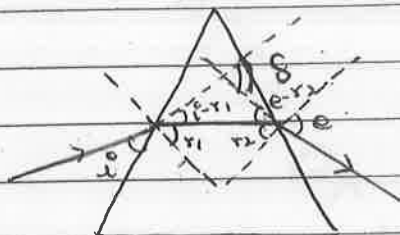
Prism :-



$$A + 90 - i + 90 - r = 180^\circ$$

$$A = r_1 + r_2$$

angle of prism



$$\delta = i + e - A$$

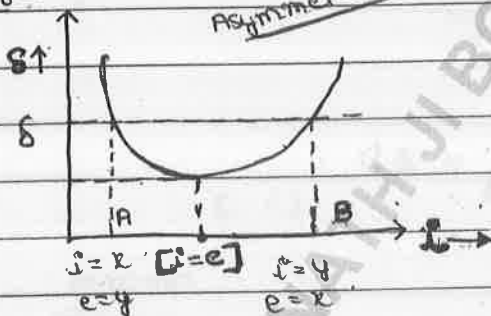
$\delta \rightarrow$ angle of deviation

$i \rightarrow$ incidence angle

$e \rightarrow$ emergence angle

$A \rightarrow$ prism angle

Graph :-



Conclusion \rightarrow

For every value of δ there are two possible values of i .

But for δ_{min} there is only 1 value of i .

Practice curve

at A $\Rightarrow \delta = i + e - A$

$$\delta = x + y - A$$

at B $\Rightarrow i + e - A = \delta$

$$\delta = x + y - A$$

condition for minimum deviation :-

1. $i = e$

deviation (2)

deviation (3)

2. $r_1 = r_2$



since $i = e$

$$r_1 = r_2$$

3. $A = r_1 + r_2$

$$A = r_1 + r_2$$

$$A = 2r$$

$$i \sin i = r \sin r_1$$

$$i \sin i = r \sin r_2$$

since $i = e$

$$A = 2r$$

$$r = A/2$$

$$r_1 = r_2$$

Date ___ / ___ / ___

$\delta = i^e - A$

at δ_{min}

$\delta = 2i - A$

$i = \frac{\delta_{min} + A}{2}$

Snell's law :-

$\mu \sin i = \sin r$

$\sin(\frac{\delta_{min} + A}{2}) = \mu \sin(A/2)$

$\mu = \frac{\sin(A + \frac{\delta_{min}}{2})}{\sin(A/2)}$

Condition of min. deviation

Short notes \rightarrow

a. $i^e = i^i$

b. $r_1 = r_2$

c. $\delta_{min} = 2i - A$

d. $\mu = \frac{\sin(A + \frac{\delta_{min}}{2})}{\sin(A/2)}$

e. $A = 2r$

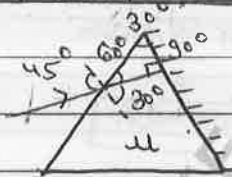
~~NOTE~~ \rightarrow at minimum deviation ray PQ is parallel to Base [condition of min deviation]
Standard points :-

(a) $A = r_1 + r_2$

(b) $\delta = i^e - A$

(c) Snell's law

Popular Example :-



one face silvered

ray \rightarrow retraces its path (at 90°)

Solve $1 \times \sin 45^\circ = \mu \sin 30^\circ$

$\frac{1}{\sqrt{2}} = \mu \times \frac{1}{2}$

$\mu = \sqrt{2}$

3 questions [self practice]

NEET 2016 $i = 45^\circ$ $A = 60^\circ$

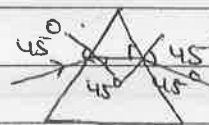
ray \rightarrow suffer minimum deviation

then find $\delta_{min} = ?$ $\mu = ?$

$\delta_{min} = 2i - A$

$= 2 \times 45^\circ - 60^\circ$

$\delta_{min} = 30^\circ$



$A = 2r$
 $A = 2 \times 45^\circ$

$A = 90^\circ$

Date ___/___/___

$$\mu = \sin(90^\circ + 0^\circ)$$

$$\sin 45^\circ = \frac{1}{\sqrt{2}} \mu = \sqrt{2}$$

Saathi

not to be used $\mu \sin 45^\circ = \mu \times 45^\circ$

$$\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}}$$

$$\boxed{\mu = 2}$$

$$\mu = \frac{\sin(60^\circ + 30^\circ)}{\sin 60^\circ} = \frac{\sin 45^\circ}{\sin 30^\circ}$$

$$\mu = \frac{1}{\sqrt{2}} \times \frac{2}{\sqrt{3}} \Rightarrow \boxed{\mu = \sqrt{2}}$$

Q2 angle of prism $m = A$

$$\mu = \cot\left(\frac{A}{2}\right)$$

$$\delta_{min} = ?$$

$$\mu = \frac{\sin(A + \delta_{min})}{2}$$

$$\left(\sin \frac{A}{2}\right)$$

$$\cot \frac{A}{2} = \frac{\sin(A + \delta_{min})}{\sin \frac{A}{2}}$$

$$\frac{\cos \frac{A}{2}}{\sin \frac{A}{2}} = \frac{\sin(A + \delta_{min})}{\sin \frac{A}{2}}$$

$$\sin(90^\circ - \frac{A}{2}) = \sin(A + \delta_{min})$$

$$90^\circ - \frac{A}{2} = \frac{A + \delta_{min}}{2}$$

$$100^\circ - A = \frac{A + \delta_{min}}{2}$$

$$\boxed{\delta_{min} = 100 - 2A}$$

Q3 angle of prism $m = A$

$$\angle i = 2A$$

return back to same path one face is silvered find $\mu = ?$

solve

$$2A \sin A \times \mu \sin 2A = \mu \sin A$$

$$2 \sin A \cos A = \mu \sin A$$

$$\mu = 2 \cos A$$

$$\boxed{\mu = 2 \cos A}$$

Date ___ / ___ / ___

Q4. Prism

$\mu = \sqrt{2}$ $\angle A = 30^\circ$ $\angle i = ?$

One of the refracting surface is made a mirror by silvering. A beam of light entering prism from other face and retrace its path (after reflection from silvered surface).

Solve $\mu \sin i = \sqrt{2} \sin 30^\circ$
 $\sin i = \sqrt{2} \times \frac{1}{2}$
 ~~$\sin i = \frac{1}{\sqrt{2}}$~~ $\sin i = 1/\sqrt{2}$
 $\angle i = 45^\circ$

Q5. For the angle of minimum deviation of prism is equal to angle of prism must be made of material whose $\mu = ?$

- (i) less than 1.
- (ii) greater than 2.
- (iii) lies b/w $\sqrt{2}$ and 1.
- (iv) lies b/w 2 and $\sqrt{2}$.

$S_{min} = 2i - A$
 $A = 2i - A$
 $\angle i = A$

Solve $\mu = \frac{\sin(A + S_{min})}{\sin A/2}$

$\mu = \frac{\sin(A+A)}{\sin A/2} = \frac{\sin A}{\sin(A/2)} = \frac{2 \sin A/2 \times \cos A/2}{\sin A/2}$
 $\mu = 2 \cos(A/2)$

$\angle i$ varies from 0° to 90° ,
 put $\angle i = 0^\circ$ $2 \times \cos(\frac{A}{2}) = 2$
 $\mu = 90^\circ \Rightarrow 2 \times \cos 45^\circ = 2 \times \frac{1}{\sqrt{2}} = \sqrt{2}$

Q6. A ray of light is incident at an angle of incidence i on one face of prism (angle $\rightarrow A$) assume to small angle and emerge normally from opposite face. If μ is ref. index then angle of incidence is nearly equal to?

- (i) A/μ
- (ii) $A/2\mu$
- (iii) μA
- (iv) $\mu A/2$

Date ___ / ___ / ___

Solve



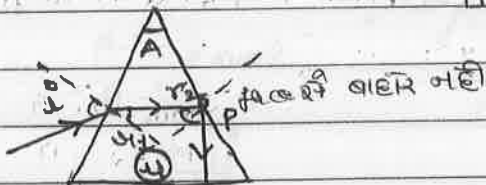
$$\mu \sin i = \mu \sin r_1$$

$$\sin i = \sin r_1$$

$$i = r_1$$

Condition of No Emergence :-

$$A > 2i_c$$



at point P :-

$$(r_2)_{\text{min}} > i_c$$

$$(r_1)_{\text{max}} > i_c$$

$$A = (r_1)_{\text{max}} + (r_2)_{\text{min}}$$

$$r_1 \rightarrow \text{max } i = 90^\circ \quad r_2 = i_c$$

$$A = r_1 + r_2$$

$$A = i_c + r_2$$

$$r_2 = A - i_c$$

condition :-

$$r_2 > i_c$$

$$A - i_c > i_c$$

$$A > i_c + i_c$$

$$A > 2i_c$$

$$\text{APPT} \rightarrow A > 2i_c \quad \text{or } \frac{A}{2} > i_c$$

$$\sin \frac{A}{2} > \sin i_c$$

$$\sin \frac{A}{2} > \frac{1}{\mu}$$

$$\mu > \frac{1}{\sin \frac{A}{2}}$$

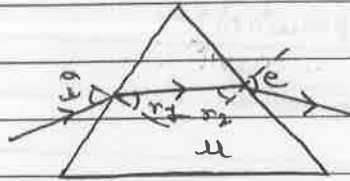
$$\mu > \text{cosec} \frac{A}{2}$$

$$\mu > \text{cosec} \frac{A}{2}$$

$$\theta = A[\mu_v - \mu_r]$$

Date ___ / ___ / ___

Thin Prism :- Its angle of prism is very small



$$i \sin i = \mu \sin r_1$$

$$\sin i \approx i$$

$$\sin r_1 \approx r_1$$

$$i = \mu r_1$$

$$\mu \sin r_2 = 1 \sin e$$

$$e = \mu r_2$$

S Formulae

since $\delta = i + e - A$

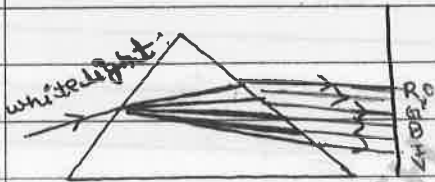
$$\delta = (\mu - 1)A$$

standard $\delta = i + e - A$

min deviation $\delta = 2i - A$

thin prism $\delta = (\mu - 1)A$

Dispersion :- The phenomenon of splitting of white light into its 7 constituent colours is known as dispersion.

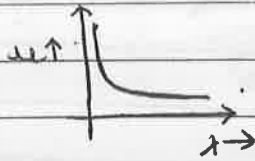


$$\delta = (\mu - 1)A$$

Cauchy's relation :-

$$\mu = A + \frac{B}{\lambda^2} + \dots$$

$$\mu \propto \frac{1}{\lambda}$$



VIBGYOR
 λ increases...
 μ red \rightarrow maximum

angular dispersion :- angle b/w 2 extreme colours

$$\theta = A(\mu_v - \mu_r)$$

$\mu = \frac{c}{v}$ $v \propto \lambda$
 μ red \rightarrow minimum

$$\delta_{\text{mean}} = \frac{\delta_v + \delta_r}{2}$$

$$\delta_{\text{mean}} = (\mu_y - 1)A$$

AA δ is called as dispersion and deviation of white light

Dispersive power :-

$$\omega = \frac{\delta}{\delta_{\text{min}}} = \frac{A(\mu_v - \mu_r)}{(\mu_y - 1)A}$$

mean deviation \rightarrow

$$\delta_{\text{mean}} = (\mu_y - 1)A$$

$$\omega = \frac{\mu_v - \mu_r}{\mu_y - 1}$$

Date ___/___/___

Combination of prisms

1) Deviation without dispersion :-



$\theta_{total} = 0$

$\theta_1 + \theta_2 = 0$

$(\mu_1 \nu_1 - \mu_1 R_1) A_1 + (\mu_2 \nu_2 - \mu_2 R_2) A_2 = 0$

$[\mu_1 \nu_1 - \mu_1 R_1] A_1 = -(\mu_2 \nu_2 - \mu_2 R_2) A_2$

नहीं है don't cross it

2) Dispersion without deviation :-

deviation \rightarrow नहीं है

$\delta_{total} = 0$

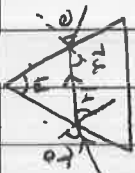
$\delta_1 + \delta_2 = 0$

$\delta_1 = -\delta_2$

$|\delta_1| = |\delta_2|$

$(\mu_1 \nu_1 - 1) A_1 = (\mu_2 \nu_2 - 1) A_2$

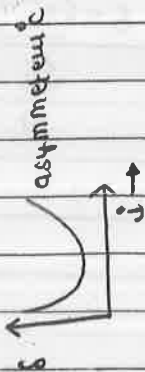
SHORT NOTES ON PRISM



$$A = r_1 + r_2$$

$$\delta = i + e - A$$

Snell's Law



② minimum deviation

$$i = e, r_1 = r_2$$

$$\delta_{min} = 2i - A$$

$$\mu = \frac{\sin(A + \frac{\delta_{min}}{2})}{\sin \frac{A}{2}}$$



* ray parallel to base

③ Dispersion

splitting in 7 colors

Cauchy's relation

$$\frac{\mu - 1}{\lambda^2} = \frac{1}{\lambda^2}$$

angular displacement

$$\theta = (\mu - \mu_R) A$$

mean deviation

$$\delta_{mean} = (\mu - 1) A$$

Dispersive power

$$\omega = \frac{\mu - \mu_R}{\mu - 1}$$

④ Deviation without dispersion

$$\theta = 0$$

$$|\omega| = 10\%$$

⑤ Dispersion without deviation

$$\delta_{net} = 0$$

$$\delta_1 + \delta_2 = 0$$

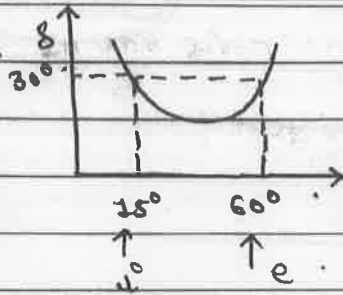
$$(\mu_1 - 1) A_1 = (\mu_2 - 1) A_2$$

- II → Q10, 13, 15, 19, 24, 25, 27, 32, 44, 46
- I → 43-54
- III → Q16
- B. Box → 8
- Date → / /

Solved eg → 21, 22, 33, 34
B. Box → ✓



Q1



find angle of prism?

find angle of prism :-

$$\delta = i + e - A$$

$$30^\circ = 15 + 60 - A$$

$$30^\circ = 75 - A$$

$$A = 45^\circ$$

Date ___/___/___

Q13 without deviation

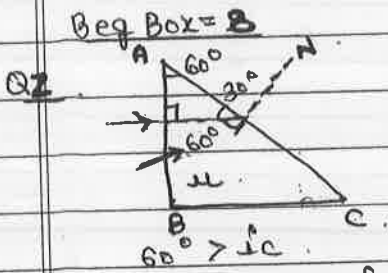
$$\delta_{net} = 0$$

$$\delta_1 = \delta_2$$

$$(\mu_1 - 1) A_1 = (\mu_2 - 1) A_2$$

$$[1.5 - 1] 15^\circ = (1.75 - 1) A_2$$

$$A_2 = 10^\circ$$

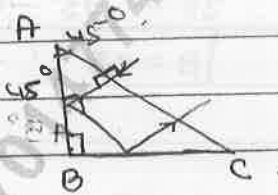


$$\sin 60^\circ > \sin i_c$$

$$\frac{\sqrt{3}}{2} > \frac{1}{\mu}$$

$$\mu > \frac{2}{\sqrt{3}}$$

EX I
Q50



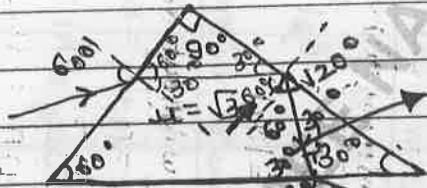
$$45^\circ > i_c$$

$$\frac{1}{\sqrt{2}} > \frac{1}{\mu}$$

$$\mu > \sqrt{2}$$

$$\mu > \sqrt{2}$$

Q3



$$1 \sin 60^\circ = \mu \sin r$$

$$1 \times \frac{\sqrt{3}}{2} = \mu \sin r$$

$$r = 30^\circ$$

Condition for TFR

$$60^\circ > i_c$$

$$\sin 60^\circ > \sin i_c$$

$$\frac{\sqrt{3}}{2} > \frac{1}{\mu}$$

$$\mu > \frac{2}{\sqrt{3}}$$

$$\frac{\sqrt{3}}{2} > \frac{1}{\sqrt{3}}$$

$$30^\circ > i_c$$

$$\frac{1}{2} > \frac{1}{\mu}$$

TFR is

total deviation =

$$38^\circ$$

$$60^\circ$$

$$30^\circ$$

$$\delta = 60^\circ - 30^\circ$$

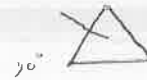
$$\frac{\sqrt{3}}{2}$$

$$\sin i_c = \frac{1}{\mu}$$

$$\sin i_c = \frac{1}{\sqrt{3}}$$

Q 48, 49, 50, 51, 48

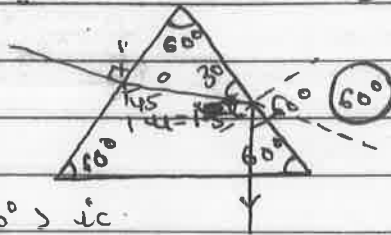
B2 = correction prism angle - x
thin prism - ✓



Saathi

Date ___ / ___ / ___

Q2 In the given situation Draw the emergent ray



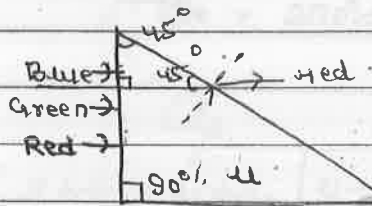
$$\sin 60^\circ > i_c$$

$$\frac{\sqrt{3}}{2} > \frac{1}{2}$$

$$\frac{\sqrt{3}}{2} > \frac{1}{2} \Rightarrow \frac{3}{2} > \frac{1}{2}$$

TIR ✓

Ex II Q27 →



$$\sin 45^\circ > i_c$$

$$\frac{1}{\sqrt{2}} > \frac{1}{2}$$

$$2 > \sqrt{2}$$

Mirror :-

Spherical mirror :-

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

mirror → mirror

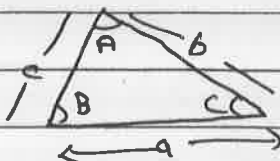
$$\frac{H_1}{H_0} = \frac{\theta}{u}$$

$$P = -\frac{1}{f}$$

$$f = R/2$$

Paraxial rays

Cartesian theorem :-



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$



$$\frac{\sin(\pi - 2\alpha)}{R} = \frac{\sin \alpha}{CF}$$

$$\frac{\sin 2\alpha}{R} = \frac{\sin \alpha}{CF}$$

$$2 \sin \alpha \cos \alpha = \frac{\sin \alpha}{CF}$$

$$CF = \frac{R}{\cos \alpha}$$

$$PF = R - CF$$

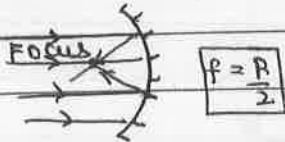
$$\text{Learn } PF = R - \frac{R}{\cos \alpha}$$

Date ___ / ___ / ___

Parallel rays $\theta \leq 5^\circ$

Hence $f = R/2$

Paraxial rays $\theta \leq 5^\circ$



Focal length is same for all colour

mirror Chromatic aberrations \rightarrow of

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

magnification

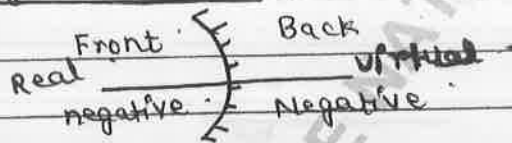
$$m_T = \frac{HI}{H_o} = \frac{-v}{u}$$

transverse

longitudinal

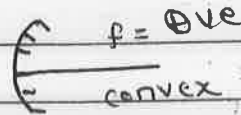
$$m_L = \frac{\text{length of image}}{\text{length of object}}$$

Sign convention

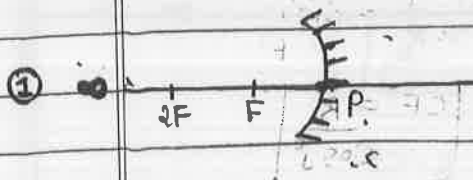


object, mention of (Real object)

Real object of Real image & that inverted of A



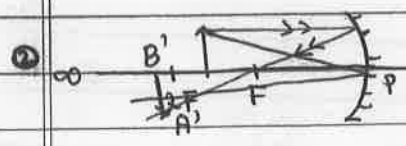
Ray Tracing



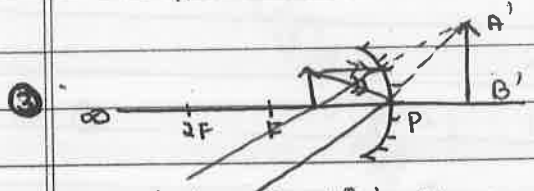
Date ___ / ___ / ___



Case I
Image
Real image
Inverted
Diminished
F and 2F के बीच



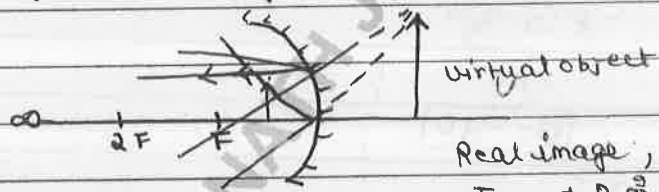
Real Image
Inverted
Enlarged
2F اور C के बीच



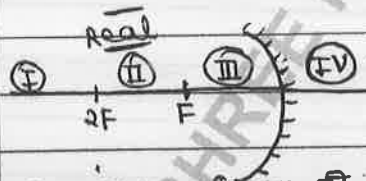
Virtual
Erect
Enlarged
used by Dentist, shaving mirror behind F and P

Q. what about virtual object

ROD → Real object diverging incident
virtual object - अनि
Incident ray → converging



Real image, Erect, diminished
F and P के बीच



Concave mirror में VO/VI possible.

Object	Image
I RO	II RI
II RO	I RI
III RO	IV VOI
IV VO	III ROI

Q1. A man has shaving mirror of focal length 20cm. How far should the mirror be held from his face in order to give an image two fold magnification?

Soln
 $M = -2$
 $M = \frac{H_i}{H_o} = -\frac{v}{u}$
 $2 = \frac{v}{u}$
 $v = 2u$

$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$
 $\frac{1}{2u} + \frac{1}{u} = \frac{1}{20}$
 $\frac{-1+2}{2u} = \frac{1}{20}$
 $\frac{1}{2u} = \frac{1}{20}$
 $u = 10 \text{ cm}$

Date ___/___/___

Q2 The focal length of concave mirror 30cm where should an object is placed so that its image is 3 times magnified real and inverted?

Given $f = -20\text{cm}$

$H_I = +3H_O$

$U = ?$

$\frac{H_I}{H_O} = \frac{-U}{V}$

$\frac{3H_O}{H_O} = \frac{-U}{V}$

$+3U = -V \quad V = -3U$

$\frac{1}{V} + \frac{1}{U} = \frac{1}{f}$

$\frac{1}{-3U} + \frac{1}{U} = \frac{1}{-30}$

$\frac{4}{3U} = -\frac{1}{30}$

$\frac{4}{3 \times 4} = -\frac{1}{30}$

$V = -40$

$V = 3 \times -40$
 $V = -120\text{cm}$

Convex Mirror



Real object of CONVEX mirror virtual image, erect diminished.

object

image

used in vehicle side mirror

convex mirror

I VO

II VI

II VO

I VI

III VO

IV RI

IV RO

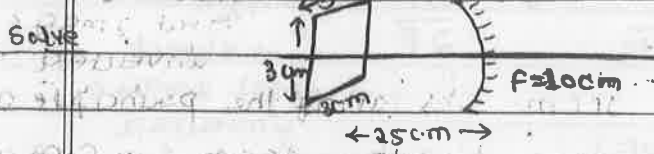
III VI

convex mirror में real की real image not possible

H.W. → Ex → Q10, 11, 12, 14, 15, 16, 18, 19, 20, 21, 23, 24
 Reg II → Q1, 2, 3, 4, 5, 6
 Date → Q1, Q2, Q3



Q. A square of side 3cm is placed at a distance of 25cm from a concave mirror of focal length 10cm. The center of the square is at a axis of mirror and the plane is normal to the axis. Calculate the area of enclosed by image of wire?



Solve
 $U = -25\text{cm}$

$f = -10\text{cm}$

$\frac{1}{v} + \frac{1}{u} = -\frac{1}{f}$

$\frac{1}{v} - \frac{1}{25} = -\frac{1}{10}$

$\frac{1}{v} = -\frac{1}{10} + \frac{1}{25}$

$\frac{1}{v} = \frac{-5+2}{50}$

$v = -\frac{50\text{cm}}{3}$

$\frac{H_I}{H_O} = -\frac{v}{u}$
 $= -\left(\frac{-50}{25}\right)$
 $= \frac{2}{1}$

$\frac{H_I}{3} = \frac{2}{1}$
 $H_I = 6\text{cm}$

$H_I = -2\text{cm}$

Area = $(2\text{cm})^2 = 4\text{cm}^2$

NOTE →

1. Object ∞ and $2F$ के बीच में
 Image → छोटी

2. Object placed b/w $2F$ and F .
 Image → Enlarged

3. Object $2F$.
 Image → $2F$ [same size]

Conclusion → Image size increased from ∞ to $2F$.

Q1. A thin rod of length $f/3$ is placed along the principle axis of a concave mirror of focal length f such that its image is real elongated just touches one end of the rod. then calculate the long magnification?

Solve A → $2F$

B → $2F - f/3 = 5f/3$

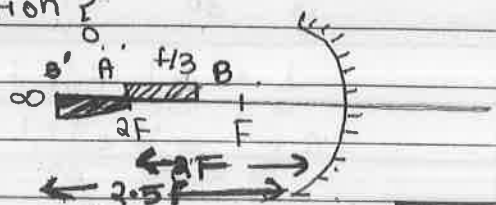
$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

$\frac{1}{v} + \frac{1}{5f/3} = \frac{1}{f}$

$\frac{1}{v} = \frac{1}{f} - \frac{3}{5f}$

$v = \frac{5f}{2}$

$v = 2.5f$



Ex III 2, 3, 4, 5, 6, 7, 9, 10, 11, 12

Saathi

Date ___/___/___

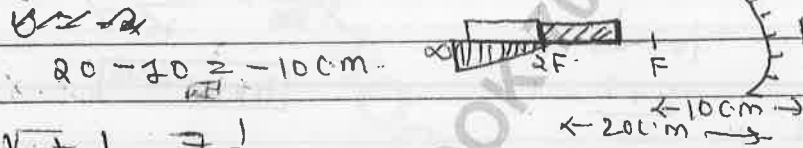
Image of rod = $2.5f - 2f$
 $= 1/2 f$

long magnification = $\frac{1f}{f/3} = \frac{3f}{2f} = 1.5$

↓
 real object
 real image
 inverted

Q2
 AIPM = 2012
 A rod of length 10cm lies along the principle axis of a concave mirror of focal length = 10cm in such a way that its end closer to the pole is 20cm away from the mirror then calculate the length of the image?

Solve



$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$

$\frac{1}{20} + \frac{1}{v} = \frac{1}{10}$

$\frac{1}{v} = \frac{1}{10} - \frac{1}{20}$

$\frac{1}{v} = \frac{2-1}{20}$

$v = 20 \text{ cm}$

$u = -20 \text{ cm}$

$f = -10 \text{ cm}$

$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$

$\frac{1}{v} - \frac{1}{20} = -\frac{1}{10}$

$v = \frac{-1}{\frac{1}{10} - \frac{1}{20}}$

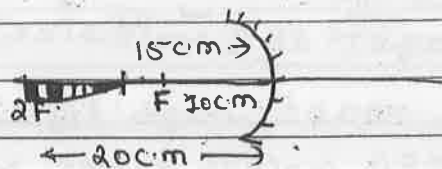
$v = \frac{-2+1}{20}$

$v = -20 \text{ cm}$

B की पर्याय :-

$u = -20 \text{ cm}$

$f = -10 \text{ cm}$



$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$

$\frac{1}{15} + \frac{1}{v} = \frac{1}{10}$

$\frac{1}{v} = \frac{1}{10} - \frac{1}{15}$

$\frac{1}{v} = \frac{3-2}{30}$

$v = 30 \text{ cm}$

length of image = 5cm

$v = -15 \text{ cm}$

Date ___/___/___

velocity concept :-

x-axis :- along principle axis

Power $\frac{dI}{dt} = -m^2 \frac{dO}{dt}$

y-axis :- perpendicular to principle axis

Question asked $\frac{dI}{dt} = m^2 \frac{dO}{dt}$

$m \rightarrow$ magnification

$$m = \frac{H_I}{H_O} = -\frac{v}{u}$$

व्यक्ति $m = \frac{f}{f-u}$

Q17 A point object is moving on the principle axis of a concave mirror of focal length 24cm. towards the mirror. when it is at a distance of 60cm from the mirror its velocity is 9cm/sec. then calculate the velocity of image at that instant?

$$f = -24\text{cm}$$

$$u = -60\text{cm}$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{60} = -\frac{1}{24}$$

$$\frac{1}{v} = -\frac{1}{24} + \frac{1}{60}$$

$$\frac{1}{v} = \frac{-5+2}{120}$$

$$v = \frac{120}{-3} \quad \boxed{v = -40\text{cm}}$$

$$m = -\frac{v}{u}$$

$$= -\frac{(-40)}{60}$$

$$= \frac{4}{3} = 1.33 \quad \text{SD}$$

$$m = \frac{f}{f-u} = \frac{-24}{-24}$$

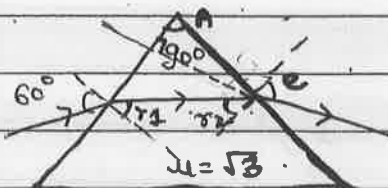
$$\frac{dI}{dt} = -\left(\frac{2}{3}\right)^2 [u_0 - u_m]$$

$$v_I - u_m = -\frac{4}{9} [9\hat{i} - 0]$$

$$v_I - 0 = -\frac{4}{9} \times 9\hat{i}$$

$$\boxed{v_I = -4\hat{i}}$$

Q14



Double refraction?

$$\mu \sin 60^\circ = \sqrt{3} \sin r_1$$

$$\frac{\sqrt{3}}{2} = \sqrt{3} \sin r_1$$

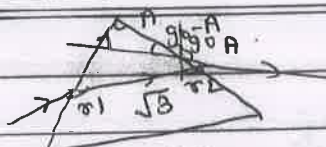
$$\boxed{r_1 = 30^\circ}$$

Q13 → length — x Height ✓

Ex 1
~~Q13~~ object 2F 4x 299018 di image 2F 4x ही 40001 ।

saathi

Date: / /



$$A = r_1 + r_2$$

$$A = 30^\circ + r_2$$

$$r_2 = A - 30^\circ$$

$$\sqrt{3} \sin r_2 = 1 \sin A$$

$$\sqrt{3} \sin(A - 30^\circ) = 1 \times \sin A$$

$$\sqrt{3} [\sin A \cos 30^\circ - \cos A \sin 30^\circ] = \sin A$$

$$\sqrt{3} \left[\sin A \times \frac{\sqrt{3}}{2} - \cos A \times \frac{1}{2} \right] = \sin A$$

$$\frac{\sqrt{3}}{2} [\sqrt{3} \sin A - \cos A] = \sin A$$

$$3 \sin A - \sqrt{3} \cos A = 2 \sin A$$

$$3 \sin A - 2 \sin A = \sqrt{3} \cos A$$

$$\frac{\sin A}{\cos A} = \sqrt{3}$$

$$\tan A = \sqrt{3} \Rightarrow A = 60^\circ$$

Q3. APMS

focal length = +f

$$H_I = \frac{+1}{n} H_O$$

$$\frac{H_I}{H_O} = \frac{-v}{u}$$

$$\frac{+1}{n} = \frac{-v}{u}$$

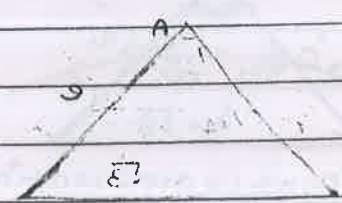
$$\frac{-1}{n} + \frac{1}{u} = \frac{-1}{f}$$

$$-\frac{n}{u} + \frac{1}{u} = \frac{1}{f}$$

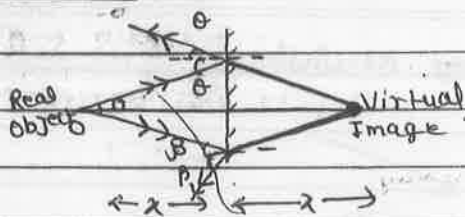
$$-\frac{n-1}{u} = \frac{1}{f}$$

$$u = -(n-1)f$$

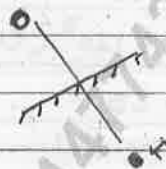
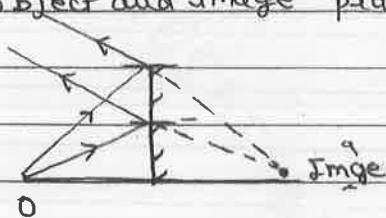
$$u = -(n-1)f$$



Plane Mirror



Line joining object and image is always \perp to mirror.
 Object and image plane mirror are opp. side



Plane mirror
 3rd yr

Real object \rightarrow V.I.

V. object \rightarrow R. image

Incident - converging \rightarrow virtual object

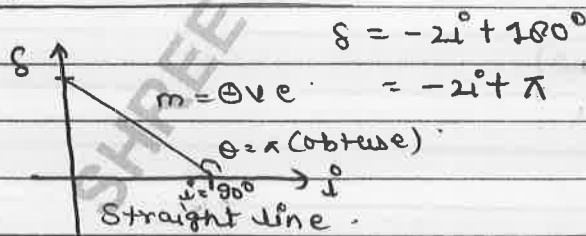


Angle of Deviation (δ) :-



$\delta = 180 - 2i$

graph b/w δ and i



if $i = 90^\circ$ then $\delta = 0^\circ$

if $i = 90^\circ$

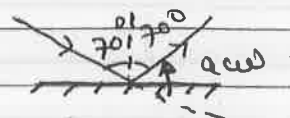
$\delta = 180 - (90 \times 2)$

$\delta = 0^\circ$

δ c.w $\approx 2i$ a.c.w = ? let see how to check?



$\delta = 180 - 2(30)$
 $\delta = 120^\circ$

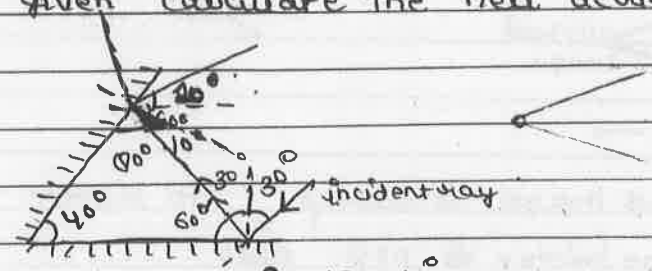


$\delta = 180 - 2(70)$

$\delta = 40^\circ$

Date ___/___/___

Q1 In given calculate the nett deviation?



$$\delta = 100 - 40$$

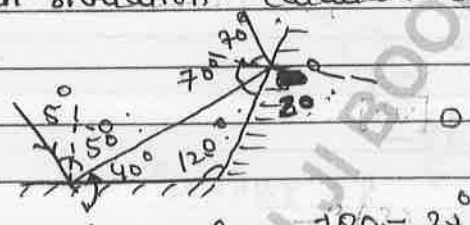
$$\delta = 120^\circ \text{ (CCW)}$$

$$\delta = 180 - 20$$

$$\delta = 160^\circ \text{ (CCW)}$$

$$\delta_{\text{nett}} = 160 + 120 = 280^\circ \text{ CW}$$

Q2 In the given situation calculate the $\delta_{\text{nett}} = ?$



$$\delta_1 = 100 - 20$$

$$\delta_1 = 80^\circ \text{ [CCW]}$$

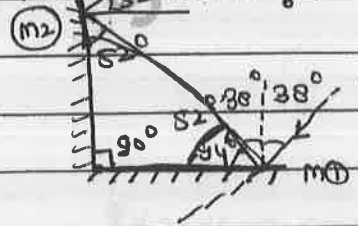
$$\delta_2 = 180 - 20$$

$$= 160 - 140$$

$$= 40^\circ \text{ (CCW)}$$

$$\delta_{\text{nett}} = 120^\circ$$

Q3 calculate the $\delta_{\text{nett}} = ?$



16	16
130	190
20	176
76	94
	76
	8

$$\delta_1 = 100 - 76$$

$$= 70^\circ \text{ CCW}$$

$$\delta_2 = 180 - 2 \times 52$$

$$= 76$$

$$\delta_{\text{nett}} = 100 = 70 + 76$$

$$= 100^\circ$$

H.W → Ex II → Q1 - Q27
 Ex III → Q1 - Q8

Saathi

Date ___ / ___ / ___

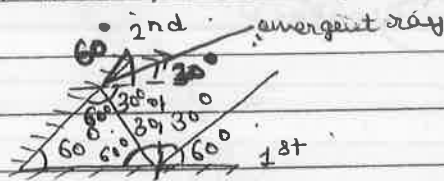
SHORT TRICK ⇒ $\theta_{\text{net}} = 360 - 2\theta$

θ → angle b/w mirror → 2θ

★ If 2 mirrors are perpendicular to each other then incident ray and emergent ray are antiparallel to each other.

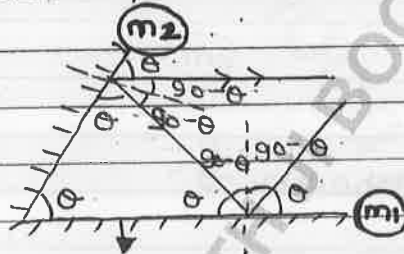
Q4 Two plane mirror are inclined to each other at an angle 60° . If ray of light incident on first mirror is parallel to second mirror, it is reflected from 2nd mirror.

Solve
 Conceptual Question



emergent ray and 1st mirror are parallel

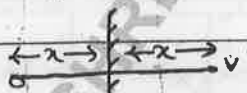
★ Concept get from previous question



In this Δ $3\theta = 180^\circ$

$\theta = 60^\circ$

velocity concept in plane mirror :-



y-axis :- $\vec{v}_I = \vec{v}_O$

z-axis :- $\vec{v}_I = \vec{v}_O$

y-z plane

$\frac{dx_O}{dt} = -\frac{dx_I}{dt}$

$\frac{d}{dt} \vec{x}_O = -\frac{d}{dt} \vec{x}_I$

$\vec{v}_O = -\vec{v}_I$

$\vec{v}_O - \vec{v}_m = -[\vec{v}_I - \vec{v}_m]$

$\vec{v}_O - \vec{v}_m = -\vec{v}_I + \vec{v}_m$

$\vec{v}_I = 2\vec{v}_m - \vec{v}_O$

mirror

spherical

$v_I/m = -m^2 v_O/m$

$m = 1$

$\vec{v}_I/m = -\vec{v}_O/m$

If mirror is z-plane

$\vec{v}_I = 2\vec{v}_m - \vec{v}_O$ y-axis

Mirror $y-z = x/y/z = z$ formula.

$x-y = x/y/z = z$ formula.

$y-z = x/y/z = z$ formula.

Date $z-k = x/y/z = y$ formula.

Saathi

Q. Plane mirror is moving with velocity $4\hat{i} + 5\hat{j} + 6\hat{k}$. A point object in front of mirror moves with velocity $3\hat{i} + 4\hat{j} + 5\hat{k}$. The mirror is placed in $y-z$ plane then calculate the velocity of image?

$$v_{\vec{i}} = 2v_{\vec{m}} - v_{\vec{o}} \rightarrow \text{along } (x)$$

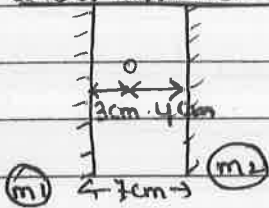
x comp + y comp + z comp
Formula y/z part object velocity

$$\begin{aligned} v_{\vec{i}} &= 2(4\hat{i}) - (3\hat{i}) \\ &= 8\hat{i} - 3\hat{i} \\ &= 5\hat{i} \end{aligned}$$

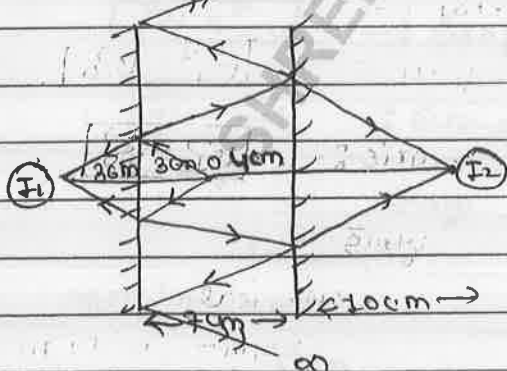
$$v_{\vec{i}} = 5\hat{i} + 4\hat{j} + 5\hat{k}$$

Multiple reflection :-

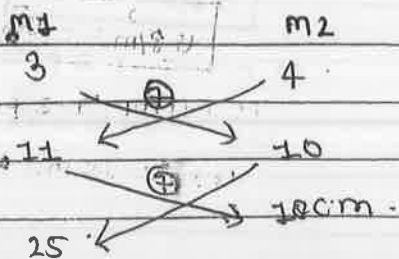
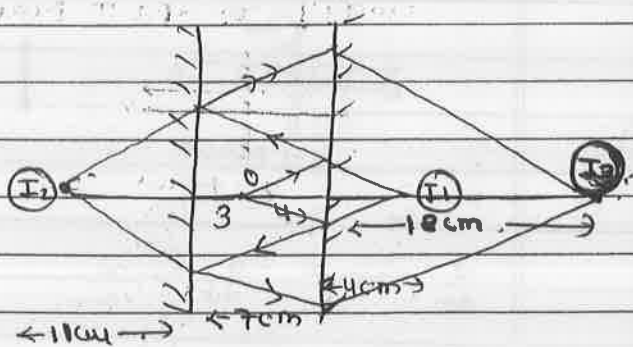
(i) when mirrors are parallel to each other \rightarrow



हिना पला मूलेक्शन म२ स० :-

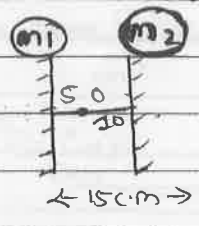
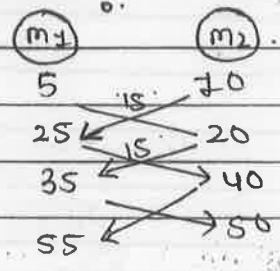


हिना पला मूलेक्शन म१ स० :-



Date ___ / ___ / ___

Q. In given situation calculate the distance of first 3 image from mirror m_2 ?



Case (ii) when mirrors are inclined to each other:-

(i) first find $\frac{360}{\theta}$

Even

odd

no. of image = $\frac{360}{\theta} - 1$

Object \rightarrow Symm. (angle bisector)

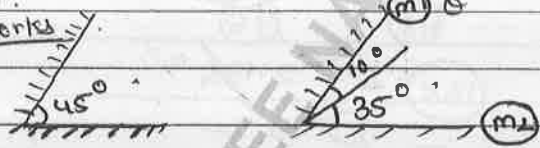
Obj \rightarrow asymmetric

no. of image = $\frac{360}{\theta} - 1$

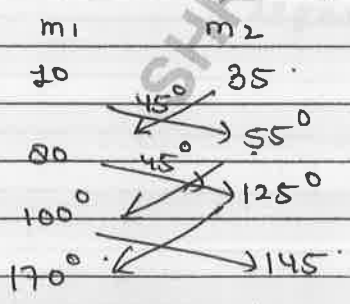
no. of image

$\frac{360}{\theta}$

method :- always works



4th image overlapp krati



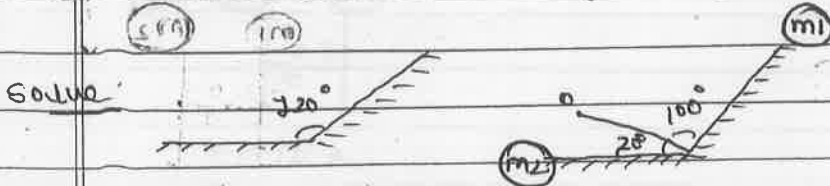
Ques \rightarrow Q1, Q4, Q6, Q7, Q8

Ans \rightarrow Q1, Q2, Q3, Q4, Q5, Q6, Q9

Saathi

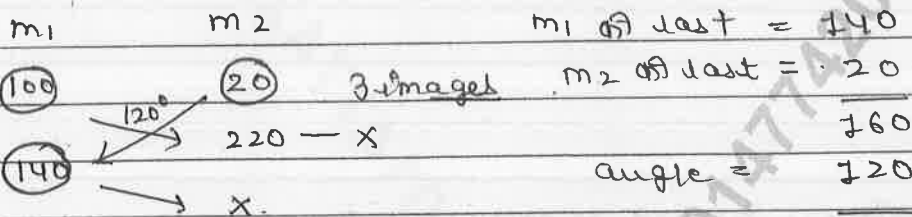
Date ___/___/___

Q1 Calculate the no. of images in given situation?



Solve

$$\frac{360}{120} = 3 \text{ images}$$



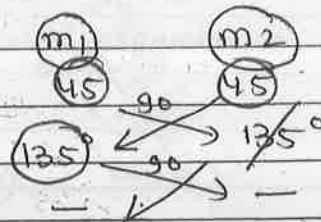
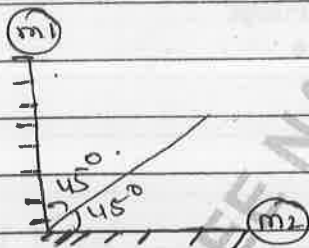
\therefore no overlapping $\rightarrow 280$

Q2 Two mirrors are perpendicular to each other and there is a lamp in b/w the mirror then calculate the no. of images of lamp? [learnas result]

Solve

$$\frac{360}{90} = 4$$

$$4 - 1 = 3 \text{ images}$$



3 images

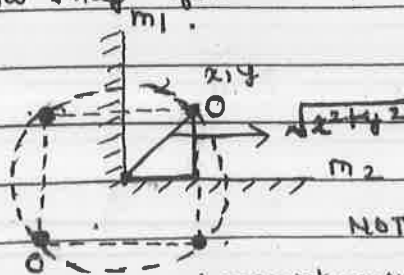
Overlapping = ?

$$m_1 \text{ off last} = 135$$

$$m_2 \text{ off last} = 135$$

$$\text{mirror} = \frac{90}{360}$$

How image formed \rightarrow



all image lie in a circle

center \rightarrow vertex

point of intersecting of mirror

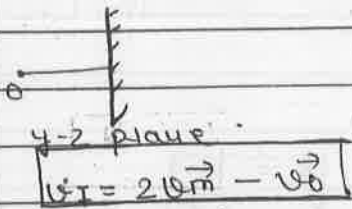
NOTE \rightarrow A person is in a room whose ceiling

and 2 adjacent walls are mirror then total 7 images are formed.

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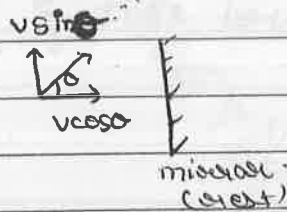
velocity concept^o - Applications -

* If nothing given then consider the always consider in x-y-z plane



y-axis $u_i = u_o$
z-axis $v_i = v_o$

eg
[III]



ans

$$u_i = -v \cos \theta \hat{i} + v \sin \theta \hat{j}$$

x-axis

$$u_i = 2(0) - (v \cos \theta \hat{i})$$

$$u_i = -v \cos \theta \hat{i}$$

y-axis $u_i = v \cos \theta \hat{j} + v \sin \theta \hat{j}$

Sometimes ask \rightarrow

$$u_{i/o} = u_i - u_o$$

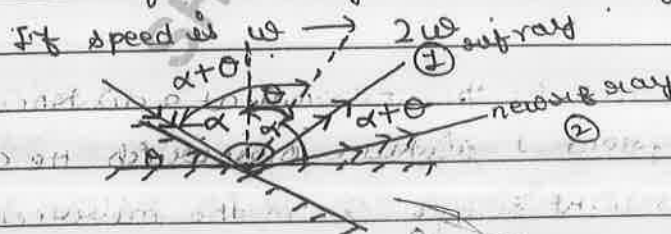
$$= -v \cos \theta \hat{i} + v \sin \theta \hat{j} - [v \cos \theta \hat{i} + v \sin \theta \hat{j}]$$

$$u_{i/o} = -2v \cos \theta \hat{i}$$

NOTE \rightarrow If mirror is rotated by an angle θ keeping incident ray fixed

then reflected ray is rotated by an angle 2θ [same direction]

* If speed is u



reference



Q1 A Beam of light from a source is incident normally on a plane mirror fixed at a certain distance x from a source. When a mirror is rotated through a small angle θ the spot of a light is found to move through a distance y . then calculate the angle θ ?

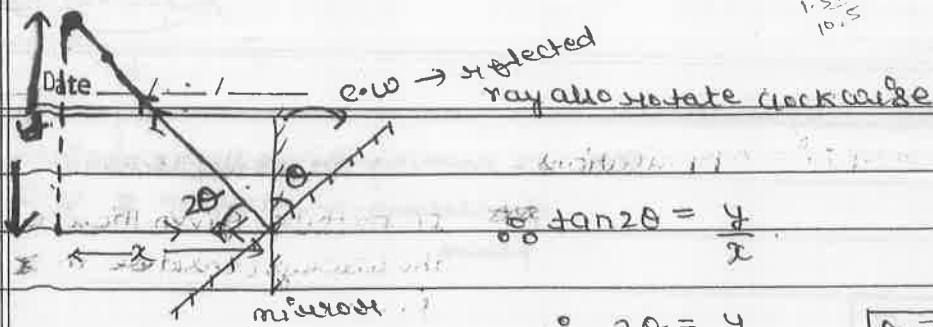
① y/x

② x/y

③ x/y

④ $y/2x$

(saathi)

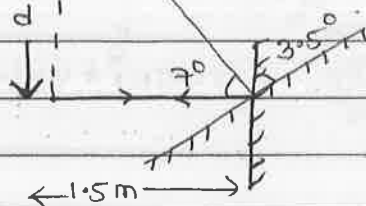


$$\tan 2\theta = \frac{d}{x}$$

$$\tan 2\theta = \frac{d}{x}$$

$$\theta = \frac{d}{2x}$$

Q2 In the given situation mirror is rotated by 3.5° then calculate the displacement of reflected spot?



$$\tan 7^\circ = \frac{d}{1.5}$$

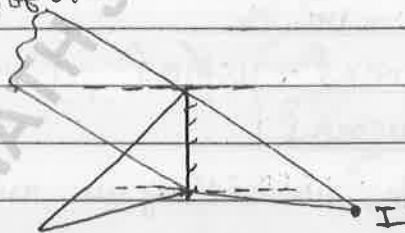
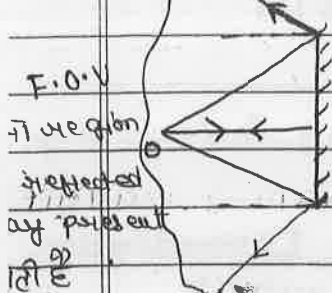
$$\tan \theta = \frac{7 \times 7}{100}$$

$$\tan 7^\circ \rightarrow x \cdot 7^\circ$$

Convert into radian must: $\frac{7 \times 7}{100} = \frac{d}{1.5}$

$$d = \frac{10.5 \times 7}{100}$$

Field of view :- field of view

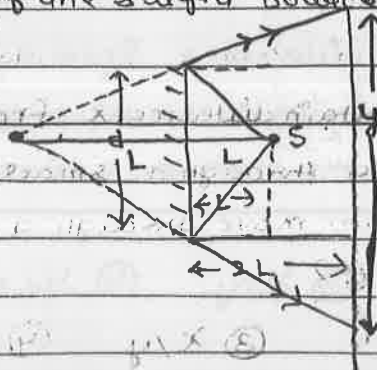


cannot see see image

Q3 A man walks in front of the mirror at a distance $2d$ as shown. The greatest distance over which he can see the image of the light source S in the mirror?

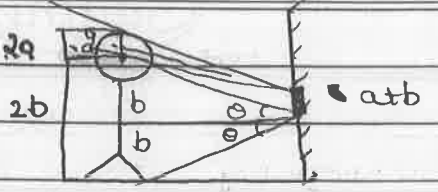
$$\frac{d}{x} = \frac{4}{3d}$$

$$4 = 3d$$



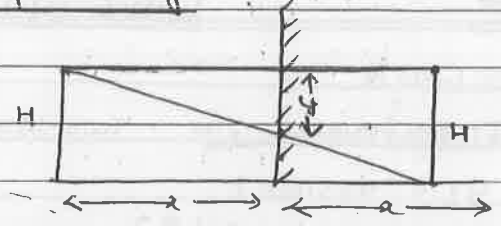
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Ex. 29



$H = 2a + 2b$

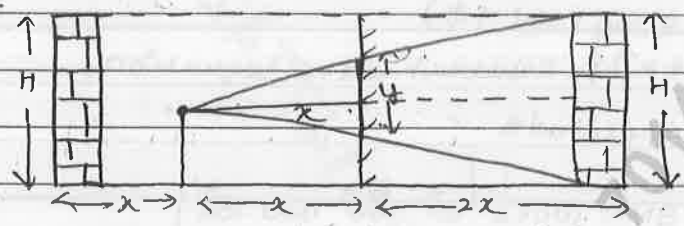
Simplest way



$\frac{y}{x} = \frac{H}{2x}$

$y = H/2$

Q2



$\frac{y}{x} = \frac{H}{3x}$

$y = H/3$

SHREE NATHJI BOOK

Date ___/___/___ WAVE OPTICS

Section-A

Interference :- Two waves

$$y_1 = a_1 \sin \omega t \quad \omega \rightarrow \text{frequency}$$

$$y_2 = a_2 \sin(\omega t + \phi) \quad a \rightarrow \text{amplitude}$$

Principle of superposition

$$y_{\text{net}} = y_1 + y_2$$

$$y_{\text{net}} = a_1 \sin \omega t + a_2 \sin(\omega t + \phi)$$

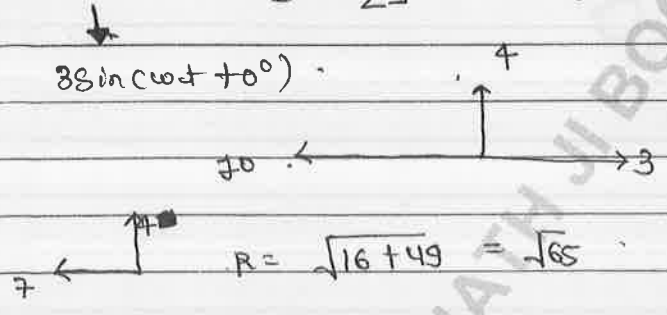
$$y_{\text{net}} = R \sin[\omega t + \alpha] \quad \text{Resultant wave equation}$$

↓
resultant amplitude

Phase → add

अनुक्रमित SHM wave को जोड़ें add करें।

$$3 \sin \omega t + 4 \sin[\omega t + \frac{\pi}{2}] + 10 \sin[\omega t + \pi]$$



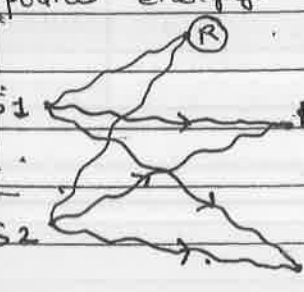
$$R = \sqrt{a_1^2 + a_2^2 + 2a_1a_2 \cos \phi} \rightarrow \text{phase diff}$$

$$\tan \alpha = \frac{a_2 \sin \phi}{a_1 + a_2 \cos \phi}$$

angle made from a_1

Interference is a phenomenon in which redistribution of energy takes place at some points energy become maximum [Cons. Int.] and at some points energy becomes minimum [Destruct. Int.]

- Phase diff must be constant
- Frequency same
- Sustained Interference condition



Interference position dependent -
P Energy maximum
Q Energy minimum

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Constructive

$n = 0, 1, 2, 3$

Phase diff = $0, 2\pi, 4\pi, 2n\pi$

$R = \sqrt{a_1^2 + a_2^2 + 2a_1a_2 \cos \theta}$

$\cos 0 = 1$

$\cos 2\pi = 1$

$R = a_1 + a_2$

Bright Fringes

Destructive

$n = 0, 1, 2, 3$

Phase diff = $\pi, 3\pi, 5\pi \dots (2n+1)\pi$

$\cos \pi = -1$

$\cos 3\pi = -1$

$R = a_1 - a_2$

Dark Fringes

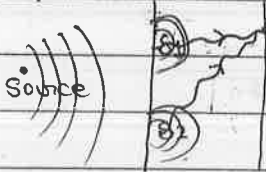
Two independent source can never be coherent

Independent source always incoherent

Methods to produce coherent source \rightarrow

Method I

By division of wavefront



YDSE

Intensity Concept \rightarrow

Intensity \propto [amplitude]²

$I = k(\text{amp})^2$

$I_1 = k(a_1)^2$

$I_2 = k(a_2)^2$

$I = k(R)^2$

we know that

$R = \sqrt{R_1^2 + R_2^2 + 2R_1R_2 \cos \phi}$

Squaring

$R^2 = R_1^2 + R_2^2 + 2R_1R_2 \cos \phi$

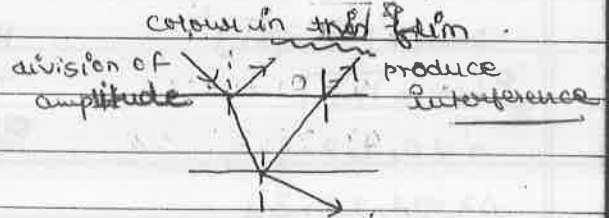
$R^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$

$\frac{I}{k} = \frac{I_1}{k} + \frac{I_2}{k} + 2\sqrt{\frac{I_1}{k}}\sqrt{\frac{I_2}{k}} \cos \phi$

$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$

Method II

By division of amplitude



Constructive Interference

$\cos 0, 2\pi = 1$

$I_{\text{max}} = (\sqrt{I_1} + \sqrt{I_2})^2$

Destructive Interference \rightarrow

$I_{\text{min}} = (\sqrt{I_1} - \sqrt{I_2})^2$

Concept: $\Delta x \rightarrow$ path diff
 $\Delta \phi =$ Phase difference

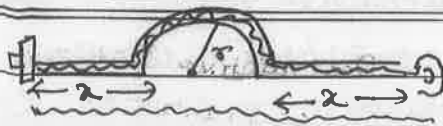
Relation \rightarrow

$\Delta \phi = \frac{2\pi}{\lambda} \cdot \Delta x$

$\Delta x \rightarrow$ Path difference

(saathi)

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Path ① = $2x + 2t$

Path ② = $x + 2t + \pi r$

$$\Delta x = [2\mu t + 2x] - [2x + 2t]$$

$$= 2\mu t - 2t$$

$$= 2(\mu - 1)t$$

Show notes :-

Constructive \neq Destructive

$\Delta \phi = 0, 2\pi, 4\pi \dots 2n\pi$

$\Delta \phi = \pi, 3\pi, 5\pi \dots (2n+1)\pi$

$R_{max} = a_1 + a_2$

$n = 0, 1, 2 \dots$

$I_{max} = (\sqrt{I_1} + \sqrt{I_2})^2$

$R_{min} = a_1 - a_2$

$\Delta x = n\lambda$

$I_{min} = (\sqrt{I_1} - \sqrt{I_2})^2$

$n = 0, 1, 2 \dots$

$\Delta x = (2n+1)\frac{\lambda}{2}$

$\Delta x = 0, \lambda, 2\lambda, 3\lambda$

$n = 0, 1, 2 \dots$

$\Delta x = \frac{\lambda}{2}, \frac{3\lambda}{2}, \frac{5\lambda}{2}$

$\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2}$

$R = \sqrt{a_1^2 + a_2^2 + 2a_1a_2 \cos \phi}$

$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$

$\cos 120^\circ = -\frac{1}{2}$

$\cos 150^\circ = \frac{\sqrt{3}}{2}$

Practice \rightarrow 5 Questions

NEET-2016 $\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2}$

Calculate the value of $I_{max} - I_{min} = ?$

$\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2}$

$I_{max} = (\sqrt{I_1} + \sqrt{I_2})^2$ $I_{min} = (\sqrt{I_1} - \sqrt{I_2})^2$

$= I_1 + I_2 + 2\sqrt{I_1 I_2}$ $= I_1 + I_2 - 2\sqrt{I_1 I_2}$

Phenomenon of interference is shown by all types of waves, eg → electro, Transverse, light, sound etc.

Saathi

$$\frac{n+1+2\sqrt{n} - (n+1-2\sqrt{n})}{n+1+2\sqrt{n} + (n+1-2\sqrt{n})}$$

$$= \frac{\cancel{n+1} + 2\sqrt{n} - \cancel{n+1} + 2\sqrt{n}}{n+1+2\sqrt{n} + n+1-2\sqrt{n}}$$

$$= \frac{2 \times 2\sqrt{n}}{2(n+1)}$$

$$= \frac{2\sqrt{n}}{n+1}$$

Q2. Intensity of two waves are I_1 and I_2 resp. find out the resultant intensity if the phase diff b/w them is π ?
A.I.M.S - 2016

Solve

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

$$I = 9 + 1 + 2\sqrt{9 \times 1} \cos 180^\circ$$

$$I = 10 - 6$$

$$I = 4$$

कौनसी काह नी बात :-

$$\frac{a_1}{a_2} = \frac{3}{1} \therefore \frac{I_1}{I_2} = \frac{9}{1}$$

Q3 If the ratio of amplitude of 2 source is $3:5$ then calculate the ratio of $\frac{I_{max}}{I_{min}}$.

Solve

$$\frac{a_1}{a_2} = \frac{3}{5} \Rightarrow \frac{I_1}{I_2} = \frac{9}{25}$$

$$\frac{I_{max}}{I_{min}} = \frac{(\sqrt{I_1} + \sqrt{I_2})^2}{(\sqrt{I_1} - \sqrt{I_2})^2} = \frac{[\sqrt{9} + \sqrt{25}]^2}{[\sqrt{9} - \sqrt{25}]^2} = \frac{9 + 25 + 2 \times 3 \times 5}{9 + 25 - 2 \times 3 \times 5}$$

$$= \frac{9 + 25 + 30}{9 + 25 - 30}$$

Q4 If the intensity ratio of 2 waves is $9:1$ then calculate the ratio of $\frac{A_{max}}{A_{min}}$.

$$\frac{I_1}{I_2} = \frac{9}{1} = \frac{a_1^2}{a_2^2} = \frac{9}{1} \therefore \frac{a_1}{a_2} = \frac{3}{1}$$

$$\frac{R_{max}}{R_{min}} = \frac{4}{2}$$

Saathi

Date / /

Q5 If interference have max and min in 36:1 ratio then calculate the ratio of amplitude?

Solve $\frac{I_{\max}}{I_{\min}} = \frac{36}{1}$

$$\frac{(\sqrt{I_1} + \sqrt{I_2})^2}{(\sqrt{I_1} - \sqrt{I_2})^2} = \frac{36}{1}$$

$$\frac{\sqrt{I_1} + \sqrt{I_2}}{\sqrt{I_1} - \sqrt{I_2}} = \frac{6}{1}$$

$$\sqrt{I_1} + \sqrt{I_2} = 6\sqrt{I_1} - 6\sqrt{I_2}$$

$$7\sqrt{I_2} = 5\sqrt{I_1}$$

$$\frac{\sqrt{I_1}}{\sqrt{I_2}} = \frac{7}{5}$$

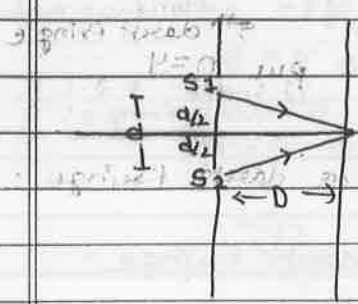
$$\boxed{\frac{I_1}{I_2} = \frac{49}{25}}$$

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Young double slit experiment [YDSE] :-

Thomas Young

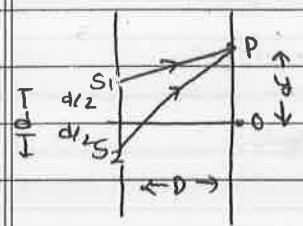
experiment prove \rightarrow Interference
[light \rightarrow wave nature]



$d \rightarrow$ distance b/w slits
 $D \rightarrow$ distance b/w slit and screen

$\Delta x = 0$
at O
Constructive central fringe
always bright

Screen



$$\Delta x = S_2P - S_1P = \frac{y d}{D}$$

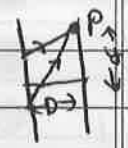
If $y = 0$ then $\Delta x = 0$ [Center of Screen (I)]

① Case (i) Bright fringe :-

Constructive interference
 $\Delta x = n \lambda \rightarrow$ [always named]

$$\Delta x = \frac{y d}{D} = n \lambda$$

If $n = 0$
 $y = 0$



$$y = \frac{n \lambda D}{d}$$

variation / position / distance of n^{th} Bright fringe

If $n = 1$ $\frac{\lambda D}{d}$ 1st Bright fringe

$$n = 2 \quad \frac{2 \lambda D}{d}$$

Fringe width = distance b/w $n=0$

Successive Bright fringe

$$= \frac{2 \lambda D}{d} - \frac{\lambda D}{d}$$

$$\left(\frac{\Delta \phi}{\lambda}\right)^2 = 200 \dots$$

Fringe width $\rightarrow \beta = \frac{\lambda D}{d}$

② Case (ii) Dark fringe :-

$$\Delta x = \left[2n + \frac{1}{2}\right] \lambda$$

$$\Delta x = \frac{y d}{D} = \left[2n + \frac{1}{2}\right] \lambda$$

$y = \frac{(2n + \frac{1}{2}) \lambda D}{2d} \rightarrow$ variation / position / distance of n^{th} dark fringe

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- $n=0$ $y_1 = \frac{1D}{2d}$ → 1st dark fringe ~~1st~~ n^{th} dark fringe :-
→ put $n = [n^{\text{th}} - 1]$
- $n=1$ $y_2 = \frac{3D}{2d}$ → 2nd dark fringe eg:- 7th dark fringe
→ put $n = 9$.
- $n=2$ $y_3 = \frac{5D}{2d}$ → 3rd dark fringe 5th dark fringe
put $n = 4$

Fringe width → distance b/w successive dark fringe.


$$\beta = y_2 - y_1$$

$$= \frac{3D}{2d} - \frac{1D}{2d}$$

$$\boxed{\beta = \frac{D}{d}}$$
 same as that of bright fringe

~~1st~~ In YDSE → equal width (β)

Key-points For YDSE :-

1. $\Delta x = \frac{y d}{D}$ 

2. Location of n^{th} bright fringe → [Constructive Interference]

$$\boxed{y = n \frac{\lambda D}{d}}$$

- 3rd bright → put $n = 3$
- 7th bright → put $n = 7$

3. width :-
$$\boxed{\beta = \frac{\lambda D}{d}}$$

4. Location of n^{th} ~~bright~~ dark fringe :- $I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$

$$\boxed{y = (2n+1) \frac{\lambda D}{2d}}$$

- 1st dark → $n = 0$
- 2nd dark → $n = 1$
- 3rd dark → $n = 2$
- 4th dark → $n = 3$

If $I_1 = I_2 = I_0$
$$\boxed{I = 4I_0 \cos^2 \left(\frac{\Delta \phi}{2} \right)}$$

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$$I = 4I_0 \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$I_{max} = [\sqrt{I_1} + \sqrt{I_2}]^2$$

$$I_1 = I_2 = I_0$$

$$I_{max} = 4I_0$$

$$I = I_{max} \cos^2\left(\frac{\Delta\phi}{2}\right)$$

max intensity $e^{i\omega t}$, $e^{i(\omega t + \phi)}$, $e^{i\omega t}$ Bright fringe constructive interference

$$I = I_{max} \cos^2\left(\frac{\Delta\phi}{2}\right) = I_{center} \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$I = I_{max} \cos^2\left(\frac{\Delta\phi}{2}\right) = I_{center} \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$\Delta d \rightarrow \frac{2\pi \Delta x}{\lambda}$

$$\Delta\phi = \frac{2\pi \Delta x}{\lambda} \rightarrow \text{path difference}$$

Phase difference

$$\cos \pi = -1, \cos 2\pi = +1$$

$$\frac{2\pi \Delta x}{\lambda} \Delta\phi = \frac{2\pi \times 1}{100} \times \frac{2\pi \Delta x}{100}$$

Q1 In YDSE the intensity of a light at a point on the screen where the path difference is $\lambda/4$ is K . calculate the intensity at a point where the path difference is $\lambda/2$.

- (a) K
- (b) $K/2$
- (c) $K/4$
- (d) 0

$$\Delta x = \lambda/4 \rightarrow I \rightarrow K$$

$$I = I_{max} \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$I = I_0 \times \cos^2\left(\frac{2\pi}{2}\right)$$

$$I = I_0$$

$$K =$$

$$\Delta x = \lambda/4 \rightarrow \frac{2\pi \times \lambda}{\lambda} \times \frac{\lambda}{4} = \frac{\pi}{2}$$

$$\Delta\phi = \frac{\pi}{2}$$

$$I = I_0 \times \cos^2\left(\frac{90^\circ}{2}\right)$$

$$I = I_0 \times \frac{1}{\sqrt{2}}$$

$$I = \frac{I_0}{2}$$

$$\frac{\Delta\phi}{2} = \frac{\pi}{2} = 90^\circ$$

$$I = K/4$$

Q2 In YDSE experiment the intensity of the central bright fringe is 8 mW/m^2 . calculate the intensity at a point where the path difference is $\lambda/3$.

AJFMG
2019

Q3 Sodium lamp illuminates yellow light.

$$\frac{2\lambda}{\lambda} \times \frac{1}{3} = \frac{2}{3}$$

(saathi)

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$$8 \times 10^{-3} \times \cos^2\left(\frac{2\lambda}{3\lambda}\right)$$

$$8 \times 10^{-3} \times \frac{1}{4}$$

$$I = 2 \times 10^{-3} \text{ W/m}^2$$

Q3 In YDSE the intensity of central bright fringe is $I_0 = 0.01 \text{ watt/m}^2$ then calculate the intensity at a point

Having path difference $\lambda/3$.

soln.

$$I = I_0 \cos^2\left(\frac{\pi}{2} \times \frac{\lambda/3}{\lambda}\right)$$

$$I = 0.01 \times \frac{1}{4}$$

$$I = \frac{0.01}{4}$$

$$I = 0.25 \times 10^{-2} \text{ W/m}^2$$

$$\Delta\phi = \frac{2\pi}{\lambda} \times \frac{\lambda}{3}$$

$$= \frac{2\pi}{3}$$

Ans.

$$\frac{2\pi}{3} \times \frac{\lambda}{\lambda}$$

$$\frac{2\pi}{3}$$

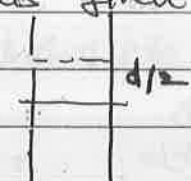
Q4 The maximum intensity in YDSE is I_0 . then calculate intensity in front of \pm one of the slits given.

$$D = 20 \text{ cm}$$

$$\lambda = 500 \text{ nm}$$

$$\Delta x = \frac{yD}{D}$$

$$\Delta x = \frac{d/2 \times D}{D}$$



soln.

$$I_{\text{max}} = I_0 \cos^2\left(\frac{90^\circ}{2}\right)$$

$$I_{\text{max}} = I_0 \times \frac{1}{2}$$

$$I_{\text{max}} = \frac{I_0}{2}$$

$$\Delta x = \frac{d}{20}$$

$$\Delta x = \frac{d}{20}$$

$$\Delta x = \frac{51}{20}$$

$$\Delta x = \frac{1}{4}$$

$$\Delta\phi = \frac{2\pi}{\lambda} \times \frac{\lambda}{4}$$

$$\Delta\phi = \frac{\pi}{2}$$

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos(\Delta\phi)$$

$$I \propto I_0 \cos^2\left(\frac{\Delta\phi}{2}\right)$$

dark
less dark

$$I_{\max} = [\sqrt{I_1} + \sqrt{I_2}]^2$$

$$I_{\min} = [\sqrt{I_1} - \sqrt{I_2}]^2$$

Constructive Interference → Both source have same intensity
dark → 95% or 96% Dark

Q. If intensity of source of interference change or if it change?
Contrast of fringes will decrease
dark become less dark

Q. In YDSE experiment the $\lambda = 600\text{nm}$. at a point the intensity is 50% of the max. value. then calculate the path difference at that point?

Solve:

$$I_{\max} = I_0 \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$\Delta\phi = \frac{\pi}{2}$$

$$\frac{50}{100} I_{\max} = I_{\max} \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$\frac{1}{2} = \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$\frac{\pi}{2} = \frac{2\pi}{\lambda} \times \Delta x$$

$$\frac{1}{\sqrt{2}} = \cos\left(\frac{\Delta\phi}{2}\right)$$

$$\frac{1}{4} = \Delta x$$

$$\frac{\pi}{4} = \frac{\Delta\phi}{2}$$

$$\frac{600 \times 10^{-9}}{4}$$

$$150\text{nm} = \Delta x$$

Q. Intensity of 2 coherent sources is 9 units and 4 units resp. then calculate the max. intensity in the interference pattern

Solve:

$$I_{\max} = [\sqrt{I_1} + \sqrt{I_2}]^2$$

$$= [\sqrt{9} + \sqrt{4}]^2 = (3+2)^2$$

$$= 9 \times 4 + 2 \times 3 \times 4 = 25 \text{ unit}$$

$$= 13 + 24 = 37$$

H.W. EXI → Q8, Q9, Q11, Q12, Q13, Q14, 15, 16, 17, 18, 20, 21, 22, 24, 25, 26, 27, 28, 30, 31, 32, 33, 36, 37, 39, 41, 42, 43, 46, 48, 49, 50, 53, 54, 68, 69.

Saathi

Date / /

Q3 Two waves having intensity I and same frequency superpose each other at a point, calculate the resultant intensity if they interfere constructively.

Solve $I_{max} = [\sqrt{I_1} + \sqrt{I_2}]^2$

$$I_{max} = 2I \times 2$$

$$I_{max} = 4I$$



Intensity of wave with width

Intensity of light \propto width of slit

$$\frac{I_1}{I_2} = \frac{\omega_1}{\omega_2}$$

कभी कभी हमें width of slit का ratio देना है $\frac{\omega_1}{\omega_2} = \frac{4}{9}$ मुझे समझना चाहिए।

$$\frac{I_1}{I_2} = \frac{4}{9}$$

width का ratio है 4 की intensity का ratio है।

Q3 Two slit in YDSE experiment have width ratio 1:25

calculate the ratio of I_{max} & I_{min}

$$\frac{I_1}{I_2} = \frac{1}{25}$$

$$I_{max} = 1 + 25 + 2 \times 1 \times 5$$

$$= 26 + 10 = 36$$

$$I_{min} = 1 + 25 - 2 \times 1 \times 5$$

$$= (1+25) - 10$$

$$= 16$$

$$\frac{I_{max}}{I_{min}} = \frac{36}{16} = \frac{9}{4}$$

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NOTE →

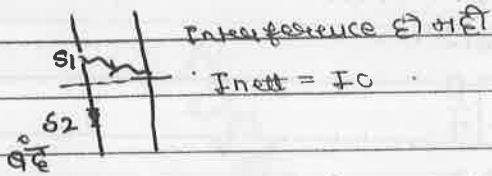


Result → In YDSE
if one of the slit is closed

$$I_{4I_0} = \frac{I}{4} \cdot 4I_0$$

$$I_{max} = 4I_0$$

If one of the slit is closed



Q1. In YDSE, the central maxima is observed to be I_0 . If one of the slit is closed then intensity at central maxima will be?

- (i) $\frac{I_0}{2}$ (ii) $\frac{I_0}{\sqrt{2}}$ (iii) $\frac{I_0}{4}$ (iv) I_0

Solve $I_{4I_0} = \frac{1}{4} I_{4I_0}$

$$I_{4I_0} = \frac{1}{4} I_0$$

Q2. In Intensity of central fringe obtained in the pattern due to two identical slit is I . When one of the slit is closed, the intensity at same I_0 then correct relation

(i) $I = I_0$

$$I_{4I_0} = \frac{1}{4} I_{4I_0}$$

(ii) $I = 2I_0$

$$I_0 = \frac{1}{4} I$$

(iii) $I = 4I_0$

$$I = 4I_0$$

(iv) $I = \frac{I_0}{4}$

When YDSE Setup is immersed in a liquid :-

$$\lambda \propto \frac{1}{\mu}$$

$$\lambda_{\mu} = \frac{\lambda_{air}}{\mu}$$

$$\beta_{\mu} = \frac{\beta_{air}}{\mu}$$

medium H immerse or H 42

β of H

2x4+1

Date ___/___/___

शुद्धी :- द मी. मर्यादा मर्यादा द/म पुत मर्यादा

air	medium
$\beta = 1D$	$\beta = \left[\frac{1}{\mu} \right] \frac{D}{d}$
→ Bright position	Bright position
$y = n \frac{\lambda D}{d}$	$y = n \times \left[\frac{1}{\mu} \right] \frac{\lambda D}{d}$
→ dark position	dark position
$y = [2n+1] \frac{\lambda D}{2d}$	$y = [2n+1] \frac{\lambda D}{2\mu d}$

Q2

NEET 2017, YDSE 2nd performed in air then in medium. It is found that 8th bright fringe in the medium is at where 5th dark fringe lies in air then calculate the μ of medium?

Solve.

$$8 \times \lambda \times \frac{D}{d} = 9 \times \frac{\lambda D}{2d}$$

$$\frac{16}{d} = \frac{9\lambda}{2d}$$

$$\boxed{\frac{16}{9} = \mu}$$

Q2. In YDSE. $d = 0.12 \text{ mm}$.
 $D = 1 \text{ m}$
 $\lambda = 6000 \text{ \AA}$

- (i) find position of 2nd maxima from center.
- (ii) position of 3rd minima from center.

(1)

$$y = n \frac{\lambda D}{d}$$

$$2 \times \frac{6000 \times 10^{-10} \times 1}{0.12 \times 10^{-3}}$$

$$1500 \times 10^{-11}$$

$$1.5 \times 10^{-8} \text{ meter}$$

Date ___ / ___ / ___

$$\begin{aligned}
 \lambda_0 = \text{3rd minima} &= \frac{(2 \times 2 + 1) 6 \times 10^{-7} \times 1}{2 \times 12 \times 10^{-5}} \\
 &= \frac{5 \times 6 \times 10^{-7}}{2 \times 12 \times 10^{-5}} \\
 &= \frac{25 \times 10^{-3}}{2} \text{ meter}
 \end{aligned}$$

Q3. In YDSE the slits are 2mm apart and it is illuminated with a light of $\lambda_1 = 12000 \text{ \AA}$ and $\lambda_2 = 10,000 \text{ \AA}$. At what minimum distance from the common central bright fringe on the screen 2m from the slit a bright fringe from 1 interference pattern coincide with bright fringe from other interference pattern?

Solve $d = 2\text{mm} = 2 \times 10^{-3}$
 $D = 2\text{m}$

$$\begin{aligned}
 y &= \frac{n_1 \lambda_1 D}{d} = \frac{1 \times 12000 \times 10^{-10} \times 2}{2 \times 10^{-3}} \\
 &= 6 \times 2 \times 10^{-7} \\
 &= 12 \times 10^{-7} \Rightarrow 1.2 \times 10^{-6} \times 10^3 \\
 &= 1.2 \times 10^{-3} \text{ m}
 \end{aligned}$$

Bright fringe at location

$$y = \frac{n \lambda D}{d}$$

$$\begin{aligned}
 \lambda_1 &= 12000 \text{ \AA} \\
 \lambda_2 &= 10000 \text{ \AA}
 \end{aligned}$$

$$y_1 = \frac{n_1 \lambda_1 D}{d}$$

$$y_2 = \frac{n_2 \lambda_2 D}{d}$$

exactly overlapp \rightarrow

$$\frac{n_1 \lambda_1 D}{d} = \frac{n_2 \lambda_2 D}{d}$$

$$\frac{n_1}{n_2} = \frac{\lambda_2}{\lambda_1} = \frac{12}{10}$$

$$\boxed{\frac{n_1}{n_2} = \frac{5}{6}}$$

$$y = \frac{n \lambda D}{d}$$

$$= \frac{5 \times 12000 \times 10^{-10} \times 2}{2 \times 10^{-3}}$$

$$= \underline{6 \text{ mm}}$$

$\lambda_1 = 12000 \text{ \AA}$ at 5th Bright

$\lambda_2 = 10000 \text{ \AA}$ at 6th Bright

Solved) 1, 2, 3, 5, 6, 7, 8.

Q. 809 → complete.

2 → 3, 4, 6, 7, 9, 10.

Ex II → 1, 2, 4, 6, 8, 13, 15, 17, 19, 20, 22, 23, 26, 28.

Date / / 29, 30, 36

Saathi

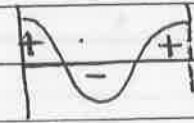
Intensity Average: -

[cos φ average = 0.]

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

Source → Incoherent

Phase difference → always change



$$I_{\text{net}} = I_1 + I_2 + 2\sqrt{I_1 I_2} \times [0]$$

$$I_{\text{net}} = I_1 + I_2$$

Ex II

Q22. Bright Fringe →

Pr

$$y = \frac{\lambda D}{d}$$

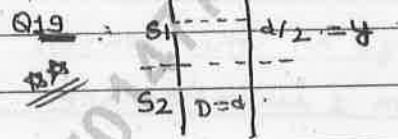
$$y \propto \lambda$$

$$\frac{y_1}{y_2} = \frac{\lambda_1}{\lambda_2}$$

$$\frac{20 \text{ mm}}{y_2} = \frac{500 \times 10^{-9}}{550 \times 10^{-9}}$$

$$y_2 = 21 \text{ mm}$$

$$\Delta y = y_2 - y_1 = 1 \text{ mm}$$



$$I = I_0 \cos^2 \left(\frac{\Delta \phi}{2} \right)$$

$$\Delta \phi = ?$$

$$\Delta \phi = \frac{2\pi}{\lambda} \Delta x$$

$$\Delta x = \frac{y d}{D}$$

$$\Delta x = \frac{d/2 \times d}{D}$$

$$\Delta x = \frac{d^2}{2D}$$

$$\Delta x = \frac{d^2}{4D}$$

$$\Delta x = \frac{d}{4}$$

$$\Delta \phi = \frac{2\pi \times d}{\lambda \times 4}$$

$$\Delta \phi = \frac{\pi}{2}$$

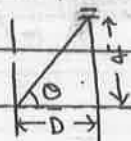
$$I = \frac{I_0}{2}$$

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Angular position / Angular Fringe width concept →

NEET = 2018
NEET = 2019

position / location of Bright fringe from centre



$$y = \frac{n\lambda D}{d}$$

angular position of Bright fringe →

$$\theta = \frac{n\lambda}{d}$$

$\sin \theta = \frac{y}{D}$ Funda

angular fringe width →

$$\alpha = \frac{\lambda}{d}$$

$\alpha \rightarrow$ ENTH radian θ

$$d_{med} = \frac{\alpha \lambda d}{\lambda}$$

position
Bright

$$y = \frac{n\lambda D}{d}$$

→ dark

$$y = (2n+1) \frac{\lambda D}{2d}$$

→ Fringe width

$$\beta = \frac{\lambda D}{d}$$

angular position

~~$$y = \frac{n\lambda D}{d}$$~~

$$\theta = \frac{n\lambda}{d}$$

$$\theta = (2n+1) \frac{\lambda}{2d}$$

angular fringe

$$\alpha = \frac{\lambda}{d}$$

Q1. YDSE

$\lambda \rightarrow$ same

$$d_1 = 0.2 \text{ mm}$$

319

$$\alpha_2 = 0.21$$

angular fringe width

distance b/w slits $d_2 = ?$

$$\alpha_1 = 0.20$$

Solve

$$\alpha = \frac{\lambda}{d}$$

$$\frac{\alpha_1}{\alpha_2} = \frac{d_2}{d_1}$$

$$\frac{0.20}{0.21} = \frac{d_2}{0.2}$$

$$\frac{0.20 \times 0.2}{0.21} = \frac{0.40}{0.21} = d_2 = \frac{4}{21} = 0.19 \text{ mm}$$

Q2

In YDSE the distance b/w the slits is $d = 0.2 \text{ mm}$ and the screen is placed at a distance of 25 cm and wavelength of light used is 5000 \AA then calculate angular position of first dark fringe?

Solve

$$\theta = \frac{\lambda}{2d}$$

$$2500 \times 10^{-3} \quad 2.5 \pi$$

$$= \frac{25 \times 10^{-7} \times \pi}{2 \times 0.2 \times 10^{-3}} = 25 \times 10^{-3} \times \pi$$

$$2.5 \pi$$

Ex 7 → 60, 68, 47, 52, 55, 56, 58, 63, 65, 67, 66, 71, 72, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100

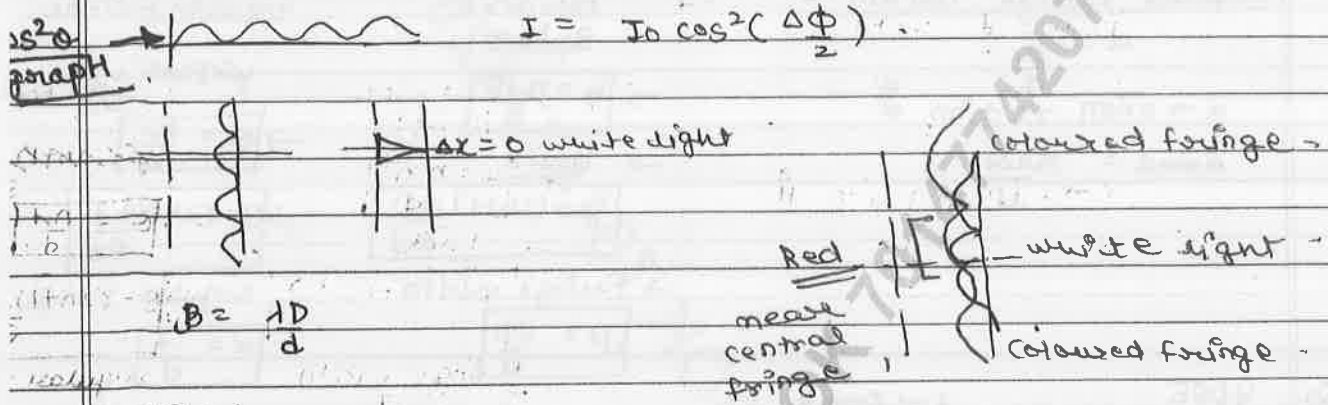
Saathi

Date: / /

$$\theta = \frac{1.99 \times 10^8 \times 2.5 \times 10^{-3}}{1.25 \times 10^8}$$

$$\theta = 0.45 \text{ radians}$$

YDSE setup with the help of white light :-



$$\beta = \frac{D}{d}$$

$$\beta \propto 1$$

जिसका 1 ज्यादा उसका β भी ज्यादा

VFBOR → 1 ज्यादा

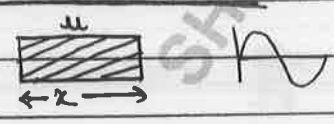
Red ⇒ 1, β ज्यादा

white light → सभी colour का maxima centre पर overlap.

central fringe → white → NEET

central fringe की आस-पास कौन सा colour Red colour

Effect of thin film →



इसकी समय में

$$\mu = \frac{c}{v} \Rightarrow v = \frac{c}{\mu}$$

$$\text{time} = \frac{\text{distance}}{\text{speed}} = \frac{t}{\frac{c}{\mu}}$$

← x → !
कौन distance = ?
distance = speed × time

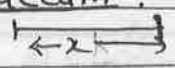
$$x = \mu x$$

$$x' = \frac{\mu x}{\mu}$$

$$x' = \mu x$$

medium

vacuum



$$\Delta\phi = \frac{2\pi}{\lambda} \times 2x$$

$$\Delta\phi = \frac{2\pi}{\lambda} \Delta x \text{ रदा}$$

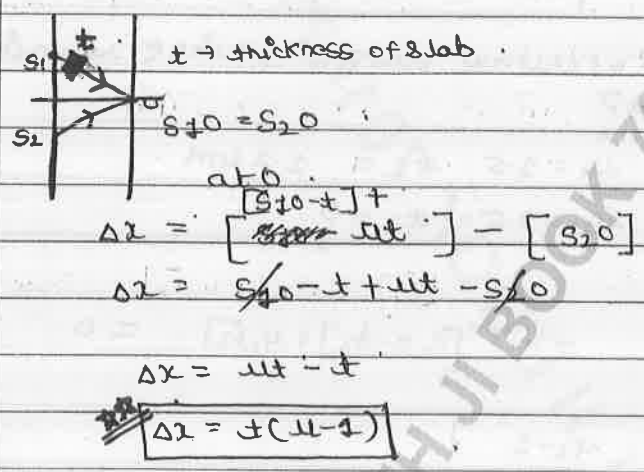
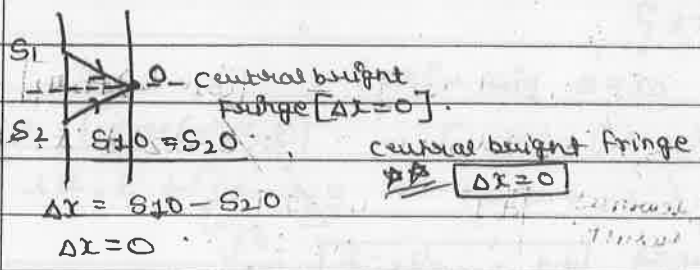
$$\Delta\phi = \frac{2\pi}{\lambda} \times \mu x$$

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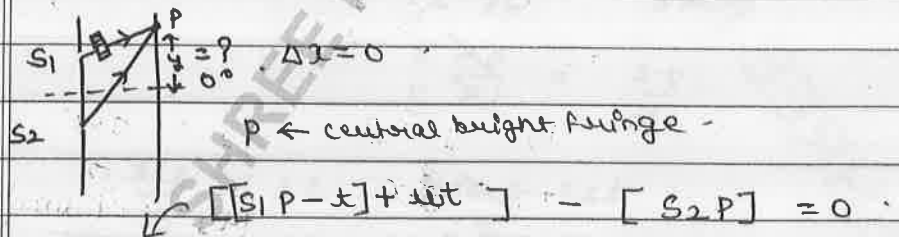
Conclusion →

medium में $\mu < 1$ चलाता = Vacuum में $\mu < 1$ चलाता

medium में $\mu > 1$ चलाता = Vacuum में $\mu > 1$ चलाता



at O $\Delta x \neq 0$
 इसी कारण मध्य में O पर central bright fringe नहीं बनती।



Learn how to write it very imp
 For questions asked in NEET & AFMS
 $S_1P - t + \mu t - S_2P = 0$
 $t(\mu - 1) = S_2P - S_1P$
 $t(\mu - 1) = yd$

$y = \frac{t(\mu - 1)D}{d}$	इसी कारण central bright fringe shift होता है।
Next fringe displaced = $\frac{y}{\beta}$	

Show that Δx for slab = $t(\mu-1) = \frac{yd}{D}$

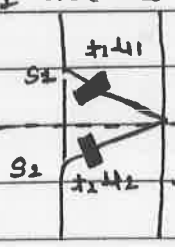
Δx for 2 slab = $(\mu_1-1)t_1 = (\mu_2-1)t_2$

saathi

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Practice →

Q1. If central fringe is formed at 0. find relation b/w μ_1 and μ_2 t_1 and t_2 ?



$\Delta x = 0$ ही गोटा घडोण ।

$[(S_1 0 - t_1) + t_1 \mu_1] - [(S_2 0 - t_2) + t_2 \mu_2] = 0$

$S_1 0 - t_1 + \mu_1 t_1 = S_2 0 - t_2 + \mu_2 t_2$

Result

$\frac{t_1}{t_2} = \frac{\mu_2 - 1}{\mu_1 - 1}$

Q2



Q1 If position of central bright fringe remain unaltered?

Slab 1 = $\mu_1 = 1.5$ $t_1 = 1.2 \mu m$

Slab 2 = $\mu_2 = 2.5$ $t_2 = ?$

Solve $\Delta x = 0$

$[(S_1 0 - t_1) + \mu_1 t_1] - [(S_2 0 - t_2) + \mu_2 t_2] = 0$

Q3

Slab 2 राना अत
Fringe-width अत
no effect

$\frac{t_1}{t_2} = \frac{\mu_2 - 1}{\mu_1 - 1}$

$\frac{1.2 \mu m}{t_2} = \frac{2.5 - 1}{1.5 - 1}$

$\frac{1.2}{t_2} = \frac{0.5}{0.5} \Rightarrow t_2 = 1.2 \mu m$

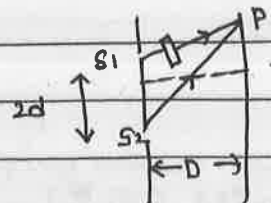
~~$t_2 = 1.2 \mu m$~~

$t_2 = \frac{1.2}{3}$

~~$t_2 = 0.4 \mu m$~~

$t_2 = 0.4 \mu m$

Q3



calculate displacement of fringe system

$t(\mu-1) = \frac{y d}{D}$

$y = \frac{t(\mu-1) D}{d}$

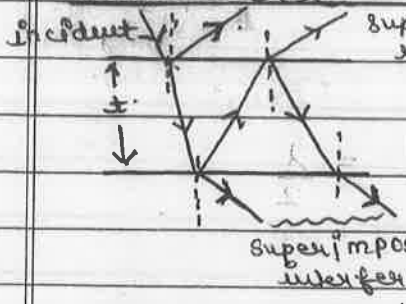
$= \frac{t \left(\frac{5}{3} - 1 \right) D}{d}$

$= \frac{t \times \frac{2}{3} D}{d}$

$= \frac{2 t D}{3 d}$

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Colour in a thin Film \rightarrow



$t = 0.4 \mu m$ [order]

μ = refractive index
 t \rightarrow thickness of film
 α \rightarrow angle of refraction

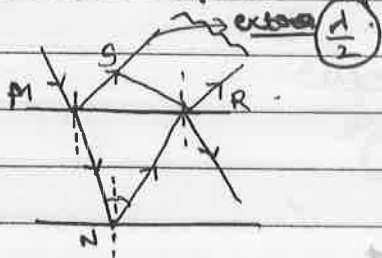
Transmitted System

$\Delta x = 2\mu t \cos \alpha$ α \rightarrow refracted angle

If Bright $\rightarrow \Delta x = n\lambda$

If dark $\rightarrow \Delta x = (2n+1) \frac{\lambda}{2}$

what about reflected system \rightarrow



$\frac{1}{2}$ λ \rightarrow 2nd concept [wave theory]

rarer \rightarrow denser
 at boundary $\phi = \pi$

$\Delta x = ?$

$\lambda = \frac{2\pi \times \Delta x}{1}$

$\Delta x = 2\mu t \cos \alpha - \frac{\lambda}{2}$

reflected system

$\Delta x = \frac{\lambda}{2}$

Conclusion \rightarrow reflected system $\rightarrow \Delta x = 2\mu t \cos \alpha - \frac{\lambda}{2}$

\rightarrow transmitted system $\rightarrow \Delta x = 2\mu t \cos \alpha$

\rightarrow Bright $\rightarrow \Delta x = n\lambda$

\rightarrow Dark $\rightarrow \Delta x = [2n+1] \frac{\lambda}{2}$

Q1. Light of $\lambda = 6000 \text{ \AA}$ is incident on a thin glass plate of $\mu = 1.5$ such that angle of refraction into the plate is 60° then calculate the smallest thickness of the plate which will make it appear dark by reflection? put $n=1$ [minimum]

Solve

$\Delta x = (2n+1) \frac{\lambda}{2}$

$2 \times 1.5 \times t \times \cos 60^\circ = \frac{3 \times 6 \times 10^{-7}}{2}$

$3 \times t = 3 \times 6 \times 10^{-7}$

$t = \frac{6 \times 10^{-7}}{3}$

$t = 2 \times 10^{-7}$

$t = 0.4 \mu m$

Date ___/___/___

Q3 Concept \rightarrow Reflected system -
 $t \rightarrow 0$ [thickness negligible] -

कौन सी कोलर?

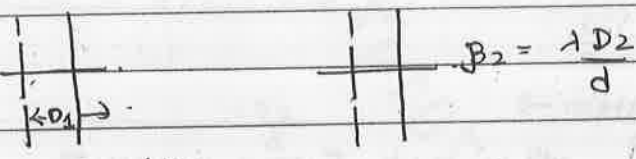
$$\Delta x = \frac{2\mu t \cos \theta}{\lambda} = \frac{1}{2} \quad \Delta x = \frac{-1}{2} = \frac{1}{2}$$

$\Delta x \geq \lambda/2$ implies

Destructive (dark)

Q5

B.Box 2



$$\beta_1 = \frac{\lambda D_1}{d}$$

$$\beta_2 - \beta_1 = \frac{\lambda \Delta D}{d}$$

$$\Delta \beta = \frac{\lambda \Delta D}{d}$$

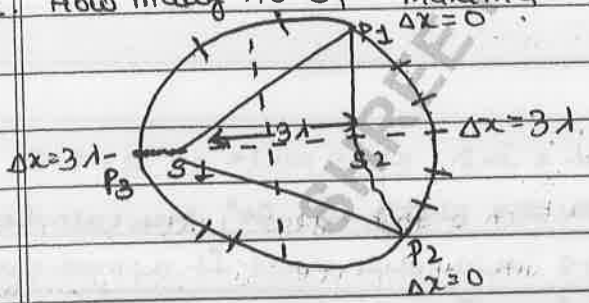
$$3 \times 10^{-5} = \frac{\lambda (5 \times 10^{-2})}{10^{-3}}$$

$$\frac{3 \times 10^{-8}}{5 \times 10^{-2}} = 0.6 \times 10^{-6}$$

$$6 \times 10^{-8} = \lambda$$

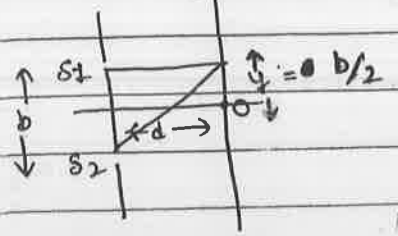
$$600 \text{ nm} = \lambda$$

Q1. How many no. of maxima are obtained on circular screen?



$n = 12$

Q2. In the given situation Separation b/w slit is b and screen is placed at d from the slits at a point on the screen directly in front of one of the slits, certain wavelengths are missing find these missing wavelengths?



Missing \rightarrow Destructive

Destructive -

$$\Delta x = (2n+1) \frac{\lambda}{2}$$

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$$\frac{b \times b}{d} = \frac{b^2}{2d}$$

$$\frac{b^2}{2d} = (2n+1) \frac{\lambda}{2}$$

$$\lambda = \frac{2b^2}{(2n+1)d} \quad \text{missing wavelengths}$$

put $n=0$ $\lambda = b^2/d$

$n=1$ $\lambda = \frac{b^2}{3d}$... and so on

Q2 In YDSE it is found that the intensity ratio b/w bright and dark fringes is 9 calculate

(i) $\frac{I_1}{I_2}$ Solve $\frac{I_{max}}{I_{min}} = 9$

(ii) $\frac{a_1}{a_2}$ $\frac{\sqrt{I_1} + \sqrt{I_2}}{\sqrt{I_1} - \sqrt{I_2}} = \frac{3}{1}$

$$\sqrt{I_1} + \sqrt{I_2} = 3\sqrt{I_1} - 3\sqrt{I_2}$$

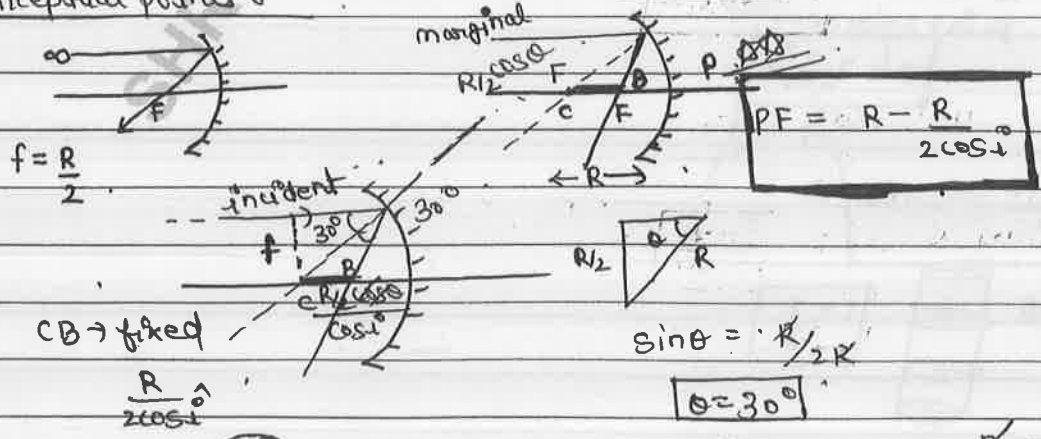
$$4\sqrt{I_2} = 3\sqrt{I_1} - \sqrt{I_1}$$

$$\frac{4}{2} = \frac{\sqrt{I_1}}{\sqrt{I_2}}$$

$$\frac{2}{1} = \frac{\sqrt{I_1}}{\sqrt{I_2}} = \frac{a_1}{a_2}$$

$$\frac{4}{1} = \frac{I_1}{I_2}$$

Conceptual points :-



CB \rightarrow fixed

$$\frac{R}{2 \cos \theta}$$

$$\sin \theta = \frac{R/2}{R}$$

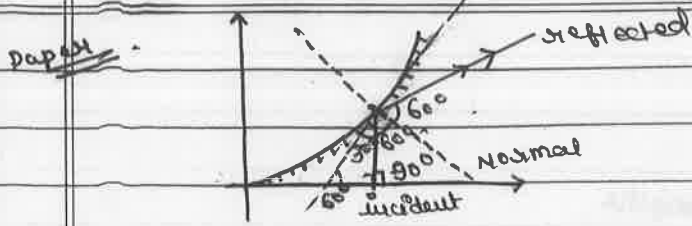
$$\theta = 30^\circ$$

$$\left(\frac{CB}{f} \right) = ?$$

distance CB $\rightarrow \frac{R}{2 \times \sqrt{3}/2} = \frac{R/\sqrt{3}}{R/2}$

$$2/\sqrt{3}$$

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$$\frac{dy}{dx} = \tan \theta$$

$$2(2x) = \tan \theta$$

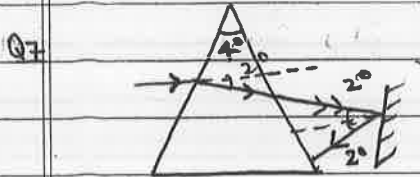
$$4x = \sqrt{3}$$

$$x = \frac{\sqrt{3}}{4}$$

mirror = $\theta = 180 - 2i$
 $60^\circ = 180 - 2i$

$$120 = 2i$$

$$i = 60^\circ$$



$$S = (u-v)A$$

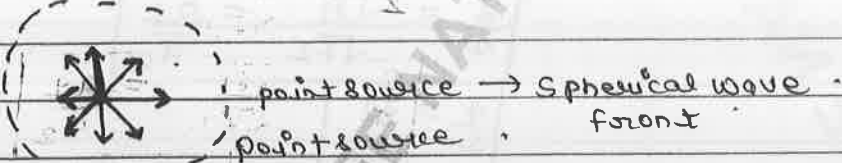
$$= (2.5-2) \times 4$$

$$S = 2.00$$

Q • By what angle the mirror is rotated so that ray after reflection become horizontal?

Q7 ~~mirror ki theta~~ reflected ray 2° horizontal
ray 2° horizontal → mirror 1° horizontal

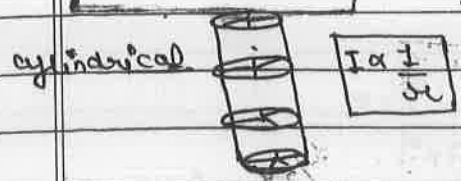
Huygen's wave Theory :- The locus of all the point which vibrate in same phase is called wavefront



point source

$$I \propto \frac{1}{r^2}$$

line source



Date ___ / ___ / ___

Huygen's wave theory :-

Hypothetical medium \rightarrow Ether.

~~main drawback~~ \rightarrow explanation of medium ether.

Huygen's wave theory is applicable for all types of wave -
wave nature.

Interference } explanation
diffraction } explanation

photoelectric effect \rightarrow cannot explain by Huygen's wave theory.

Wavefront kaise travel krte :-

Geometrical construction

Secondary wavelets

at consecutive wavefronts
distance = λ

Wavefront travels with speed of light

$\Delta x = n \lambda$
 $\Delta x = 0, \lambda, 2\lambda, \dots$

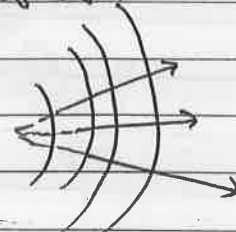
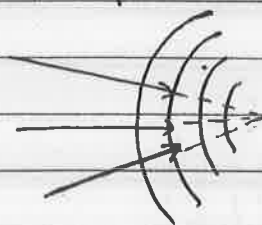
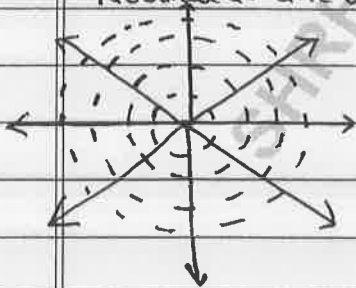
$\Delta x = (2n+1) \lambda / 2$
 $\frac{\lambda}{2}, \frac{3\lambda}{2}, \dots$

Each point on wavefront acts as a source of secondary wavefront. It emits wavelets in all direction which travel with the speed of light.

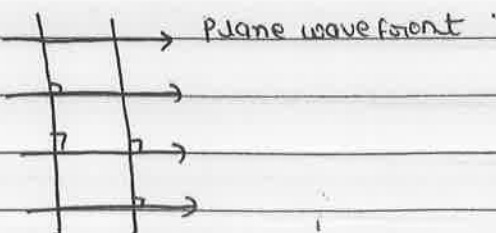
The tangent plane to these secondary wavelets represent new position of the wavefront.

~~concept~~ \rightarrow

Normal to the wavefront represents ~~ray~~ ray of light.

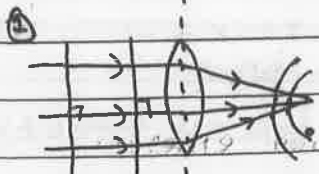


Diverging wavefront -



saathi

Date / /



Incident wavefront
Plane

Reflected wavefront
Spherical



plane
[Incident]

Diverging wavefront
reflected



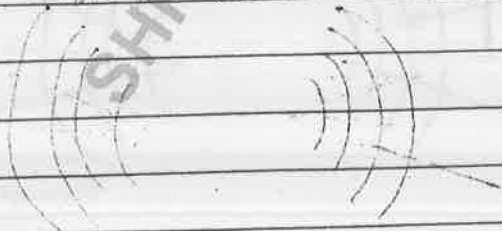
plane
[Incident]

plane
[reflected]



incident
plane

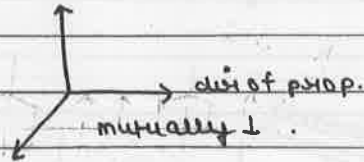
Reflected



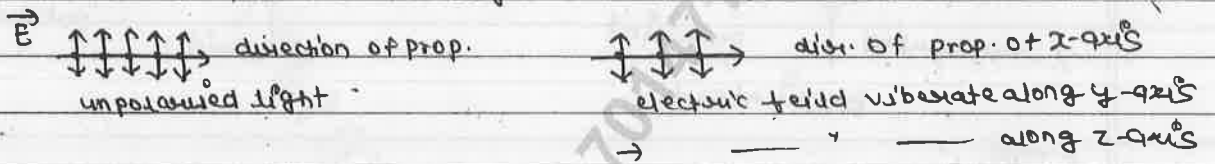
Date ___ / ___ / ___

SECTION-B

Polarisation → According to Maxwell light waves are electromagnetic transverse wave in which \vec{E} , \vec{B} and direction of propagation are mutually perpendicular to each other.



unpolarised light → If dir. of \vec{E} is present in all possible directions then such a light is called unpolarised light.



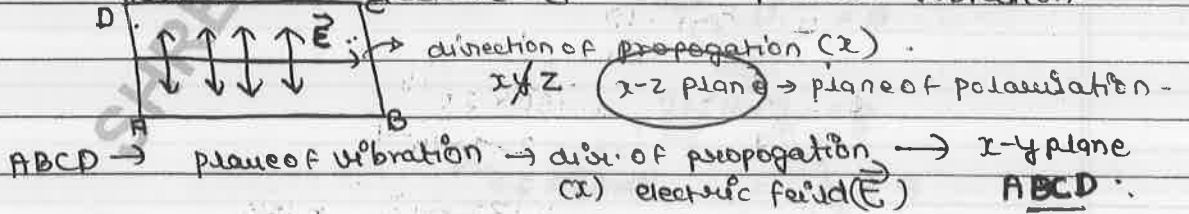
Polarised light → If direction of E restricted to only in \perp plane.



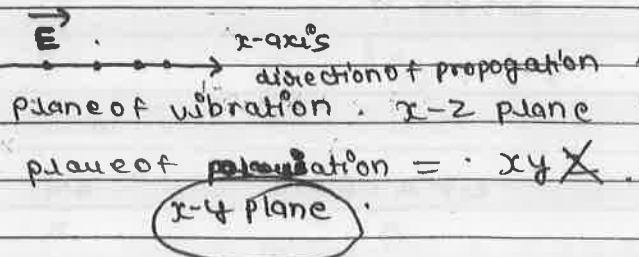
Plane of vibration and plane of polarisation

Plane of polarisation → The plane containing direction of propagation plane which is perpendicular to plane of vibration and there is no vibration of \vec{E} called plane of polarisation.

Plane of vibration → The plane containing direction of propagation and vibration of electric \vec{E} called plane of vibration.



Ex 2



methods to convert unpolarised light into polarised light →

- ① By dichroism (By polaroid) - [Law of Malus]
- ② By reflection [Brewster's law]
- ③ By double refraction
- ④ By scattering

2.7×10
 $\frac{216}{2.7 \times 10}$
 486

saathi

Date ___/___/___

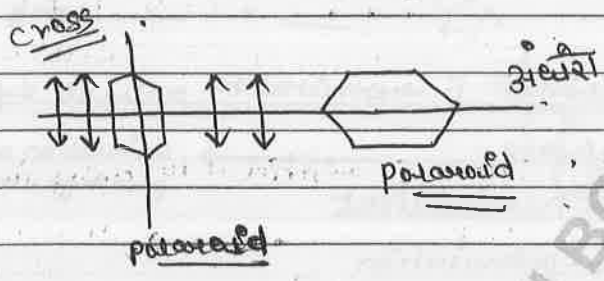
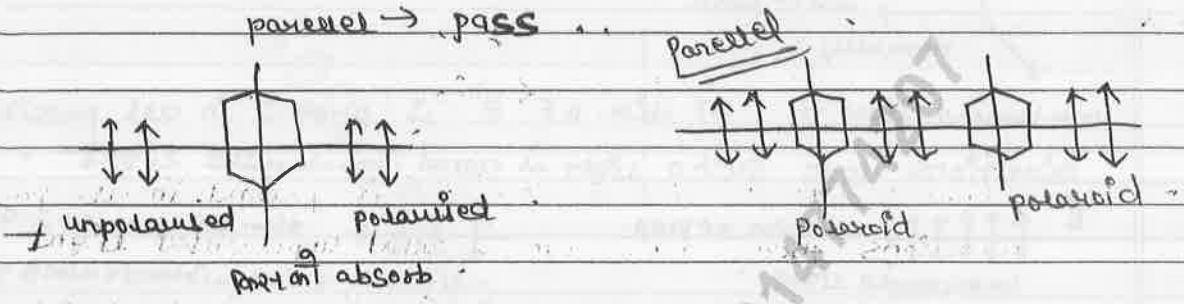
By Dichroism :-

Nature \rightarrow Special crystal \rightarrow Tourmaline.

Property \rightarrow Transmission axis $\&$ 1 component $\&$ absorb.

property \rightarrow Dichroism

parallel \rightarrow pass



Race \rightarrow Interference

Q. $d = 0.4 \text{ mm} = 4 \times 10^{-4} \text{ m}$

$D = 20 \text{ cm} = 20 \times 10^{-2} \text{ m}$

$\lambda = 5460 \text{ \AA} = 5460 \times 10^{-10} \text{ m}$

$\theta = \frac{\lambda}{2d}$

$\theta = \frac{(2n+1)\lambda}{2d}$

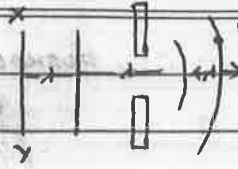
$\theta = 1 = \frac{2730 \times 10^{-10}}{2 \times 4 \times 10^{-4}}$

$2730 \times 10^{-6} \times 10^6$

$2.7 \times 1.8 \times 10^1 = 0.4$

$\lambda \times \lambda = \dots$

Date / /



time = distance / speed

$$t = \frac{3\lambda}{c}$$

Q17 $I = I_0 \cos^2(\frac{\Delta\phi}{2})$

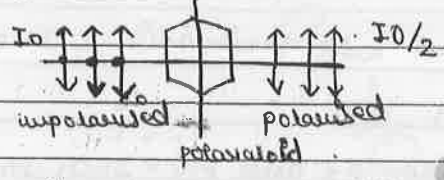
$d \rightarrow I_0$

$\frac{2\pi \times d}{\lambda} \times \lambda$ (2π)

$\frac{d}{\lambda} = \frac{2\lambda \times \frac{1}{3}}{\lambda} \Rightarrow \frac{\pi}{3} = 60^\circ$

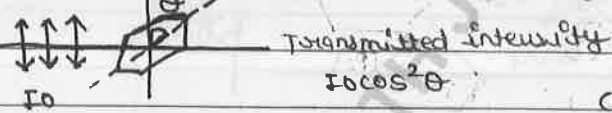
$$I = \frac{I_0}{4}$$

Conceptual point :-

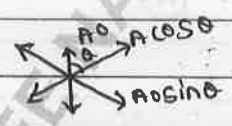
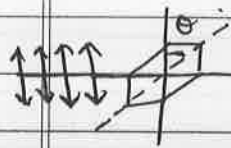


Polaroid -> Based on principle of dichroism

Law of Malus :-



Component $\rightarrow A \cos \theta$ [Pass \rightarrow Transmit]
Intensity = ?
 $I \propto (\text{amp})^2$



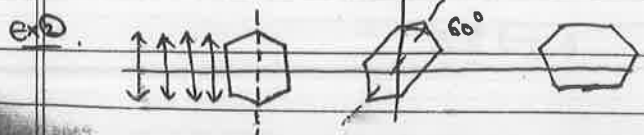
Trans. $I = K(\text{amp})^2$
 $= K(A_0 \cos \theta)^2$
 $= K A_0^2 \cos^2 \theta$

How to apply Malus law \rightarrow

Trans. $I = I_0 \cos^2 \theta$



$I = I_0 \cos^2 \theta$
 $I = \frac{I_0}{2} \times (\frac{\sqrt{3}}{2})^2$
 $I = \frac{I_0 \times 3}{2 \times 4} = \frac{3I_0}{8}$



P2 and P3 are \perp to each other

~~Q3~~ [Malus law if angle consecutive of air is given write]]

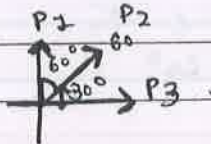
Saathi

Date ___ / ___ / ___

$$\frac{I_0 \times \cos^2(\theta)}{2}$$

$$\frac{I_0 \times \frac{1}{4}}{2} = \frac{I_0}{8} = P_2$$

$$P_3 = I = \frac{I_0}{8}$$



~~Q3~~ Malus law →

$$\frac{I_0 \times \cos^2 30}{8}$$

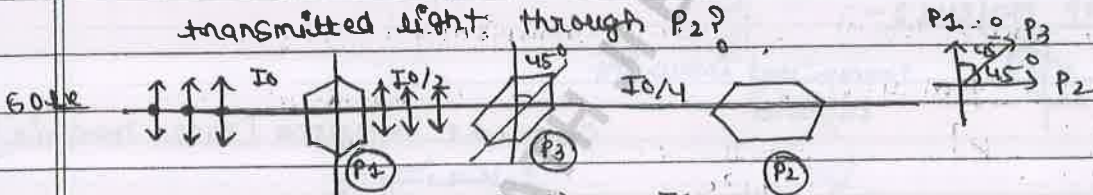
$$\frac{I_0 \times \frac{3}{4}}{8} = \frac{3I_0}{32}$$

Q3 NEET 2017

Two polaroids P₁ and P₂ are placed with their axis ⊥ to each other.

unpolarised light I₀ is incident on P₁.

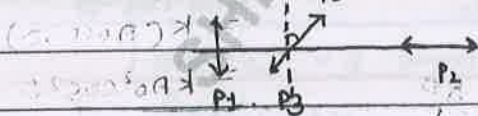
A 3rd polaroid P₃ is kept b/w P₁ and P₂ such that its axis makes an angle of 45° with P₁ then calculate the I of transmitted light through P₂?



$$I_{P3} = \frac{I_0 \cos^2(45^\circ)}{2} = \frac{I_0}{4}$$

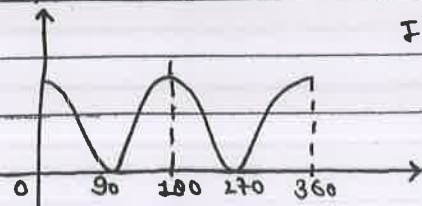
$$I_{P2} = \frac{I_0 \cos^2 45^\circ}{4} = \frac{I_0}{8}$$

simplified diagram - 45°



Conceptual points :- $I = I_0 \cos^2 \theta$

I is function of $\cos^2 \theta$



Polaroid → Intensity

maximum = 2 times

minimum = 2 times

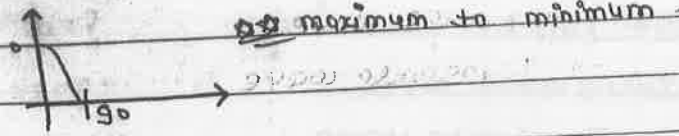
$\Delta \rightarrow 2\pi$

11/10/2021

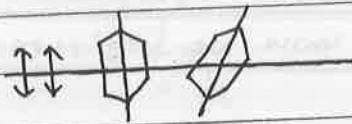
Saathi

Date ___ / ___ / ___

Q. Two polaroids are oriented such that their principle axis making an angle of 60° with each other. Calculate the % of incident unpolarised light which pass through the system?



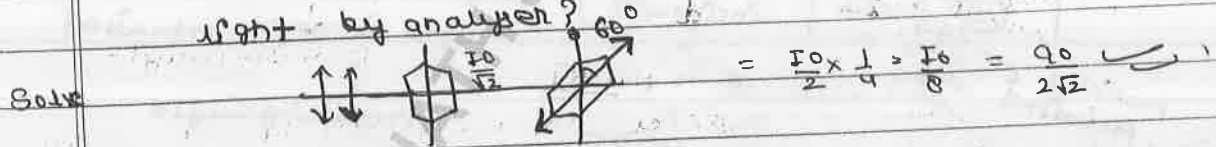
Q. Two polaroids are oriented such that their principle axis making an angle of 60° with each other. Calculate the % of incident unpolarised light which pass through the system?



$$\frac{I_0 \cos^2 60^\circ}{2} = \frac{I_0 \times \frac{1}{4}}{2} = \frac{I_0}{8}$$

$$\frac{I_0}{8} \times 100 = 12.5\%$$

Q. Unpolarised light has a amplitude a_0 and angle b/w analyser and polariser. Calculate the amplitude of transmitted light by analyser?



Solve

$$I \propto a^2$$

$$\frac{I_0 \cos^2 60^\circ}{2} = \frac{I_0}{4} = \frac{a_0^2}{2}$$

P.T.O

Ex 1 → 1-7, 106-121

Ex 3 → 1-5, 7-10

Bag Box (6) → Complete

Saathi

Date / /

Only Transverse wave can be polarised

Light wave are Transverse wave

Electromagnetic wave → Transverse wave

Radio-wave

micro-wave

Infrared

Visible

U.V rays

X-rays

γ-rays

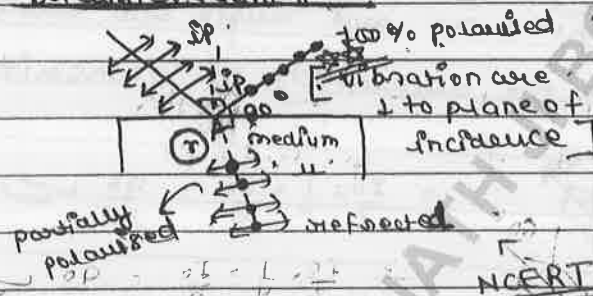
Electromagnetic waves
They can be polarised

Sound wave → cannot be polarised

because sound wave are longitudinal waves

Method no. 2 :- By Reflection

Brewster's Law :-



i_p → polarising angle
↓
angle of incidence at which reflected light is 100% polarised.
↓
polarising angle

Experiments →

at particular angle

extent of polarisation depend on angle of incidence

reflected ray → 100% polarised

reflected ray and refracted ray are \perp to each other

Snell's Law :-

Derivation →

$$i_p + 90 + r = 180^\circ$$

$$r = 90 - i_p$$

$$\mu \sin i_p = \mu \sin r$$

$$\mu \sin i_p = \mu \sin(90 - i_p)$$

$$\sin i_p = \mu \cos i_p$$

$$\tan i_p = \mu$$

concept :-

$$\mu = \tan i_p$$

$$\mu = c/v$$

critical angle

$$\sin i_c = 1/\mu$$

Date ___ / ___ / ___

Ex 2 angle of polarisation $i_p = 60^\circ$

$\mu = ?$

Speed of light in medium

angle of refraction = ?

Solve $\mu = \tan i_p$

① $\mu = \sqrt{3}$

$\mu = \frac{c}{v}$

② $v = \frac{c}{\sqrt{3}} = 2.732 \times 10^8$

③ $\sin r = \frac{1}{\sqrt{3}}$

$r = \sin^{-1} \frac{1}{\sqrt{3}}$

Ex 2 medium

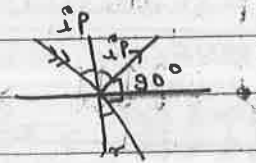
$\mu = 1.732 = \sqrt{3}$

angle of refraction = $r = ?$

$\mu = \tan i_p$

$\sqrt{3} = \tan i_p$

$i_p = 60^\circ$



$i_p + 90 + r = 180$

$r = 90^\circ$

Q3

$R = \sqrt{a_1^2 + a_2^2 + 2a_1a_2 \cos \phi}$

$= \sqrt{a^2 + a^2 + 2a^2 \cos \phi}$

$= \sqrt{2a^2 + 2a^2 \cos \phi}$

$= \sqrt{2a^2 (1 + \cos \phi)}$

$\cos \phi = \frac{2 \cos^2 \delta_1 - 1}{2}$

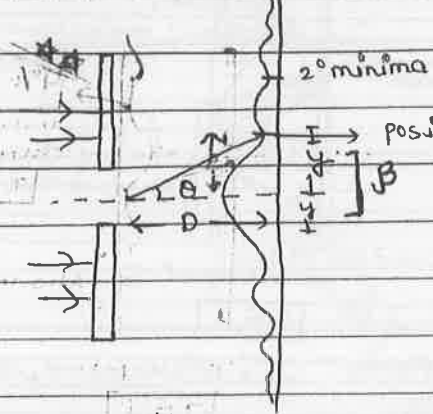
$R = \sqrt{2a^2 (1 + \frac{2 \cos^2 \delta_1 - 1}{2})}$

$R = 2a \cos^2 \delta_1$

(saathi)

Date ___/___/___

Position of minima :-



$\tan \theta = \frac{y}{D}$
 $\theta = y/D$

$I = I_0 \sin^2 \left(\frac{\pi a \sin \theta}{\lambda} \right)$

minima $I = 0$

$\sin^2 \left(\frac{\pi a \sin \theta}{\lambda} \right) = 0$

$\sin \left(\frac{\pi a \sin \theta}{\lambda} \right) = 0$

$\sin 0^\circ = 0$ or $\pi, 2\pi, 3\pi, 4\pi, \dots, n\pi$

$\sin \left[\frac{\pi a \sin \theta}{\lambda} \right] = \sin n\pi$

$\frac{\pi a \sin \theta}{\lambda} = n\pi$

$a \sin \theta = n\lambda$ Condition of minima

put $n = 1, 2, 3$

1st minima \rightarrow

put $n = 1$

$a \sin \theta = \lambda$

$\sin \theta = \lambda/a$

$\theta = \lambda/a$ angular position of 1st minima

position of 1st secondary minima

$y = \frac{\lambda D}{a}$ Frequent asked Question

$a =$ width of slit

NOTE \rightarrow width of central maxima $= 2y$

angular width of central maxima $= 2\theta$

SHORT NOTES :-

(i) Fraunhofer single slit diffraction \rightarrow

wavefront \rightarrow Plane



$\Delta x = \lambda$

$\sin \theta = \lambda/a$

maxima central maxima

Date ___/___/___

width \rightarrow unequal

central maxing \rightarrow width \rightarrow other fringes \rightarrow compression \rightarrow double \therefore

(5) position of secondary maxima \rightarrow

$$a \sin \theta = n \lambda \quad n = 1, 2, 3, 4, \dots$$

position of secondary minima \rightarrow

$$a \sin \theta = (2n+1) \frac{\lambda}{2} \quad n = 1, 2, 3, \dots$$

$$\text{width of central maxima} = \frac{2\lambda D}{a}$$

$$\text{width of central minima} = \frac{2\lambda}{a}$$

* If red light replaced by green light

V.F.B. (VIBR) : λ decreased pattern \rightarrow narrower

* If slit width narrower \rightarrow then \uparrow width = $\frac{2\lambda D}{a}$

pattern \rightarrow spread $\quad a \downarrow$

(6) position of first minima $\rightarrow \theta = \frac{\lambda D}{a}$

$$\text{position of first angular minima} = \frac{\lambda}{a}$$

Homework

Ex I \rightarrow 105, 104, 102, 101, 99, 97, 95, 94, 93, 92, 91, 89, 88, 86, 84

Ex II \rightarrow Q5, Q8, Q10, Q11, Q14, Q21, Q38

Ex III \rightarrow Q6, Q11, Q12

Solve Q \rightarrow 14, 15, 16, 17, 19, 20

Box 4 \rightarrow pura

Q99. $\lambda = 5000 \text{ \AA}$

distance of 1st minima = 5mm

$$D = 2 \text{ m}$$

$$a = ?$$

$$y = \frac{\lambda D}{a}$$

$$5 \times 10^{-3} = \frac{5000 \times 10^{-10} \times 2}{a}$$

$$a = \frac{5000 \times 10^{-10} \times 2}{5 \times 10^{-3}}$$

$$= \frac{2 \times 10^{-7}}{10^{-3}} = 2 \times 10^{-4}$$

$$= 0.2 \times 10^{-3}$$

$$= 0.2 \text{ mm}$$

$$\frac{600 \times 10^{-9}}{6.2} \times \frac{1.2 \times 10^{-3}}{2} \times \frac{1000}{2} \times 10^{-6} \times \frac{\pi}{10^4}$$

diff, convex, conductor
Ray optics

Saathi

Date / /

Q91 $d = 6000 \text{ \AA}$

$D = 2 \text{ m}$

$a = 0.2 \text{ mm}$

width of central maxima = 2γ

$$\frac{2\lambda D}{a} = \frac{2 \times 6000 \times 10^{-10} \times 2}{2 \times 10^{-4}}$$

$$\frac{12 \times 10^{-7}}{10^{-4}} = \frac{12 \times 10^{-3}}{1} = 12 \text{ mm}$$

Q95 $\lambda = 600 \times 10^{-9}$

$a = 1.2$

$\theta = ?$

$$\theta = \frac{\lambda}{a} = \frac{600 \times 10^{-9}}{1.2}$$

$$\frac{1}{2} = \frac{1.2}{2}$$

$$\theta = \frac{500 \times 10^{-9} \times \pi}{10^4 \times 360} = \frac{\pi}{6}$$

$a \sin \theta = n \lambda$

$a \sin \theta = \lambda$

$1.2 \times 10^{-3} \times \sin \theta = 600 \times 10^{-9}$

$\sin \theta = \frac{600 \times 10^{-9}}{1.2 \times 10^{-3}} \times \frac{1}{6.2}$

$\sin \theta = 1/2$

$\theta = \frac{\pi}{6} \text{ radian}$

38

Q98 $a = 0.6 \text{ mm}$

$\lambda = 4 \text{ nm}$

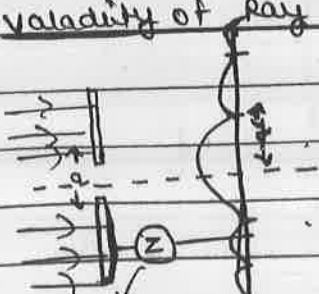
$\gamma = \frac{\lambda D}{a}$

$4 \times 10^{-9} = \frac{1.2 \times 10^{-3} \times 2}{a}$

$\frac{4 \times 10^{-9}}{2} = \frac{2.4 \times 10^{-6}}{a}$

500 nm

Validity of Ray optics -



1st minima

$\gamma = \frac{\lambda D}{a} \text{ (rad)}$

wave-optics dominate

$\gamma > a$

$\frac{\lambda z}{a} > a$

$\lambda z > a^2$

Fresnel distance

Date ___ / ___ / ___

Concept:-

AIIMS 2018. $\cos 15^\circ = ?$

$$\cos(45-30) = \cos 45^\circ \cos 30^\circ + \sin 45^\circ \sin 30^\circ$$

Break
If arbitrary
Value asked

$$= \frac{1}{\sqrt{2}} + \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} + \frac{1}{2}$$

$$= \frac{1}{2\sqrt{2}} [\sqrt{3} + 1]$$

Resolving power:-

NEET=2013

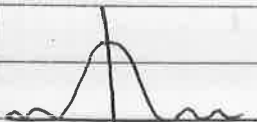
Telescope :- $R.P = \frac{d}{1.22 \lambda}$ → diameter of aperture of objective lens.

microscope :- $R.P = \frac{2.44 \sin \theta}{1.22 \lambda}$

$$R.P \propto \frac{1}{\lambda}$$

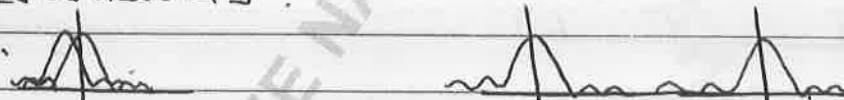
Ray criteria :-

$$R.P \propto \frac{1}{\theta}$$



[just resolved]

[clearly resolved]



2 points are just resolved by an optical system when central max. of diffraction pattern due to 1 falls on the 1st minimum of the diff. pattern of other objective lens.

NEET=2018 3-1081 Telescope मीत?

magnifying power ↑ = $\frac{f_o}{f_e}$ $\begin{matrix} f_o \uparrow \\ f_e \downarrow \end{matrix}$

resolving power ↑

EX III
Q6

diameter of aperture of objective lens
maxima

$$R.P = \frac{d}{1.22 \lambda}$$

$$a \sin \theta = (2n+1) \lambda / 2$$

1st maxima $\Rightarrow n=1$

$$a \sin \theta = \frac{3\lambda}{2}$$

Q11

angular width of central maxima = $\frac{2\lambda}{a}$ radian

$$\frac{3.14 \times 3}{9.42}$$

Saathi

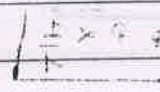
Date / /

$$\frac{21}{9} \times \frac{180}{\pi} \text{ degree}$$

$$\frac{2 \times 3600 \times 10^{-10}}{3} \times \frac{180}{3.14} \text{ degree}$$

$$\frac{10 \times 10^{-5} \times 10^{-2}}{3} \times \frac{180}{3.14}$$

$$\frac{360 \times 10^{-7}}{10^{-7} \times 9.42} = 38.2^{\circ} \text{ ANS}$$



SHREE NATHJI BOOK 7014774207